

# Graph Embedding based Tensor Analysis for Gait Recognition

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**Abstract**— Human gait recognition faces the challenge in feature extraction due to covariate conditions such as carrying and clothing, view angle, aging and other several. The large amount of data is generated while analyzing the silhouettes of an individual subject through different covariates. This leads to the higher computational cost and curse of dimensionality. In interest of paring down the same a graph embedding framework technique is enforced wherein any dimensionality reduction algorithm can be characterized in a common framework. An image when considered as a second order tensor helps in capturing the spatial relationship between the pixels. In this paper the tensor based dimensionality reduction algorithm is expressed through a graph embedding framework which helps to find out the hidden information lying in the lower dimensions of the manifold.

**Keywords**—Gait Recognition; Feature Extraction; Graph Embedding, Tensor.

## I. INTRODUCTION

Various biometrics like fingerprint, iris endeavor very good recognition rate but needs subject compliance under controlled environment. In contrast gait-as behavioral biometric allows flexibility to capture subject gait signature without approval and cooperation. The working resolution requirement offered by gait is very low. These set of advantages offer gait as unique candidate for video surveillance application. The number of attempts made by researchers to improve recognition rate under experimental environment but found to degrade performance in presence of diverse factor known as covariates. Thus robust human gait recognition offers unique challenge for feature extraction in presence of covariates. Different covariates can be classified as 1) Conditions that affect gait itself like shoes, injury, speed, pregnancy, affliction of the legs or feet, drunkenness and time i.e. increase in age and 2). Conditions that affect features extracted from gait are carrying condition, clothing condition, view angle etc.

## II. OVERVIEW OF GAIT RECOGNITION

Basic block diagram showing processing of video sequence of the silhouettes is shown in Figure 1. The human detection is attained by background subtraction and silhouette extraction methods. Since the obtained silhouette is in a raw format, it is normalized so as to make it unaltered for variation in zoom angle and alignment. To extract a gait cycle for analysis from binary

extracted silhouette the gait cycle extraction method is helpful wherein video sequence of one complete gait cycle is being mapped to single template; the process is called as temporal normalization. Mapping of temporal information, on to single template improves computational efficiency. Features extraction and discriminant analysis on gait template of walking person gives robust discriminative features that are stored in the database as training. In testing mode, discriminative features from sample under test are compared with the one from training set by classification scheme to recognize human identity.

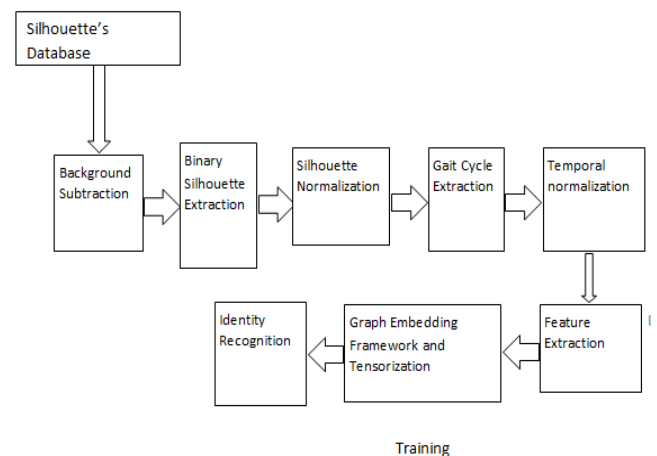


Figure. 1: Basic Block Diagram of Gait Recognition

### a. Background Subtraction and Binary Silhouette Extraction

Baseline algorithm proposed by Sarkaret. al [10] extracts the motion silhouette in each frame by background subtraction, within the semi-manually defined bounding boxes. For SOTON database the gait sequences are derived in the laboratory, aiming for near-perfect conditions to obtain the best possible silhouette [22]. The dynamic signature is obtained by chroma-key subtraction in conjunction with a connected components algorithm followed by windowing. Liang Wang et.al [20] has adopted change detection based on background subtraction. The improved version of background subtraction procedure can be applied to any realistic scene to extract moving silhouettes of walking figures from the background. The silhouettes are made binary so as to remove the coloring, intensity and illumination variation.

