Reversible Data Hiding in JPEG Images with Multi-objective Optimization

Zhaoxia Yin, Member, IEEE, Yuan Ji, Bin Luo

Abstract—Among various methods of reversible data hiding (RDH) in JPEG images, the consideration in designing is only the image quality, but the image quality and the file size expansion are equally important in JPEG images. Based on this situation, we propose a RDH scheme in JPEG images considering both the image quality and the file size expansion while designing the algorithm. The multi-objective optimization strategy is utilized to realize the balance of the two objectives. Specifically, the cover is divided into several non-overlapping signals firstly, and after that, the embedding costs of signals are calculated using the knowledge of the JPEG compression. Next, the optimized combination of signals for embedding data is gained by the multi-objective optimization. Experimental results show the better performance of our proposed RDH compared with state-of-the-art RDH in JPEG images.

Index Terms—reversible data hiding, JPEG images, multiobjective optimization, histogram shifting.

I. INTRODUCTION

N OWADAYS, data is abundant and exists everywhere, and the importance of data privacy is getting more and more attention, so the technology of data hiding is developing fast. The traditional way of protecting data is encryption, but it can expose the transmission way of additional data. Then, data hiding appeared to make up for this shortcoming, it can hide the additional data into cover medium which can be shared publicly, so the behavior of transferring additional data is invisible. As technology advances, some applications have more requirements for data hiding, they may need both the additional data and the cover be lossless. That is to say, the cover must be fully recovered after the additional data is extracted. This technology is named reversible data hiding (RDH) [1]–[9], it can be employed in many fields, such as military, medicine, forensics and so on.

Image is a frequently used form of data in our daily life, so many RDH algorithms are designed on images. Furthermore, the Joint Photographic Experts Group (JPEG) is a widely used image format in the network, thus the research of RDH in JPEG images is very popular. The RDH in spatial domain is growing rapidly, but the corresponding algorithms cannot be directly utilized in JPEG images, that is because the RDH in spatial domain is designed using the redundancy of images and the JPEG images are obtained by compressing the redundancy of spatial domain images which means there is less redundant space in JPEG images. In addition, the RDH in spatial images

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TABLE I THE DIFFERENCES OF RDH IN SPATIAL DOMAIN AND JPEG DOMAIN.

needn't consider the file size, but the RDH in JPEG images which are compressed format must take it into consideration. Here, table I gives the differences of RDH in spatial domain and JPEG domain. Obviously, the file size is also an important metric for RDH in JPEG images except for the image quality and the payload because the compression of images is to reduce the file size of images.

RDH in JPEG images has also developed in recent years. It can be divided into four categories. The first one is based on the lossless compression first proposed in [10], this paper includes not only method based on lossless compression but also the data hiding approach through modifying quantization table according to their parity. The next method is based on the quantization table modification [10], [11]. Wang et al. proposed a RDH scheme that modifies the DCT coefficients to embed data while the corresponding values in the quantization table make changes [11]. It can achieve good effects both in capacity and image quality, but the file size is relatively large. The third method is based on modifying the Huffman table [12]-[14] which can well keep the file size of JPEG image unchanged. However, its embedding capacity is rare. The fourth category is the method based on the modification of quantized DCT coefficients [15]-[21]. In 2016, Huang et al. [15] applied the histogram shifting (HS) in the RDH scheme for JPEG images, where some non-zero AC coefficients valued '1' and '-1' are used as the peak points to embed additional data, and other non-zero AC coefficients shift to make room for additional data while the remaining coefficients keep unchanged. And Huang et al. took a block selection strategy which is based on the number of zero AC coefficients in the block to decide which block is chosen to embed data first. Good image quality and embedding capacity are realized in [15], besides, the file size is kept well. Then Wedaj et al. [16] proposed an improved RDH in JPEG images based on the new coefficient selection strategy, which is improved on the

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 TABLE II

 THE CONSIDERATIONS OF RDH IN JPEG DOMAIN.

considerations	Rate and distortion performance	File size expansion
Huang et al. [15]	\checkmark	
Hong <i>et al.</i> [17]	\checkmark	
Hou <i>et al.</i> [19]	\checkmark	
Proposed scheme	\checkmark	\checkmark

basis of Huang *et al.*'s work. The additional data is embedded according to the embedding cost in each position of the block. In addition, Hong *et al.* [17] and Hou *et al.* [19] also made improvement on the basis of the work of Huang *et al.*. Hou *et al.* [19] proposed a method based on DCT frequency and block selection. They considered the influence of the quantization step in quantified DCT coefficients' change and simulated distortion in blocks before embedding, the scheme combines the selection strategy of [15] and [16]. The method can keep good visual quality and also keep a small expansion in file size. Liu *et al.* [20] utilized difference expansion(DE) in RDH scheme for JPEG images which obtains high capacity but the quality of the image is not so good. Because this method modifies the quantized coefficients to a large extent and it causes bigger distortion.

From all of the above, we can see that image quality and embedding capacity are very important, and file size is equally important for RDH in JPEG images. However, the past all works haven't taken the file size into consideration separately while designing methods. Here, we use file size expansion to better display the changes of the cover file size after embedding data. And Table II shows the considerations of RDH in JPEG images while designing the algorithm. It is clear that the state-of-the-art RDHs in JPEG images don't take the file size expansion into account. Thus, we propose a scheme combining not only the rate and distortion performance but also the file size expansion. An optimization strategy is used to balance the two called multi-objective optimization which will achieve different effects according to different requirements. In addition, the distortion and file size expansion of JPEG images are well designed to better map to the image quality and file size. Experiment results show that the method outperforms the previous works in both image quality and file size expansion.

