

# OFDM RoFSO Links with Relays Over Turbulence Channels and Nonzero Boresight Pointing Errors

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**Abstract**—In the last few years, the radio on free space optics (RoFSO) technology that involves effective wireless transmissions of multiple radio frequency (RF) signals via free space optical (FSO) links, has drawn great research and commercial interest. However, its deployment suffers from atmospheric turbulence and pointing errors effects that strongly degrade the performance of such optical wireless links. In order to combat these impairments, in this work, we investigate the performance of various realistic RoFSO scenarios that may employ orthogonal frequency-division multiplexing (OFDM) scheme with Quadrature Amplitude Modulation (QAM) format and Decode and Forward (DF) relay node(s) over weak to strong turbulence channels emulated through the very accurate recently launched Malaga or  $M$ -distribution model along with the presence of various nonzero boresight pointing errors effects with different jitters for the elevation and the horizontal displacement modeled through the suitable Beckmann distribution. Under these conditions we extract closed-form mathematical expressions for the crucial performance metrics of the Outage Probability (OP) and the Average Bit Error Rate (ABER) of the examined RoFSO implementations with DF relays. Proper numerical results that are validated through the corresponding simulations are provided and demonstrate the accuracy of our extracted expressions along with the usefulness of serial DF relay-assisted multi-hop configurations as an effective method to broaden the coverage of the optical wireless links.

**Index Terms**—Radio on Free space Optical (RoFSO) technology; Malaga-distribution; Decode and Forward (DF) relays; Nonzero boresight pointing errors; Orthogonal Frequency Division Multiplexing (OFDM); Quadrature Amplitude Modulation (QAM).

## I. INTRODUCTION

### A. RoF and RoFSO Techniques

Owing to the increasing demand for transferring higher data rates at a higher security level, the transmission of RF signals through optical wavelengths has attained a lot of commercial and research interest recently. In this respect, both radio over fiber (RoF) and RoFSO technologies provide the means to accommodate these growing requirements.

Transmission of RF signals by means of optical fiber links, has been utilized for many years as a cost-effective

and high-capacity solution to facilitate the wireless access [1]. Since its first demonstration for cordless or mobile telephone service in 1990, [2], the RoF technology has been developed to provide high transmission capacity, significant mobility and flexibility, as well as economic advantage due to its broad bandwidth and low attenuation characteristics. In addition, RoF systems allow multi-operator multi-service operation, and dynamic resource allocation. These potentials have made it suitable for wide range of applications including last mile solutions, extension of existing radio coverage and capacity, and backhaul. In RoF implementation, to distribute the RF signals from central station to remote stations, RF signals are placed on optical carriers and transmitted over high capacity optical fiber cables [3]-[6]. However, RoF implementation is dependent on availability of installed optical fiber cables [7].

Therefore, in the absence of fiber infrastructure (for example across a river, a very busy street, rail tracks or where right of way is not available or too expensive to pursue), RoFSO is an attractive data bridge in such instances, [7], [8]. Similar to RoF technique, it has been demonstrated recently that the RF signals can be transmitted by a line-of-sight (LOS) relatively short FSO link, using the so-called RoFSO scheme, [7], [9], [10]. In fact, by modulating RF signals on optical carriers for transmission over the free space, RoFSO systems have the same advantages and drawbacks with FSO links. More specifically, by increasing the carrier frequency from RF to that of optical waves through RoFSO technique, it is feasible to increase the information capacity by many orders of magnitude and even at a higher security level due to the fact that the information data is transmitted through a very narrow optical beam, which is very difficult to detect and interfere, [8], [11]-[17].

Other benefits of FSO propagation that also harvest RoFSO transmissions include the immunity to multipath dispersion and electromagnetic interference, the operation with lower power consumption in the unlicensed optical spectrum, the flexibility for deployment and redeployment and lower overall installation and operational costs compared to conventional radio links and fiber optics, [8], [14], [16], [18]-[22]. In view of these nice characteristics features mentioned above, RoFSO can be used either as an effective alternative or

complementary to the optical fiber network as a high capacity wireless backhaul technology for cellular networks, [1], [9], [23]-[25]. Moreover, new generation of FSO systems utilize seamless connection of free-space beam to optical fiber and therefore eliminating the necessity of converting the transmitted signal from optical-to-electrical or vice versa, [26].