### b. Silhouette Normalization

The raw binary silhouettes are reprocessed for size and scale normalization so as to have uniform height. Also the horizontal alignment of each silhouette is achieved by centering the upper half silhouette part with respect to its horizontal centroid [14].

### c. Gait Cycle Extraction

The temporal information in the gait progression can be perpetuated with the help of gait period detection since the human walking pattern may be considered as periodical motion. Sarkaret. al [10] had detected gait periodicity by a counting the number of foreground pixels  $N_f(t)$  mostly from leg region from bottom half of the silhouette in each frame over time. Gait period is estimated by computing averaging median of the distances between minima, skipping every other minimum. Chen wang et.al [9] has proposed to use degree of the individual's two legs apart from each other to represent regular human walking. Height and alignment normalization is used to improve gait period detection.

## III. GAIT REPRESENTATION APPROACHES

Most of the gait recognition methods focus on gait representation approaches in order to make it robust against covariate conditions and computationally efficient. A good representation of gait should be able to discriminate, be robust to noise and changing covariate conditions, be space efficient and be easy to compute and manipulate. Based on the way gait is represented, the existing gait recognition approaches can be divided into two categories: model based and model free approaches.

### a. Model Based Approach

Model based approach represents gait using the parameters of a model of the body configuration. But this approach has menial achievement due to demand of high resolution images as input and subtlety to image noise, self-occlusion, shadows and view changes. This incurs a higher computational requirement.

### b. Model-Free Approach

The approach constructs gait descriptor from motion dynamics of human bodies and/or static shape information of silhouettes in compact form. This presentation is more robust to noise, insensitive to the quality of silhouettes and has the advantage of low computational costs. However, they are usually not robust to viewpoints and scale.

### c. Single Template Based Gait Recognition Approach

For the compact representation of gait sequence the approach converts video frames into a single image template. A gait cycle represented using a single image offers unique advantage of low computational complexity and robustness for noise in silhouette extraction. However, they are vulnerable to appearance changes of the human silhouette.

### d. Average Silhouette Representation

The average silhouette representation proposed by Liu and Sarkar[10] captures the shape of the template and temporal dynamics of gait. Thus many researchers have adapted this method as a choice.

Let the silhouette sequence which is partitioned into subsequences of gait period length, denoted by  $S_{pk} = \{S(k), L S(k + N_{pk})\}$ .

For each subsequence the silhouettes are averaged to arrive at a set of average silhouettes.

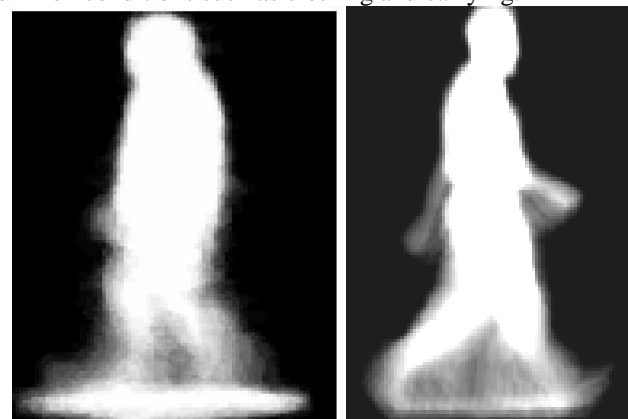
### e. Gait Energy Image

Another version of average silhouettes is the Gait Energy Image (GEI) proposed by Han and Bhanu [2]. GEI represents gait averaged over a complete cycle in a single grey scale image. Given preprocessed binary gait silhouette images at time  $t$  in a sequence, the grey level gait energy image (GEI) is defined as

$$G(x, y) = \frac{1}{N} \sum_{t=1}^N B_t(x, y) \dots (1)$$

This simple representation loses the dynamical variation between successive frames but has useful properties. (1) No silhouette alignment is required. (2) Space efficient compact representation of gait. (3) Reduced effect of noise because of the averaging procedure.