In this paper, several sections are displayed in the following. Section II gives the related works which explain some theory acknowledges and some other schemes. And the detail of the proposed scheme is shown in Section III. Section IV displays the experimental results, then the paper ends by summarizing our work in SectionV.

II. RELATED WORKS

In order to better display our proposed scheme, the prerequisite knowledge is shown first. The compression of the spatial images to the JPEG images can help to well design the RDH scheme by its characteristic or easily comprehend the principle of some RDH schemes in JPEG images. What's more, in our scheme, a multi-objective optimization math model is used to explain the target of RDH in JPEG images: minimize the file size expansion and the distortion simultaneously. Thus, the overview of JPEG compression and the multi-objective optimization are demonstrated in this section. And the based schemes which we improve on are also displayed here.

A. Overview of JPEG Compression

The essence of compression is to remove or reduce redundant information in images, so the file size of compressed images can be small. The procedure of JPEG compression is shown in Fig. 1. First, the image is divided into nonoverlapping 8×8 sized blocks. Next, do the DCT transformation on the divided blocks, and this process can be described by (1).

$$F(u,v) = \frac{1}{4}c(u)c(v\sum_{x=0}^{7}\sum_{y=0}^{7}f(x,y)\cos\frac{(2x+1)u\pi}{16}\cos\frac{(2y+1)v\pi}{16},$$
(1)

where,

$$c(u) = \begin{cases} \frac{1}{\sqrt{2}}, & \text{if } u = 0\\ 1, & otherwise, \end{cases}$$
(2)

and (x, y) represents the index of a pixel in the spatial image, f(x, y) is the pixel value in the position (x, y), (u, v) is the index of a coefficient in JPEG images, and F(u, v) is the DCT coefficient value in the position (u, v).

After the DCT transformation, the DCT matrix is gained and the coefficients are called DCT coefficients. Moreover, in each block, the first coefficient is named DC coefficient and the other 63 coefficients are AC coefficients. Then, the quantization is performed on the DCT matrix using the predefined quantization table for different quality factor (OF), the specific operation is that the DCT matrix divides by the quantization table point by point. Fig. 2 is a standard quantization table when QF=50, every position in the 8×8 sized block is called a frequency. The process of quantization causes the loss from spatial images to JPEG images, and the QF represents the degree of compression, smaller the QF the more compression. Till now, we get the compressed data, quantized DCT coefficients, which our proposed method makes modification on in this paper. The compression is done, and the quantized DCT coefficients have to be coded. Due to the different characteristics of DC and AC coefficients, different coding methods are taken. Adopt Differential Pulse Code Modulation (DPCM) to encode the DC coefficients because of the correlation of DC coefficients between adjacent blocks, and Run Length Encoding (RLE) to encode AC coefficients, besides, the AC coefficients valued '0' don't need to be encoded. After the DPCM and RLE, the Huffman encoding is further used to acquire the final binary coding of quantized DCT coefficients. And the file size is tightly close to the coding length of quantized DCT coefficients, so keeping the coding length is a good way to keep file size.

From the process of compressing the spatial images to the JPEG images, we can clearly see that the DCT procedure changes the distribution of coefficients, and the quantization achieves the essence of compression. Hence, the quantization



Fig. 1. The generation process of JPEG image.

16	11	10	16	24	40	51	61
12	12	14	19	26	58	60	55
14	13	16	24	40	57	69	56
14	17	22	29	51	87	80	62
18	22	37	56	68	109	103	77
24	35	55	64	81	104	113	92
49	64	78	87	103	121	120	101
72	92	95	98	112	100	103	99

Fig. 2. The standard quantization table when QF = 50.

table helps a lot in reducing the file size expansion while designing the RDH scheme in JPEG images.

B. Multi-objective Optimization

Multi-objective optimization refers to maximizing or minimizing multiple objectives while designing work, and satisfying constraints. In general, the sub-goals of the multi-objective optimization problem are contradictory. The improvement of one sub-goal may cause the performance of the other subgoals to be degraded, that is, to simultaneously optimize the multiple sub-goals is not possible, but they can be coordinated and compromised among themselves so that each sub-goal is optimized as much as possible. There are basically the following methods for solving multi-objective optimization: one is to reduce the multi-objective into a single objective which is easier to solve, such as main target method, linear weighting method, ideal point method, etc. The other is called the hierarchical sequence method, that is, the target is given a sequence according to its importance, and each time the next target optimal solution is found in the previous target optimal solution set until the common optimal solution is obtained. It can also be modified by the simplex method. Another method called analytic hierarchy process is a multi-objective decision-making and analysis method combining qualitative and quantitative methods, and it is more practical for the case where the target structure is complex and lacks necessary data.

The general multi-objective model is shown as (3) and (4), where $X = [x_1, x_2, ..., x_n]^T$ is the independent variable, and $f_i(X)$ is the *i*-th objective that needed to be maximized or minimized, $\phi_j(X) \leq g_j$ is the *j*-th constraint, and there are *n* variables, *k* objectives and *m* constraints in (3) and (4). The final goal is to maximize or minimize the *k* objectives while satisfying m constraints by changing the independent variable X. Moreover, the number of variables, objectives and constraints will make great differences in the final result including the running time and the optimized result.

C. Other Schemes

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The multi-objective optimization is employed to minimize the distortion and the file size expansion in RDH for JPEG images, and it is adopted on the basis of other schemes in this paper. Therefore, the other schemes that we improve on are displayed here.