This kind of FSO system realizes a bandwidth and protocol transparent system, which can be easily adapted for the transmission of RF signals through RoFSO communication, [27]. RoFSO technology has also been suggested to provide inexpensive, secure, short-range wireless transport for WiMAX (Worldwide Interoperability for Microwave Access) as reported in [28]-[32]. Additionally, another point in favor of RoFSO is that while the data rate over fiber is limited by its dispersion characteristics [33], [34] the dispersion due to atmosphere is shown to be much weaker or even negligible for short propagation distances [16], [35]-[37]. Finally, via RoFSO technology it is possible to simultaneously transmit multiple RF signals comprising heterogeneous wireless services over FSO links using wavelength-division multiplexing technology, while it can be also applied as a universal platform for enabling seamless convergence of fiber and free-space optical communication networks, thus extending broadband connectivity to underserved areas [7].

### B. Challenges of RoFSO Technology Development

However, the widespread deployment of RoFSO is hampered by several performance-degrading factors that mainly arise from the variable characteristics of the atmospheric FSO channel. Effects of fog, rain, atmospheric gases and aerosols result in beam attenuation because of photon absorption and scattering [38], [39]. It is notable that similarly to our viewing of distant object the optical transmission is most impaired by fog i.e. more than 30dB/km, because the fog aerosols have a comparable size as the used optical wavelengths, causing much scattering of the laser energy as the fog gets thicker [40]-[42]. Nevertheless, both absorption and scattering are deterministic effects that are extensively studied, especially under fog conditions [17], [43] and thus they are not treated in this paper.

Even in clear weather conditions a major impairment over FSO and RoFSO propagation is the very complex and random atmospheric turbulence effect which takes place because of the inhomogeneities of both temperature and pressure in the atmospheric channel and causes the so-called scintillation effect that results in rapid fluctuations of the irradiance of the optical signal at the receiver's side, degrading strongly the communication system's performance, [23], [36], [39], [44]-[46]. Thus, in order to emulate these turbulence-induced irradiance scintillations, accurate turbulence distribution models are required according to turbulence strength. In early works on optical wireless communications the lognormal model has been widely used [45], [47]-[52]. However, this

model has been proved to be valid only for weak turbulence conditions. Alternatively, the I-K distribution model [36], [53]-[55] and the Gamma model [16], [56]-[58] can be also used in the weak turbulence regime. Under strong turbulence conditions it has been shown that K distribution is in a good agreement with experimental results [59]-[62], while for saturated turbulence conditions the negative exponential distribution has been proved to be suitable [23], [50], [63]-[68].

A very accurate turbulence-induced fading channel model for FSO systems is the Gamma-Gamma distribution proposed by Al-Habash *et al.* in [69] and has a very good agreement with measurement data for a wide range of weak to strong turbulence conditions. This tractable mathematical model for atmospheric turbulence is based on the modified Rytov theory that was introduced by the same authors in [70], while it is notable that includes both the negative exponential and K distribution models as its marginal cases. Representative examples of the wide use of Gamma-Gamma model in optical wireless communications can be found in [9], [16], [23], [36], [71]-[78]. Nevertheless, the distribution model that leads to closed-form and mathematically tractable expressions under all turbulence regimes, unifying most of the well-known proposed statistical models for turbulence-induced irradiance fluctuations is the recently-launched *M-alaga* distribution model that was first suggested by Navas *et al.* in [79]. Indeed, lognormal, negative exponential, gamma, K and even gamma-gamma model are proved to be special cases of *M-alaga* distribution, [79].

In this context, *M-(alaga)* distribution is gaining popularity in scientific bibliography recently, as it can be realized in [24], [80]-[84] and it will be also used to model the irradiance scintillations in the current work. Additionally, Ansari *et al.* derived in [81] very useful unified formulas and asymptotic expressions for the most important performance metrics of an FSO link operating over *M-alaga* turbulence, such as the outage probability, the error rate of a variety of modulation schemes and the ergodic capacity. Furthermore, Sandalidis *et al.* in [85] proposed the mixture Gamma distribution model as an accurate approximation of the turbulence effect, mainly in an attempt to simplify the expressions of Gamma-Gamma and *M-(alaga)* functions, [85], [86].