GEI representation captures explicitly the shape and dynamics of the subject. Pixels with high intensity values in a GEI correspond to body parts that move little during a walking cycle (e.g. head, torso), while pixels with low intensity values correspond to body parts that move constantly (e.g. lower parts of legs and arms). This explicit representation of shape makes the average silhouette (GEI) representation of gait vulnerable to appearance changes of the human silhouette caused by common conditions such as clothing and carrying.



(a) Average Silhouette

(b) Gait Energy Image

Figure. 2: Preprocessed Silhouettes

## IV. SPECTRAL REGRESSION AND SUBSPACE LEARNING

Dimensionality reduction has been always a challenge in pattern recognition and machine learning field. It preserves low dimensional features in order of increasing importance, making computationally efficient without compromising with discriminative effectiveness. The linear dimensionality algorithms such as PCA and LDA shows acceptable performance but face the challenges in real world problem when the data is sampled from nonlinear high dimensional space[5][12][13]. Other methods such as Locally Linear Embedding (LLE), ISOMAP and Laplacian Eigenmap (LE) which are classified as manifold learning methods reduces the dimensionality and preserves the

significant inter relationship. LLE and LE tries to preserve the local geometry of data by mapping the neighboring points in the lower dimensional subspace of manifold [7][16]. ISOMAP works with the global geometry by preserving it to local and global scales and mapping close points on the manifold to nearby points in low dimensional space and similar to farther points in the training dataset[7][18].

There are various endeavor have been made by minimizing objective function either with embedding function in linear or Hilbert space. But the computation turns up complex in time as well as in memory as it implicates Eigen decomposition of dense matrices[4][5][7][8]. Thus applying these methods to large datasets is futile. Some alternative approaches were attempted by applying a kernel view but these techniques are data dependent and produce no result for unnoticed data. Spectral Regression (SR) algorithm proposed by Deng Cai et.al.[7] is based on regression and spectral graph theory. The SR algorithm works with supervised, semi supervised and unsupervised data and provides efficient dimensionality reduction. To uncover intrinsic discriminative structure in the data, the SR technique constructs an affinity graph for labeled as well as unlabeled points in data and in turn the graph learns the responses from both types of points [7][19]. Moreover the general regression technique is then applied for learning the embedding function. SR provides the regression framework to learn the embedding functions which sidestep the issues with the Eigen decomposition computation for dense matrices.

#### V. GRAPH BASED TENSOR SUBSPACE ANALYSIS AND GRAPH EMBEDDING FRAMEWORK

The correlation between the nearby pixels of an image is essential for finding a projection. Recently there has been a lot of interest in extending the ordinary vector-based subspace learning approaches to tensor space. [6][15]

##### A. Graph Based Tensor Subspace Analysis

Let  $T \in R^{m_1} \otimes R^{m_2}$  be image represented as second order tensor capturing spatial relationship between the pixels and  $\{u_k\}_{k=1}^{m_1}$ ,  $\{v_l\}_{l=1}^{m_2}$  be an orthonormal basis of  $R^{m_1}$  and  $R^{m_2}$  respectively. Further, Deng Cai et.al [7] has shown that  $\{u_i \otimes v_j\}$  forms a basis of tensor space  $R^{m_1} \otimes R^{m_2}$ . The

projection of T on the basis  $u_i \otimes v_j$  is computed as their inner product as

$$Y = \langle T, u_i \otimes v_j \rangle = \langle T, u_i v_j^T \rangle = u_i^T T v_j$$

The vector based approaches are linear i.e.  $y_i = a^T X_i$  where  $X_i \in R^m$ ,  $a$  is projection vector and  $y_i$  is single dimensional embedding on the projection vector. Hence tensor based approach is multilinear with  $y_i = u^T T_i v$ . The tensor basis  $uv^T$  will have  $m_1 + m_2$  degrees of freedom with m values. The constraint for tensor approach by considering as a special case of the vector approach is as follows:

$$a_{i+m_1(j-1)} = u_i v_j$$

where  $a_i, u_i$  and  $v_j$  are the i-th elements in  $a, u$  and  $v$  respectively.