1) Huang et al.'s scheme: Huang et al. proposed a RDH scheme for JPEG images using the existing HS technology, they analyzed the characteristics of DC and AC coefficients and found that the DC coefficients are rather flat in histogram while the AC coefficients are sharper. And another reason they chose the AC coefficients to embed additional data is the changes in DC coefficients may make great distortion in JPEG images because of their containing more information of JPEG images. What's more, it can be seen that in the histogram of AC coefficients, the amplitude of value '0' is the largest and the amplitude of absolute value '1' is the second largest. But for the sake of file size expansion, the AC coefficients valued '0' are not considered to embed data. And then, the AC coefficients valued '1' and '-1' are chosen to embed data combining HS. After the embedded coefficients are determined, which block is selected to embed data first should be taken into account. They selected the block according to the number of AC coefficients valued '0' in the block, the number is smaller, the order of block is later. In general, the block with more AC coefficients valued '0' means flat block, that's to say, there will be less distortion in this block. Following the two stages, coefficients choice and block selection, additional data is embedded into the chosen



Fig. 3. The embedding process of Huang et al.'s scheme.

coefficients in selected blocks. In addition, the embedding process of Huang et al.'s scheme is shown in Fig. 3.

The scheme achieves good image quality and low file size expansion. And the block selection strategy is proposed first for RDH in JPEG images in [15]. Huang *et al.*'s work made a great push in RDH for JPEG images, but the scheme only considers the smoothness of blocks, and the number of AC coefficients valued '0' cannot exactly represent the smoothness. From the overview of JPEG compression, we can see that the coefficients in JPEG images are not the same as the one in spatial images, they are got by the process of DCT and quantization. The quantization table has influence on the distortion that distortion will be different for the same coefficients in different positions.

2) Hou et al.'s scheme: Hou et al. designed a RDH scheme for JPEG images on the basis of Huang et al.'s work, they made up for the shortcoming of Huang et al.'s work that the quantization table is not taken into consideration. First, this method calculates the average distortion of each frequency in the quantized DCT blocks. Second, select the top K frequencies according to the descending order of the average distortion of each block with only K frequencies. Fourth, select the K frequencies of blocks with small distortion to embed data. Finally, do the cycle from second to fourth to choose different K to search for the best PSNR of the stego image.

The stage of calculating the average distortion of each frequency in the quantized DCT blocks is the embodiment of considering the quantization step. And the average distortion value is evaluated by (5)-(7):

$$cost(u,v) = \frac{\sum_{x=0}^{7} \sum_{y=0}^{7} \Delta f(x,y)^2}{64},$$
(5)

$$J_{u,v} = (0.5 * C_{u,v} + C_{out}) * cost(u,v),$$
(6)

$$UD_{u,v} = \frac{J_{u,v}}{C_{u,v}},\tag{7}$$

where u, v represent the position of frequency, $\Delta f(x, y)$ means the modification in the spatial image that caused by the operation in the JPEG domain, and it can be gained by (14), and cost(u, v) indicates the frequency (u, v)'s corresponding distortion in the spatial domain. $C_{u,v}$ is the number of AC coefficients valued '1' and '-1', C_{out} means the number of AC coefficients whose absolute values are bigger than 1, $J_{u,v}$ shows the total distortion of the frequency (u, v) in all blocks, $UD_{u,v}$ means the averge distortion of each frequency which is the basis for frequency sorting. What can be seen is that the quantization table is fully utilized in the compute of cost(u, v).

It is undeniable that Hou et al.'s method has achieved better effects in image quality and file size expansion. However, the methods of Huang et al. and Hou et al. consider only the distortion, and the file size is not considered separately. Besides, the block selection strategy also can be improved, both of the two methods embed data sequentially in descending order of distortion in blocks. But there may exist some situations that the combination of two blocks with large distortion is better than three combinations with less distortion in the result of distortion and file size. The multi-objective optimization can solve the two disadvantages by its model and the balance of distortion and file size expansion.

III. PROPOSED SCHEME

In this section, the proposed scheme is detailed. The framework of the proposed algorithm is shown in Fig. 4. We can see from the figure that the how to get the optimized signal combination is the last step before embedding data and it is the core step of our proposed scheme, so the multi-objective optimization is applied in our method to get the optimized signal combination. And the math model suitable for our proposed scheme is described here. Moreover, the costs sets of RDH in JPEG images include three aspects: the embedding capacity, the distortion and the file size expansion. And the embedding capacity is fixed in our proposed scheme for using HS in [15], besides, it is significant to better measure the distortion and the file size expansion of the cover. In the following of this section, the calculation of the three costs is described in detail.

A. Math Model

The metrics of RDH in JPEG images are the payload, image quality, and file size. The ultimate goal of the algorithm is making the image quality best and minimizing the file size while keeping the payload. Thus, the goal in RDH in JPEG images with multi-objective optimization are the image quality and file size, the constraint is the payload. According to the characteristics of objectives in our problems that the file size may decrease as the image quality improve, this paper uses the main target method to solve the multi-objective optimization.

In order to facilitate the visual display of the multi-objective optimization formula of RDH in JPEG images, several mathematical parameters are used here to represent the various information of the JPEG image. The cover is divided into k equalsized blocks to form a signal set S, that $S = \{s_1, s_2, ..., s_k\}$,

Fig. 4. The proposed multi-objective optimization embedding process.