Another significant concern of FSO and RoFSO development is the unavoidable presence of pointing errors due to building sway, namely misalignments between the transmit and receive terminals that diminish the line of sight between them. More precisely, thermal expansion, strong wind and weak earthquakes result in the sway of the high-rise buildings where the optical wireless terminals are usually located, and thus, optical beam vibrations are occurred which result, in turn, in significant misalignment-induced irradiance fluctuations at the receiver's side [12], [87]-[89]. The pointing errors create a random effect, and thus, in order to emulate its

consequences, i.e., the misalignment-induced fading, we need an accurate distribution model. One such, widely utilized distribution model was first proposed by Farid *et al.* in [12], considering detector aperture size, beam width and jitter variance through Rayleigh distribution. Typical examples in which this pointing error model is involved to derive the joint turbulence-induced and misalignment-induced fading could be found in [12], [16], [82], [88], [89]. Nonetheless, according to this model, the boresight component of pointing is assumed to be zero and both horizontal and elevation displacement are assumed to follow an independent, identically distributed zero-mean Gaussian distribution.

Although typical terrestrial FSO systems are initially installed with near zero boresight error, the boresight is still considerable due to the thermal expansion of the buildings [90]. Thus, in practical point of view pointing errors consist of both, nonzero boresight and jitter components. It should be mentioned here that the boresight is the fixed displacement between beam center and detector's center, while the jitter is the random offset of the beam center at detector plane, which is mainly caused by building sway and building vibration. In view of the above, Gappmair *et al.* in [91] extended the analysis carried out in [12] in order to assume different jitters for the elevation and the horizontal displacement, considering that the radial displacement at the receiver follows a Hoyt distribution. In [90], Yang *et al.* based once again on [12], derived a more generalized statistical model to describe the pointing error effects with non-zero boresight displacement, considering that the radial displacement at the receiver follows a lognormal-Rician distribution this time.

Recently, Ansari *et al.* extracted in [92] unified expression for the moments of the average SNR of a FSO link operating over lognormal, Rician-lognormal and  $M$ - (alaga) turbulent channels along with nonzero and zero boresight pointing errors. Based on these expressions they also presented in [92] unified asymptotic formulas applicable in a wide SNR range for the ergodic capacity in terms of simple elementary functions for the respective turbulence models. Then, AlQuwaiee *et al.* presented in [93] a more generalized pointing error approach through the versatile statistical Beckman distribution model that includes many distributions as special cases such as Rayleigh, Hoyt and lognormal-Rician among others. Additionally, they derived a generic expression of the asymptotic capacity of FSO systems under the joint impact of generalized pointing errors and Gamma-Gamma or lognormal modelled turbulence. More recently, Boluda-Ruiz *et al.* derived an approximate expression for the combined pdf with atmospheric turbulence and non-zero boresight pointing errors in [94] by introducing an efficient and accurate approximation of the Beckmann distribution, which is used to model generalized pointing errors with quite high precision [94].

In view of the above and considering also the growing interest that non-zero boresight pointing errors hypothesis

has raised in technical literature recently [84], [90]-[95], in this work we focus on the model proposed in [94] in order to study the impact of non-zero boresight misalignment fading on RoFSO performance, as it will be presented in more detail below.

### C. Methods for RoFSO Performance Improvements

In order to improve the performance of an FSO system impaired by the combined turbulence-induced and misalignment-induced fading, particular attention is given to the modulation format to be employed. Modulation techniques can be generally classified into two categories. The first is single-carrier modulation, in which the data are carried on a single main carrier. This is the "conventional" modulation format that has been the workhorse in optical communications for more than three decades.