##### B. Graph Embedding Framework

Graph embedding is a common framework which offers the unified view for the analysis of popular dimensionality reduction algorithms [1][3][5]. In order to minimize computational complexity of dimensionality reduction algorithms these are represented in graph embedding framework. Graph embedding methods represent each vertex of a graph as a low-dimensional vector that preserves similarities between the vertex pairs, where similarity is measured by a graph similarity matrix that characterizes certain statistical or geometric properties of the data set. The vector representations of the vertices can be obtained from the eigenvectors corresponding to the leading eigenvalues of the graph Laplacian matrix with certain constraints. [1][3][5]

#### VI. TENSOR LOCALITY PRESERVING PROJECTION

Tensor Locality Preserving Projection (TLPP) method which can be applied in a supervised or semi supervised fashion provides a way to linearly approximate the eigenfunctions of the Laplace Beltrami operator in a tensor space. Hence it can model the geometric and topological properties of an unknown manifold embedded in a tensor space with some data points sampled randomly from the manifold. Based on  $n$  data points  $A_1, \dots, A_n$  from a manifold  $M \subset R^{I_1 \times \dots \times I_k}$ , local geometric structure of  $M$  can be constructed using graph  $G$ . The affinity matrix is defined as  $S = [S_{ij}]_{n \times n}$  which is defined based on heat kernel as:

$$s_{ij} = \begin{cases} \exp\left(-\|A_i - A_j\|_2^F / t\right) & \text{if } A_j \in O(K, A_i) \\ & \text{or } A_i \in O(K, A_j); \dots (2) \\ 0 & \text{otherwise.} \end{cases}$$

Let  $U_i \in R^{I_i \times I_i}$  ( $i=1, \dots, k$ ) be the corresponding transformation matrices. Based on the neighborhood graph  $G$ , the optimization problem for TLPP can be expressed as:

$$\begin{aligned} & \arg \min Q(U_1, \dots, U_k) \\ & = \sum_i \|B_i - \sum_j s_{ij} B_j\|_F^2 \\ & = \sum_{i,j} \|A_{i \times 1 \dots \times k} U_k - A_{j \times 1 \dots \times k} U_k\|_F^2 s_{ij}, \\ & \text{s.t } \sum_i \|A_{i \times 1 \dots \times k} U_k\|_F^2 d_{ii} = 1 \quad \dots (3) \end{aligned}$$

If the points  $A_i$  and  $A_j$  are far apart then the objective function suffer from high penalty. Higher the value of the  $d_{ii}$  the point that is represented by  $A_i$  is more important in the tensor space. Let  $y_i^f$  be denoted as  $A_i \times_1 U_1 \dots \times_{f-1} U_{f-1} \dots U_k$ . The optimization function that is based on tensor properties as well as on trace is as follows:

$$\begin{aligned} & \arg \min P_f(U_f) \\ & = \text{tr} \left\{ U_f^T \sum_{i,j} s_{i,j} (Y_i^{(f)} - Y_j^{(f)}) (Y_i^{(f)} - Y_j^{(f)})^T U_f \right\}; \end{aligned}$$

$$\text{s.t } \text{tr} \left\{ U_f^T \sum_{i,j} s'_{i,j} (Y_i^{(f)} - Y_j^{(f)}) (Y_i^{(f)} - Y_j^{(f)})^T U_f \right\} = 1 \dots (4)$$