here, s_i represents the *i*-th signal. Correspondingly, R is a set of embedding capacity of each signal, $R = \{r_1, r_2, ..., r_k\}$, similarly r_i denotes the capacity of the *i*-th signal. D is the image distortion cost set, $D = \{d_1, d_2, ..., d_k\}$, and d_i means the distortion of the *i*-th signal after embedding data. E is the file size expansion cost set, $E = \{e_1, e_2, ..., e_k\}$, also e_i indicates the *i*-th signal's file size expansion after embedding data. After JPEG image is represented by these mathematical parameters, the math model can be designed as (8):

$$\begin{cases} \min(V \times E^T) \\ \min(V \times D^T) \\ s.t. \quad C - V \times R^T \le 0, \end{cases}$$
(8)

where V is the decision variable, expressed in the form of $V = \{v_1, v_2, ..., v_k\}$, besides, $v_i \in \{0, 1\}$, and if v_i equals 0, the *i*-th signal will not be used to embed data, in the contrast, if v_i equals 1, the *i*-th signal will be selected for embedding. In addition, the $V \times E^T$ represents the total file size expansion, the sum of the file size expansion in the selected signals. And $V \times D^T$ means the total distortion, the sum of distortion after embedding in the selected signals. In addition, min is the minimization function making our goal minimized, C is the length of the additional data and $V \times R^T$ represents the total embedding capacity of the selected signals, and $C - V \times R^T \leq 0$ is the constraint that the selected signals must satisfy the payload.

$$\min \quad V \times D^{T}$$

$$s.t. \begin{cases} C - V \times R^{T} \le 0 \\ V \times E^{T} \le E^{*} + \alpha E^{*}, \end{cases}$$
(9)

To better solve this multi-objective problem and reduce the computational complexity, we convert one of the goals into a constraint like (9). The model in (9) means that we convert the file size expansion into a constraint and minimize the distortion, where E^* is the optimal value of the target file size expansion, and the $E^* + \alpha E^*$ is the limit of file size expansion in the model and the weight α means the degree of constraint that the file size expansion needs to satisfy. Applying (9), the multi-objective optimization problem in the proposed scheme can be solved very well.

B. Costs Getting

1) embedding capacity: The embedding capacity of each signal is the number of data each signal can embed, and it is depending on the embedding method. If the adopted embedding method is HS in AC coefficients, then the embedding capacity is the number of AC coefficients which are selected to embed, usually valued '1' and '-1'. All the coefficients that can embed data are embeddable coefficients. In our proposed scheme, HS is utilized to embed data as Huang *et al.*'s

scheme, so the signal embedding capacity is the number of AC coefficients valued '1' and '-1' in each signal.

$$r_i = \sum_{j=2}^{64} sign(s_{ij}),$$
 (10)

$$sign(s_{ij}) = \begin{cases} 1, & \text{if } s_{ij} \text{ is embeddable coefficient} \\ 0, & \text{if } s_{ij} \text{ isn't embeddable coefficient.} \end{cases}$$
(11)

The embedding capacity r_i of each signal s_i is computed by (10), where s_{ij} represents the *j*-th coefficient in the *i*-th signal, and $sign(s_{ij})$ means whether s_{ij} is embeddable or not.

2) distortion designing: Image quality is a criterion to measure the performance of the RDH in JPEG images, so the distortion function is designed to reflect the image quality which is inversely proportional to it. And the image quality is reflected in the spatial domain, but we modify the coefficients in the DCT domain to embed data. Therefore, if we want to detect the distortion in spatial images using the modification in quantized DCT coefficients, we must establish a link from the DCT domain to the spatial domain for distortion. We can analyze from the generation process of JPEG images shown in section II-A that the inverse quantization and the inverse DCT transformation should be executed in order on the modification of the quantized DCT coefficients to exactly reflect the modification in spatial images. And the inverse process is displayed in Fig. 5. According to the theoretical analysis, the distortion function in [19] is designed very well, so we use it as our distortion function to measure the image quality, and it is shown following:

$$d_i = IDCT(diff. * Q), \tag{12}$$

$$diff = s_i - s'_i,\tag{13}$$

Assume that s'_i is the current signal that emulates embedding the additional data, s_i is the original signal, diffrepresents the modification of quantized DCT coefficients due to the embedding of additional data. The operator .* means multiplying point by point. Q displays the quantization step, and diff.*Q is the process of inverse quantization. IDCT is the function that does inverse DCT transformation, the compute of IDCT transformation is as (14):

$$f(x,y) = \frac{1}{4} \sum_{u=0}^{7} \sum_{v=0}^{7} c(u)c(v)F(u,v)\cos\frac{(2x+1)u\pi}{16}\cos\frac{(2y+1)v\pi}{16},$$
(14)

where F(u, v) represents the coefficient in quantized DCT matrix, (u, v) is the index of position of the coefficient in quantized DCT matrix, and c(u), c(v) is the same meaning as that in (2). Besides, (x, y) is the index of position of the pixel in the spatial domain. After two inverse transformations,



Fig. 5. The distortion calculation in the spatial domain caused by changes in the DCT domain.

the changes in the DCT domain are well mapped to the spatial domain, and then it can well reflect the quality of stego images.

3) file size designing: The significance of file size expansion during embedding is obvious from the analysis in section I and III-A. But the file size has never been considered separately in the design of existing RDH in JPEG images. How to design the file size expansion of a signal is very important.

$$e_i = \frac{L(s'_i) - L(s_i)}{L(s_i)} \times 100\%,$$
(15)

The file size expansion can be calculated by (15), where s_i is the *i*-th signal in the cover, and $L(s_i)$ is the function to count the coding length of the signal s_i . And e_i means the ratio of the stego signal file size to the original signal file size in each signal s_i , which is the percentage increase of the file size after embedding. We use the percentage increase of the file size instead of the file size to measure the effects of the scheme, that is because the percentage can intuitively reflect the file size changes in the original signal.

C. Data Embedding and Extraction

There will give the processes of data embedding and extraction, and the embedding method is the HS which is the same as the method in [15], where the AC coefficients valued '1' and '-1' are used to embed additional data, if the data is '0', the embeddable coefficients keep unchanged, if the data is '1', the embeddable coefficients move to a direction with a large absolute value by 1. The other AC coefficients whose absolute values are bigger than the embeddable coefficients shift to a direction with a large absolute value by 1, and the AC coefficients valued '0' is immovable.