Single-carrier modulation has in fact experienced rapid advancement in recent years [96]. Indeed, the most widely utilized modulation format in the commercial and research field is the On-Off Keying (OOK) with Intensity Modulation/Direct Detection (IM/DD) signaling technique, mainly due to its simplicity [91]. However, it requires an adaptive threshold to optimally perform in turbulent atmosphere [39], [45]. This drawback may be circumvented via Pulse Position Modulation (PPM) technique, although it performs a spectral efficiency much lower than that of OOK signals [46], [91]. The second category of modulation technique is multicarrier transmission, in which the data are carried through many closely spaced subcarriers, [96]. Thus, an effective alternative to both OOK and PPM schemes is the Subcarrier Intensity Modulation (SIM) technique that was first suggested in [97] for optical wireless links. In a SIM FSO system a pre-modulated, usually with a Phase Shift Keying (PSK) modulation format and properly biased RF subcarrier is used to modulate the intensity of the optical carrier [98]. Therefore, by employing any multicarrier technique, like SIM, the performance of the optical wireless transmission is enhanced due to the fact that multiple subcarriers are used to carry the information and thus increased throughput is obtained.

Additionally, in the SIM FSO concept many works have been recently presented, [68], [71], [99]-[102]. Additionally, Orthogonal Frequency Division Multiple Access (OFDM) over optical link is a special class of multicarrier (multiple-subcarrier) intensity modulation category that has only recently gained significant attention in the optical communication community [9], [24], [25], [96], [98] and will be also employed in the current work below. In basic terms, OFDM refers to data transmissions in parallel on a number of different frequencies, while the subcarrier frequencies are chosen so that the signals are mathematically orthogonal over one OFDM symbol period. In general, OFDM is one of the most popular techniques for broadband wireless communications and it is known for its increased robustness against frequency selective fading,

intersymbol and narrow-band interference, as well as for its high channel efficiency.

Consequently, it has been adopted in a wide range in the RF domain including digital audio/video broadcasting (DAB/DVB), wireless local area networks (LANs) also known as IEEE 802.11a/g or Wi-Fi, asymmetric digital subcarrier line (ADSL; ITUG.992.1), wireless metropolitan area networks (WiMAX; 802.16e) and long-term evolution (LTE)-the fourth generation mobile communications technology [9], [96]. Nevertheless, the application of OFDM to optical domain occurred surprisingly late, mainly due to the fact that its robustness against optical channel dispersion was not recognized until Dixon et al. proposed in [103] the use of OFDM to combat modal dispersion in multimode fiber (MMF) channel that resembles that of the wireless one in terms of multipath fading [96]. However, Optical OFDM (O-OFDM) apart from interference immunity due to its orthogonality property and that multiple independent bit streams are modulated onto subcarriers at different frequencies multiplexed in the RF domain with IM/DD scheme offering high capacity links, it suffers mainly from the following drawbacks.

To begin with, the baseband OFDM signal is complex and bipolar, while IM/DD requires a real and positive RF signal to drive the laser diode (LD). Therefore, we need to transform the OFDM signal to unipolar by adding for instance a DC bias to the OFDM signal (DC-OFDM; DCO-OFDM) so that the resulting signal becomes positive [104]. Note that this DC bias should be large enough to prevent clipping and distortion in the optical domain [9], [73]. The latter translates into average optical power inefficiency especially for IM/DD DC-OFDM (DCO-OFDM), while the large number of subcarriers creates unfavorable high peak-to-average power ratios (PARP) and finally distortions due to LD nonlinearities may be occurred [1], [73], [105]. Still, OFDM remains a very well-established modulation scheme for modern broadband communication systems such as OFDM-over-FSO or RoFSO as it is demonstrated both theoretically and experimentally in [9], [24], [25], [34], [73], [106]-[108]. Moreover, it should be mentioned that in order to successfully apply OFDM to FSO some additional OFDM modification techniques are proposed such as asymmetrically clipped O-OFDM (ACO-OFDM), flipped OFDM (Flip-OFDM), unipolar OFDM (U-OFDM) and instead of direct-detection O-OFDM (DDO-OFDM) the coherent O-OFDM (CO-OFDM), [96], [98], [109]-[112].

As already mentioned above, the negative consequences of atmospheric turbulence on FSO and RoFSO transmissions are getting worse as the optical signal is propagating over longer distances. Thus, especially for link ranges longer than 1km, the combined turbulence-induced and misalignment induced fading becomes a major performance and coverage area limiting factor in such wireless systems. A very promising technique to combat this distance-dependency of the combined turbulence-induced and misalignment-induced

fading is the use of relays that create intermediate shorter hops and thus they can lead to longer (total) link length and performance improvements. Relay-assisted links may employ either DF or Amplify-and-Forward (AF) relays that may be connected either serially (i.e. multi-hop transmission) or in parallel (i.e. cooperative diversity).