Since the information lies in the lower dimension of manifold; solving for the eigenvectors corresponding to the  $l$  smallest eigenvalues in the generalized eigenvalue equation

$$\left( \sum_{i,j} (Y_i^{(f)} - Y_j^{(f)}) (Y_i^{(f)} - Y_j^{(f)})^T s_{ij} \right) u = \lambda \left( \sum_i Y_i^{(f)} Y_i^{(f)T} d_{ii} \right) u \dots (5)$$

The computation of the matrix  $U_f$  called as transformation matrix which is unknown can be obtained by solving for the smallest eigenvalue as above.

TLPP Algorithm: [1][3][5][8]

Input:  $A_1, \dots, A_n$  from  $M \subset R^{l_1 \times \dots \times l_k}$  and  $l_1 \times \dots \times l_k$ .

Step 1. Construct G and compute S;

Step 2. Steps for computation of embedding are as follows:

Initialize  $U_1^0 = I_{l_1}, \dots, U_k^0 = I_{l_k}$ ;

For  $t = 1, \dots, T_{\text{maxd}}$

For  $f = 1, \dots, k$

$$y_i^f = A_i \times_1 U_1 \dots \times_{f-1} U_{f-1} \times_{f+1} U_{f+1} \dots \times_k U_k ;$$

$$y_i^f \Rightarrow_f Y_i^{(f)} ;$$

$$H_1 = \sum_{i,j} (Y_i^{(f)} - Y_j^{(f)}) (Y_i^{(f)} - Y_j^{(f)})^T s_{ij} ;$$

$$H_2 = \sum_i Y_i^{(f)} Y_i^{(f)T} d_{ii} ;$$

$$H_1 U_f^t = H_2 U_f^t A_k, U_f^t \in R^{l_f \times l_f} ;$$

if  $\|U_f^t - U_f^{t-1}\|_F < \epsilon$  for each  $f$  then

break;

end if

end for

end for

Output:  $U_i = U_i^t \in R^{l_i \times l_i} (i = 1, \dots, k)$

### VII. EXPERIMENTAL RESULTS:

The USF gait dataset consists of 1870 silhouette sequences from 122 subjects spanning 5 covariate conditions. Each sample is third-order tensors of size  $32 \times 22 \times 10$ . The total samples used are 731. The histogram count computed is a vector of 71 values.



Figure. 3: Binary Silhouettes

Results:

Table I. shows results for proposed algorithm on USF dataset for rank 1 and rank 5 recognition rates.

Table I: Recognition Rate on USF database

| Probe   | Variation                      | Total Objects | Covariates Difference Between Gallery and Probe | Rank 1 | Rank 5 |
|---------|--------------------------------|---------------|---|--------|--------|
| A       | (G, A, L, NB, t <sub>i</sub> ) | 122           | View  | 73     | 85     |
| B       | (G, B, R, NB, t <sub>i</sub> ) | 54            | Shoe  | 62     | 75     |
| C       | (G, B, L, NB, t <sub>i</sub> ) | 54            | View, Shoe                                      | 35     | 65     |
| D       | (C, A, R, NB, t <sub>i</sub> ) | 121           | Surface   | 22     | 32     |
| E       | (C, B, R, NB, t <sub>i</sub> ) | 60            | Surface, Shoe                                   | 14     | 28     |
| F       | (C, A, L, NB, t <sub>i</sub> ) | 121           | Surface, View                                   | 8      | 25     |
| Average |                                |               |   | 35.67  | 51.6   |

### VIII. CONCLUSION

Pertaining to the tensor embedding methods which accepts data directly in the form of tensors of arbitrary order as input, TLPP algorithm has been applied to the gait images. This method exploits the intrinsic local geometric and topological properties of the manifold; they are pleading in terms of dimensionality reduction. For gait recognition experiments based on the USF dataset, tensor embedding methods gives a profound result with binary silhouettes.

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