1) Data embedding:

- Get the quantized DCT coefficients from the original JPEG image by decoding.
- Divide the DCT coefficients into some non-overlapping signals of the same size according to different schemes. The size of the signal in this paper is 8×8, but it can be any size.
- Compute the corresponding distortion cost, file size expansion and embedding capacity of each signal in the signal set applying the (10)-(15).
- Adopt the multi-objective optimization proposed in section III-A to generate the decision variable matrix V used to guide which signal is selected to embed data into. Notice that the multi-objective optimization function must satisfy the given payload, meanwhile, the distortion and file size expansion are optimal.
- Embed the additional data into the signals according to the decision variable matrix V.

• Encode the modified JPEG image to get the stego image.

What has to be aware of is that the decision variable matrix V is needed to be compressed, and then it replaces the LSBs of some special signals in the signal set like the first or the last signal, next, the LSBs of these signals are embedded following the additional data.

2) Data extraction:

- First, the quantized DCT coefficients are gained from the stego JPEG image in the same way as the first step in section III-C1.
- Perform the same block processing on the quantized DCT coefficients as embedding to obtain signals of the same size that do not overlap.
- Extract the data and recover the signals according to the decision variable matrix V. And the decision variable matrix V is extracted first from the LSBs used in the embedding process.
- Encode the recovered signals again to get the recovered JPEG image which is the same as the original JPEG image.

IV. EXPERIMENTAL RESULTS

In this section, we display the better performance of our proposed scheme in the image quality and the file size expansion based on Huang et al.'s scheme and Hou et al.'s scheme. Four gray images with size of 512×512 , Airplane, Baboon, Lena, Peppers shown in Fig. 6 are used to produce the cover signal set in our experiment. And they are compressed to JPEG images with different quality factors (QF=30,50,70,90), and also 96 gray images [22] sized 512×512 are applied to test the average performance of experiments. Besides, the weight α in (9) we used is set to 1, if it is too small, the optimal decision variable matrix cannot be gained, because the file size expansion is limited to a too small range, and if the weight is large, the optimal decision variable matrix will keep unchanged. Therefore, we choose 1 as the optimal weight according to the best result of our experiments on different weights. We discuss the performance of the algorithm as following.

A. Influence of quantization step

The impact of quantization step has been mentioned in the previous section. Fig. 7 gives the influence of quantization step in different quantization tables, different QFs correspond to different standard quantization tables. The abscissa indicates the position of the quantization step in quantization table, and it changes from 1 to 64, which means there are 64 quantization steps in the 8×8 DCT matrix. The ordinate represents the corresponding change in the spatial domain if there is one-bit change of DCT coefficient in one position. We test the



Fig. 6. Four test images sized 512×512. (a)Airplane. (b)Baboon. (c)Lena. (d)Peppers.



Fig. 7. The changes of coefficients in spatial domain while modifying one-bit in different frequencies of the quantization table.

influence of quantization step using the modification in the spatial domain which can be mapped by the corresponding change in the DCT domain. The DCT coefficient of only one position is changed by one bit at a time, and then the corresponding change in the spatial domain is calculated by the inverse quantization and IDCT transformation which is shown in (12)-(14). The influences of the quantization step are clearly to be seen from Fig. 7, the low amplitude means fewer changes in the spatial domain, and it indicates the less distortion. The different influences of different positions are evident, so the quantization step is applied in our distortion

function designing to well reflect the changes in spatial domain which are caused by embedding additional data in the DCT coefficients. From the general trend, we can observe that the lower the position, the smaller the distortion will be.

The comparisons with [15] and [19] are both based on the average results of 96 images for better contrast. Farther, the results of the four test images are also shown in Table III and Table IV to clearly see the improvement. The reason why the proposed method compares with the other two schemes individually is that the proposed method is carried on the basis of each scheme.

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Fig. 8. Average PSNR and the file size expansion under different payloads between the proposed method and Huang et al.'s [15] method.