In serial, i.e. multi-hop, DF relaying configurations the source transmits the information signal to the nearest DF relay node, which decodes the signal after detection, modulates it and retransmits it to the next relay or the destination only if the received SNR exceeds a specific decoding threshold that provides proper and reliable operation of the communication system. This process continues until the source's data arrives at the destination node. Note that one such multi-hop DF configuration will be analyzed as part of the current work. Similarly, for multi-hop AF transmissions the same procedure applies with the sole difference that each relay does not perform any decoding on the received signal but after a multiplication with a proper energy scaling term (amplification), simply forwards it to next relay or the destination.

Additionally, in parallel relaying configurations the source transmits the same signal to all relays, which, in turn, either decode and retransmit the signal (case of DF relays) or amplify and forward it (case of AF relays) to the destination [23], [113]-[117]. Over the last years the use of relay-assisted optical wireless transmissions has been discussed in many works in the open technical literature. Their results highlight the usefulness of relay-assisted transmission as a method to effectively broaden the optical wireless coverage area or as a fading-mitigation tool, [23], [83], [106], [113]-[121].

#### D. Motivation

By focusing on the issue of OFDM-based RoFSO transmissions and by considering the above phenomena and techniques, a lot of interesting work has been recently done. In [9], Bekkali et al. examined the performance of a RoFSO QAM or PSK OFDM IM/DD link over weak to strong turbulence conditions, modeled by Gamma-Gamma distribution. By using the closed-form expressions they derived they proved that RoFSO performance is highly sensitive to the atmospheric turbulence and the received optical power, while they also demonstrated that selecting an appropriate optimal optical modulation index (OMI) it is feasible to upgrade the overall RoFSO system performance. Later, Tsonev et al., first proposed in [109] an U-OFDM scheme for FSO that provides the same benefits of ACO-OFDM modulation, as well as improved demodulation for better power efficiency in Additive White Gaussian Noise (AWGN) channel, while when compared to DCO-OFDM, the proposed scheme showed better performance results in terms of BER. Next, the analysis performed Selvi and Murugesan in [34] showed that over weak turbulence conditions 3-5dB improvement is obtained for RoFSO QAM or PSK OFDM transmission compared to RF based wireless transmission. Then, Dimitrov *et al.*, studied in

[111] the double-sided signal clipping in ACO-OFDM FSO systems due to biasing issues and physical limitations of the transmitted front-end. They showed that unlike in OFDM-based RF systems, an SNR increase is not achievable simply by increasing the average electrical and/or optical power at the transmitter since the latter leads to a larger clipping distortion, and therefore, to a larger SNR penalty. Additionally, they found that ACO-OFDM is more robust to the clipping effects than DCO-OFDM for similar modulation schemes at the expense of a 50% reduction in spectral efficiency and thus, that ACO-OFDM is more suitable for applications with lower radiated average optical power, whereas DCO-OFDM promises to deliver higher throughput. Later, Tsonev et al., presented in [110] a complete analytical framework for the analysis of memoryless nonlinear distortion in an FSO system that guarantees closed-form solutions, assuming DCO-OFDM, ACO-OFDM, U-OFDM and pulse amplitude modulated discrete multitone modulation (PAM-DMT) along with QAM and PAM modulation formats.

In this context, Nistazakis et al. investigated in [73] the influence of non-linear clipping effect along with Gamma-Gamma turbulent channel and they derived mathematical expressions for the estimation of the average SNR, average BER and the outage probability as a function of the physical parameters of the OFDM FSO link. Additionally, Nistazakis *et al.* in [23] extended the work in [9] by studying the performance of a DF multi-hop RoFSO QAM or PSK OFDM system over Gamma Gamma or negative exponential turbulent channels. They demonstrated that the use of relays increases the RFO coverage area but at the expense of increased BER values, while they extracted useful closed-form expressions for the BER estimation and the design of either single RoFSO QAM or PSK OFDM links or relayed systems, according to the specific turbulence conditions, modulation format and (each) link's individual parameters, based on the demands of OFDM RoFSO configuration. More recently, Nistazakis *et al.*, in [122] extended even more the performance studies in [9] and [24], by investigating the performance of a DF multi-hop QAM RoFSO system under the presence of Gamma-Gamma or Gamma turbulence along with pointing errors.

Nevertheless, to the best of author's knowledge, there isn't any work that investigates the combined impact of both turbulence and non-zero boresight pointing error effects of a relay-assisted OFDM-based RoFSO system in the open literature so far. Thus, the performance of typical multi-hop DF relay-assisted QAM-OFDM RoFSO systems under the combined impact of a wide range of  $M$ -alaga turbulent conditions along with weak to strong non-zero boresight pointing errors is addressed in the current work. More specifically, we initially derive novel closed-form expressions for the average BER (ABER) and the outage probability (OP) of each intermediate RoFSO hop and by using them we next derive novel closed-form expressions for ABER and the OP of the total multi-hop system. In this context, we aim to reveal

that the use of DF relays can significantly broaden the RoFSO coverage area but at the expense of increased ABER and OP values compared to the initial shorter link.

Moreover we intend to demonstrate the impact of average CNDR, the number of relays and the value of the modulation order  $L$  of the employed  $L$ -QAM format on the RoFSO performance. Additionally, we aim to prove that for specific link's characteristics the use of DF relays can be considered as a fading-mitigation tool that improves the RoFSO performance for the same total link length. Proper numerical results are provided, validated by simulations that demonstrate the accuracy of our derived expressions. Note that in order to further verify our suggestions, apart from the numerical and simulation results obtained for the RoFSO link we have assumed, we also obtained further numerical and simulation results for a practical link, by using some experimental measurements performed in University of Waseda, Japan, on the 15th October, 2009, as it was presented in [82].

## II. SYSTEM MODEL

### A. Basic Principles of the Examined RoFSO System

The total RoFSO system under consideration consists of the initial transmitter, the final receiver and between them ( $H-1$ ) serially connected DF relay nodes, which create  $H$  individual intermediate optical links. Note that in order to optimize the performance of the system the DF relay nodes are placed equidistant along the direct line from source to the destination, as it was shown in [114]. The laser diode (LD) at the initial transmitter's side emits an optical OFDM signal, modulated with  $L$ -QAM modulation scheme, towards the receiver of the nearest relay node where it may be decoded and retransmitted to the next DF relay. In fact, OFDM is an effective way of multicarrier transmission where the data is transmitted in parallel and thus simultaneously, by splitting into multiple narrow band subcarriers. Thus, each RF subcarrier (our case of RoFSO) is modulated with a  $L$ -QAM format and then carried on a high frequency optical carrier emitted by LD. Recall that the subcarriers of the OFDM are orthogonal to each other since their set is realized by using the inverse fast Fourier transform (IFFT) at the transmitter and the fast Fourier transform (FFT) at the receiver, and hence the inter-symbol interference (ISI) between them is minimal allowing easier signal detection at the receiver using standard correlation techniques [9], [23]. In order to study the total system's performance, we first focus on its first intermediate link. The information signal is loaded in the  $N$  RF subcarriers and thus, the OFDM signal,  $s_{OFDM}(t)$ , after the up-conversion to the carrier frequency,  $f_c$ , just before the LD transmitter, is given as [9], [25]:

$$s_{OFDM}(t) = \sum_{n=0}^{N-1} s_n(t) \quad , \quad 0 \leq t < T_s \quad (1)$$

$$= \sum_{n=0}^{N-1} X_n \exp[i(\omega_n + 2\pi f_c)t]$$

where  $\omega_n = 2\pi/T_s$ ,  $n=0,..N-1$ , represents the angular frequency of each of the  $N$  orthogonal subcarriers,  $T_s$  is the duration of the OFDM symbols, while  $X_n$  stands for the complex data symbol of the  $n_{th}$  subcarrier, which is mapped according to selected modulation format, which here, is the  $L$ -QAM scheme with  $L$  being 4, 16 or 64, [9].