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	Payload(bit	ts)	2000	4000	6000	8000	10000
		PSNR(dB)	44.73	40.77	38.12	36.1	34.26
Lena OF=30	Huang et al. method [15]	increasement(bits)	2360	5152	8160	11072	14192
Lena QI =50		PSNR(dB)	45.28	41.63	38.8	36.52	34 41
	Proposed method	increase mont(bits)	2000	4272	7032	10032	12606
	D 1 141	increasement(bits)	2000	4272	10000	10032	1,1000
	Payload(bit	ts)	6000	8000	10000	12000	14000
	Huang et al' method [15]	PSNR(dB)	42.69	40.75	38.98	37.37	35.89
Lena QF=50	fitting et al. method [15]	increasement(bits)	8248	11056	14296	17376	20512
-		PSNR(dB)	43.31	41.19	39.45	37.74	36.02
	Proposed method	increasement(bits)	7176	10048	12920	16512	20280
	Payload(bit	te)	4000	8000	12000	16000	20000
	1 ayload(bi	DENID(JD)	40.00	45.26	12000	20.84	27.05
	Huang et al.' method [15]	PSINK(dB)	49.21	43.50	42.42	39.84	37.23
Lena QF=/0	0	increasement(bits)	5696	111/6	16952	23536	30520
	Proposed method	PSNR(dB)	49.72	45.66	42.85	40.10	37.27
	r toposed method	increasement(bits)	4616	9832	15728	22248	30360
	Payload(bit	ts)	17000	22000	27000	32000	37000
	, , , , , , , , , , , , , , , , , , ,	PSNR(dB)	47 88	45 93	44 10	42.31	40 57
Lena OE-90	Huang et al.' method [15]	increasement(bits)	23848	31776	39976	48760	57256
Lena QI =90		DCND(1D)	47.07	45.00	14.10	40700	10.64
	Proposed method	PSNR(dB)	47.97	45.98	44.19	42.40	40.64
	1	increasement(bits)	22288	30264	38512	47704	56728
	Payload(bit	ts)	7000	12000	17000	22000	27000
		PSNR(dB)	36.79	33.06	30.57	28.75	27.25
Baboon OF=30	Huang et al. method [15]	increasement(bits)	10080	17120	24920	32272	39704
		PSNR(dB)	37.13	33.42	30.89	29.02	27 33
	Proposed method	in anna a ann an t(hita)	9576	15550	22824	20784	28026
		Increasement(bits)	8370	13332	22824	30784	38930
	Payload(bit	ts)	12000	17000	22000	27000	32000
	Huang et al ' method [15]	PSNR(dB)	36.62	33.64	31.41	29.70	28.32
Baboon QF=50	mang et at. memou [13]	increasement(bits)	16920	25288	33720	42600	51160
	December 1 at 1	PSNR(dB)	36.64	33.79	31.67	29.89	28.42
	Proposed method	increasement(bits)	15592	23840	31800	40400	49736
	Payload(bit	te)	2000	12000	22000	32000	42000
	T ayload(bi	DENID(JD)	50.28	20.62	24.07	32000	42000
D I D D	Huang et al.' method [15]	PSINK(db)	30.28	39.62	54.27	51.01	28.85
Baboon QF=70	5	increasement(bits)	2984	17720	35664	54248	69744
	Proposed method	PSNR(dB)	50.53	39.73	34.37	31.14	28.87
	Troposed method	increasement(bits)	2744	16704	33344	51312	68912
	Pavload(bit	ts)	22000	32000	42000	52000	62000
		PSNR(dB)	40.02	37.22	35.18	33 56	32.24
Baboon OE-00	Huang et al.' method [15]	increasement(bits)	37696	53864	70112	85760	00004
Babboli Qr=90		DENID(ID)	37090	27.27	25.20	22.700	22.20
	Proposed method	PSNR(dB)	40.08	37.37	35.38	33.76	32.29
	1	increasement(bits)	35400	51512	67160	82344	99360
	Payload(bit	ts)	2000	4000	6000	8000	10000
	Human et al ' mathed [15]	PSNR(dB)	45.06	39.28	36.81	35.05	33.67
Airplane QF=30	Huang <i>et al.</i> method [15]	increasement(bits)	2360	5576	8568	11640	14248
· · · · · · · · · · · · · · · · · · ·		PSNR(dB)	45 01	41 10	38 30	36.13	34 32
	Proposed method	increasement(bits)	2102	4176	6944	0712	13032
Devlee d(hite)			2192	4170	10000	12000	14000
	Payload(bit	ts)	6000	8000	10000	12000	14000
	Huang et al' method [15]	PSNR(dB)	41.63	39.60	38.01	36.56	35.36
Airplane QF=50	fitting et al. method [15]	increasement(bits)	8088	11216	14096	17256	20400
		PSNR(dB)	43.12	40.86	38.91	37.23	35.69
	Proposed method	increasement(bits)	6880	9576	12432	16080	19456
	Pavload(bit	ts)	2000	6000	10000	14000	18000
	1 uyloud(bi	DENID(JD)	52.24	46.80	42.74	20.02	27.51
Alasha OF 70	Huang et al.' method [15]	FSINK(UB)	33.24	40.89	42.74	10028	37.31
Airpiane QF=/0		increasement(bits)	2096	/584	13456	19928	20/30
	Proposed method	PSNR(dB)	53.75	47.93	44.04	40.63	37.84
	roposed method	increasement(bits)	2072	6904	12568	18992	25992
	Payload(bit	ts)	12000	17000	22000	27000	32000
	· · ·	PSNR(dB)	50.31	47.78	45.21	42.76	40.81
Airplane QF=90	Huang et al. method [15]	increasement(hits)	16208	22872	31896	41448	49856
		PSNP(dR)	51.01	48 27	45 47	43.00	40.96
	Proposed method	FSINK(UB)	14400	40.27	43.47	43.00	40.90
	-	increasement(bits)	14408	22168	30232	39920	483/6
	ts)	5000	6000	7000	8000	9000	
	Huang et al ' method [15]	PSNR(dB)	39.16	37.81	36.68	35.77	34.92
Peppers QF=30	Huang <i>et al.</i> method [15]	increasement(bits)	6472	8096	9696	11192	12624
	.	PSNR(dB)	40.30	38.98	37.79	36.60	35.51
	Proposed method	increasement(hitc)	5488	7000	8440	9992	12184
	David a state of	te)	5400 6000	8000	10000	12000	14000
Peppers QF=50	Payload(bi		42.00	41.04	20.21	12000	26.20
	Huang et al.' method [15]	PSNR(dB)	43.08	41.04	39.21	37.68	30.30
	[15]	increasement(bits)	8408	11192	14232	17528	20448
	Deemonard worth of	PSNR(dB)	43.73	41.75	40.02	38.33	36.68
	proposed method	increasement(bits)	6992	9920	12920	16392	19816
Peppers QF=70	Pavload/bit	ts)	4000	8000	12000	16000	20000
	i ayiodu(bh	PSNP(dR)	49.00	45 53	42.84	40.73	38 17
	Huang et al.' method [15]		47.07	11666	17055	40.73	20220
		increasement(bits)	6040	11656	1/056	23048	29320
	Proposed method	PSNR(dB)	49.71	46.01	43.55	41.26	38.74
	rioposea memou	increasement(bits)	4824	9736	15400	21760	28160
	Payload(bit	ts)	2000	12000	22000	32000	42000
Peppers QF=90		PSNR(dB)	57.81	48.19	44.29	41.59	39.28
	Huang et al.' method [15]	increasement(hite)	2720	17576	33120	50128	67536
		DCND(JD)	57 16	18 20	14 40	41.67	30 22
	Proposed method	I SINK(UD)	37.40	+0.30	++.40	40004	37.33
		increasement(bits)	2088	10544	32224	48904	80500

B. Comparison with Huang et al.'s scheme

As we can see from the process of Huang *et al.*'s scheme, the operation is done in units of 8×8 sized DCT block. Therefore, we combine the multi-objective optimization with Huang *et al.*'s method on the basis of taking the set of 8×8 sized DCT blocks as cover in our proposed scheme.

In this part, the comparison with Huang et al.'s scheme is shown as Fig. 8. All the results are gained by the average values of 96 images. And the x-axis represents the payload, the y-axis represents the Peak Signal to Noise Ratio (PSNR) and the file size expansion respectively in the left and the right column. The PSNR can reflect the visual quality of the stego cover, the higher it represents the smaller the image distortion caused in the embedding process. In addition, the file size expansion expresses the increas of the file size after embedding data, which is expected very small. And the proposed scheme is named Huang et al.-P in the experimental results. We can obverse that the results of our proposed scheme is higher than results of Huang et al.'s scheme in the left graph and the results of our proposed scheme is lower than results of Huang et al.'s scheme in the right and in the left, the higher line means the good image quality of the stego image and in the right, the lower line indicates the small file size expansion. So, it is obvious that the proposed scheme does better than the scheme of Huang et al. both in the image quality and file size expansion.

What's more, the improvement of our proposed multiobjective optimization is getting smaller as the QF of JPEG images increases. The closer result shows that the advantage of the multi-objective optimization is weakening in the low compression image. It is because that the bigger QF means the redundant space of the image is more and.

Furthermore, the specific values of the four test images with four different QFs are shown in Table III. In the case of each QF for each image, the first line is the embedding capacity, the second and third lines are respectively the PSNR and increased file size of the stego cover generated by Huang et al.'s method, and the fourth and fifth lines are the PSNR and file size expansion of our generated stego cover.

C. Comparison with Hou et al.'s scheme

It can be seen from the analysis in section II that the cover of Hou *et al.*'s scheme is 8×8 sized blocks which are different from original 8×8 sized DCT blocks. The cover is a set of blocks that choose values in some frequencies from the original blocks and set values in the other frequencies as 0. The multi-objective optimization is performed combined with the Hou *et al.*'s scheme in this experiment to show the improvement of the proposed scheme in Fig. 9.

The meanings of x-axis and y-axis are the same as the description in section IV-B. And the result of our experiment is marker as Hou *et al.*-P in this experiment. What's more, not only the image quality gained by our scheme is higher than that of Hou *et al.*, which is obvious in the left graph in Fig. 9 that the red line is higher than the blue one as the payload increases, but also the file size expansion of our method is lower than the expansion of Hou *et al.*, expressed as the red

line lower than the blue line in the right graph in Fig. 9. In addition, the specific values of the four test images compared with the result of Hou et al.'s method are shown in Table IV. And the meaning of each line in the table is almost the same as that in Table III, expect that the second and third lines under each QF for each image are respectively the PSNR and increased file size of the cover generated by Hou et al.'s method.

V. CONCLUSION

A novel RDH scheme in JPEG images is proposed in this paper which applies multi-objective optimization. Most stateof-the-art RDH schemes in JPEG images only consider the image quality and ignore the file size expansion in designing methods. However, the file size is an important aspect for JPEG images, so multi-objective optimization is used in our proposed scheme to take consideration about the two objectives: the image quality and the file size expansion. The strategy of multi-objective optimization is carried based on other schemes, it selects the optimized combination of signals according to different division of cover in different schemes and then the additional data is embedded into the selected signals. The signal of this paper is sized 8×8 DCT coefficients, and it can also be other sizes. Higher image quality and lower file size expansion under a given payload constraint can be achieved by using the multi-objective optimization strategy to choose the combination of signals for embedding. Experimental results show that the proposed method can yield better performance than some state-of-the-art methods [15] and [19]. What's more, the cover can be any format data of the JPEG image, such as the coding domain, in the future, we will make improvement on the coding domain combined the multi-objective optimization.

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Fig. 9. Average PSNR and the file size expansion under different payloads between the proposed method and Hou et al.'s [19] method.

TABLE IV

COMPARISON OF PSNR AND INCREASED FILE SIZE IN TEST IMAGES WITH DIFFERENT QFS AND DIFFERENT PAYLOADS BETWEEN THE PROPOSED METHOD AND HOU *et al.*'S METHOD.

	Payload(b	vits)	2000	4000	6000	8000	10000
	How et al ' method [10]	PSNR(dB)	44.78	40.76	38.29	36.14	34.35
Lena QF=30	Hou et al. method [19]	increasement(bits)	2848	5200	7992	11184	14016
	Proposed method	PSNR(dB)	45.94	42.14	39.09	36.68	34.50
	r toposed method	increasement(bits)	2352	4064	6776	10008	13808
	Payload(b	oits)	6000	8000	10000	12000	14000
	Hou et al.' method [19]	PSNR(dB)	42.83	40.97	39.14	37.53	35.97
Lena QF=50	[->]	increasement(bits)	8072	10976	14096	17520	20368
	Proposed method	PSNR(dB)	43.64	41.55	39.57	37.90	36.00
	Produce d/h	increasement(bits)	7328	10072	13064	16152	20480
	Payload(b	DENID(JD)	4000	45 5 4	12000	20.05	20000
Lana OE-70	Hou et al.' method [19]	PSINK(dB)	49.85	45.54	42.09	39.93 22160	37.28
Lena Qr=/0		PSNR(dB)	50.47	11280	10708	40.33	37 39
	Proposed method	increasement(bits)	/968	10/16	16384	22448	30288
	Pavload(h	its)	17000	22000	27000	32000	37000
	Tuyloud(E	PSNR(dB)	47.92	45 95	44 13	42.36	40.61
Lena OF=90	Hou et al.' method [19]	increasement(bits)	23520	31432	39960	48816	57000
	~	PSNR(dB)	48.25	46.29	44.33	42.54	40.69
	Proposed method	increasement(bits)	22536	30248	38784	47552	56912
	Payload(b	oits)	7000	12000	17000	22000	27000
		PSNR(dB)	37.13	33.47	30.96	28.96	27.28
Baboon QF=30	Hou et al. method [19]	increasement(bits)	9616	16536	24144	31432	39336
	Proposed method	PSNR(dB)	37.66	33.95	31.30	29.26	27.39
	r toposed method	increasement(bits)	8864	15368	22664	29744	38496
	Payload(b	its)	12000	17000	22000	27000	32000
	Hou et al.' method [19]	PSNR(dB)	36.90	33.95	31.76	29.91	28.50
Baboon QF=50	filou es ass meanou [19]	increasement(bits)	16712	24544	32488	42368	50256
	Proposed method	PSNR(dB)	37.25	34.24	31.97	30.08	28.60
		increasement(bits)	15512	23320	31904	40704	49088
	Payload(b	otts)	2000	12000	22000	32000	42000
Daharan OE 70	Hou et al.' method [19]	PSNR(dB)	50.77	39.85	34.46	52400	28.86
Baboon QF=70		DEND(dD)	2830	1/640	33290	21 20	28 02
	Proposed method	increasement(bits)	2624	16728	34.74	50840	28.92
	Pavload(h	ite)	2024	32000	42000	52000	62000
	Tayload(b	PSNR(dB)	40.03	37.26	35 19	33.60	32.25
Baboon OF=90	Hou et al.' method [19]	increasement(bits)	37264	54192	69808	85336	100168
Babboli QI =90		PSNR(dB)	40.28	37.52	35.48	33.81	32.29
	Proposed method	increasement(bits)	36184	51688	67392	82864	99552
	Payload(b	oits)	2000	4000	6000	8000	10000
	How at all mathed [10]	PSNR(dB)	45.30	40.59	37.81	35.67	33.88
Airplane QF=30	Hou et al. method [19]	increasement(bits)	2232	5128	7904	11168	14168
	Proposed method	PSNR(dB)	45.95	41.53	38.61	36.27	34.37
	Toposed method	increasement(bits)	1952	4344	6744	9832	13208
	Payload(b	oits)	6000	8000	10000	12000	14000
	Hou et al.' method [19]	PSNR(dB)	42.74	40.50	38.37	36.89	35.37
Airplane QF=50		increasement(bits)	7744	10448	14048	16896	20536
	Proposed method	PSNR(dB)	43.41	41.08	39.09	37.33	35.74
		increasement(bits)	6864	9752	12760	16040	19360
	Payload(b	IIS)	2000	47.91	10000	14000	18000
Aimlana OE-70	Hou et al.' method [19]	PSINK(dB)	2028	47.81	45.80	20008	26496
Anpiane Qr=70		DSND(dB)	2920 54.48	18 23	13370	20008	20490
	Proposed method	increasement(bits)	2520	7072	12544	18960	25744
	Pavload(h	its)	12000	17000	22000	27000	32000
		PSNR(dB)	50.84	47.98	45.32	42.79	40.83
Airplane OF=90	Hou et al.' method [19]	increasement(bits)	15400	22872	31816	41040	49048
1 5	D	PSNR(dB)	51.15	48.45	45.52	43.13	40.94
	Proposed method	increasement(bits)	14888	22080	30800	39688	49368
Payload(oits)	5000	6000	7000	8000	9000
	Hou et al ' method [19]	PSNR(dB)	39.68	38.45	37.29	36.25	35.22
Peppers QF=30	Hou et al. method [19]	increasement(bits)	6192	7528	9648	10824	12768
	Proposed method	PSNR(dB)	40.57	39.22	37.90	36.73	35.54
	rioposed method	increasement(bits)	5480	6768	8544	10440	12128
Peppers QF=50	Payload(b	oits)	6000	8000	10000	12000	14000
	Hou et al.' method [19]	PSNR(dB)	43.34	41.48	39.83	38.19	36.45
		increasement(bits)	8304	10840	13888	17072	20672
	Proposed method	PSNR(dB)	44.04	42.12	40.25	38.52	36.74
	- 	increasement(bits)	7264	9664	12968	16328	19928
Peppers QF=70	Payload(b	DEND(JD)	4000	8000	12000	16000	20000
	Hou et al.' method [19]	PSNR(dB)	49.89	40.00	45.40	41.10	38.56
		PSNP(AP)	50.60	11344	13 75	22344 41.40	20944
	Proposed method	increasement(hite)	4488	40.02 9856	15712	21856	28280
	Pavload(h	sits)	2000	12000	22000	32000	42000
	i ayiodd(U	PSNR(dB)	59.02	48.82	44.54	41 64	39.18
Peppers QF=90	Hou et al.' method [19]	increasement(bits)	2248	16920	32256	50320	68488
	_	PSNR(dB)	59.52	49.21	44.83	41.83	39.35
	Proposed method	increasement(bits)	2672	15752	31320	48520	66528

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