The above OFDM signal modulates the optical intensity of the LD at the transmitter's side and owing to the non-linearity of the latter device its emitted optical power,  $P(t)$ , is given as [1], [9], [23]:

$$P(t) = P_t \left[ 1 + \sum_{n=0}^{N-1} m_n s_n(t) + a_3 \left( \sum_{n=0}^{N-1} m_n s_n(t) \right)^3 \right], \quad (2)$$

where  $P_t$  represents the average transmitted optical power,  $a_3$  stands for the third order non-linearity coefficient of the LD and  $m_n$  is the optical modulation index (OMI) of the  $n_{th}$  subcarrier, [9]. Additionally, the optical power that arrives at the receiver of the nearest to the initial transmitter DF relay node, should be equal to [9], [23]:

$$P_r(t) = P(t) L_{tot} I + n(t), \quad (3)$$

where  $L_{tot}$  represents the overall attenuation losses caused by atmosphere,  $I$  stands for the instantaneous normalized received irradiance that arrives at the receiver of the DF relay node and  $n(t)$  is the AWGN of the channel, [24]. Here, it should be mentioned that the instantaneous normalized received irradiance  $I$  is fluctuated randomly at the receiver's side due to both turbulence-induced and misalignment-induced fading. Thus it holds that  $I = I_t I_p$ , where  $I_t$  stands for the instantaneous normalized received irradiance due to atmospheric turbulence-induced fading and  $I_p$  represents the instantaneous normalized received irradiance due to misalignment-induced fading, respectively, [12], [16], [81]. Moreover, from Eqs (2) and (3), the output current at the receiver's photo-diode (DP) of the examined DF relay is expressed as [9], [23]:

$$i(t, I) = I_0 \left[ 1 + \sum_{n=0}^{N-1} m_n s_n(t) + a_3 \left( \sum_{n=0}^{N-1} m_n s_n(t) \right)^3 \right] + n_{opt}(t), \quad (4)$$

where  $I_0 = \eta L_{tot} P_t I$  is the direct current (DC) component of the received photo-current  $i(t, I)$ ,  $\eta$  stands for the PD responsivity and  $n_{opt}(t)$  represents the AWGN with zero mean and variance equal to the half of the noise power, i.e.,  $N_0/2$ , obtained as  $N_0 = 4K_B T F / R_L + 2qI_0 + I_0^2 (RIN)$ , where  $K_B$ ,  $T$ ,  $F$ ,  $R_L$ ,  $q$  and  $RIN$  represent the Boltzmann's constant, the temperature, the noise figure of the receiver, the electron charge and the relative intensity noise (RIN) process, respectively, [9], [24]. Furthermore, another performance mitigation factor that cannot be neglected is the effect of inter-modulation distortion (IMD) due to the finite linear operating range of the LD transmitter. This IMD noise for the  $N$  subcarriers is expressed as [9], [23]:

$$\sigma_{IMD,n}^2 = \frac{9a_3^2 m_n^6 I_0^2}{128} \times \left( 2n(N-n+1) + N(N-5) + 2 - \frac{(-1)^n - (-1)^{2N+n}}{2} \right)^2. \quad (5)$$

Consequently, from (4) and considering also the presence of IMD noise in (5) and that the total noise (IMD and optical noise) are Gaussian distributed we obtain that the instantaneous carrier to noise plus distortion which is arriving at the receiver of the examined DF relay node, for each of the  $N$  subcarriers,  $n$ , is given by the following approximation [9], [10], [23], [106]:

$$CNDR_n(I) \approx \frac{m_n^2 \eta^2 L_{tot}^2 P_t^2 I^2}{2(N_0/T_s + \sigma_{IMD,n}^2)}, \quad (6)$$

Similarly, the expected value of the  $CNDR_n$ , i.e.,  $CNDR_{n,EX}$ , can be obtained from (6) as follows:

$$CNDR_{n,EX} \approx \frac{(m_n \eta L_{tot} P_t E[I])^2}{2([N_0/T_s]_{AV} + [\sigma_{IMD,n}^2]_{AV})}. \quad (7)$$

where the symbol  $[.]_{AV}$  stands for the average value.

We ought to declare here that considering the presence of (non-zero boresight) pointing error effects we cannot set  $E[II]=1$  in (7) as is the case of [23, Eq. (10)] where negligible pointing error effects are considered.

### B. Atmospheric Turbulence Over the RoFSO Channel

In order to accurately emulate the atmospheric turbulence-induced fading, i.e., the random and rapid scintillations of the received irradiance that significantly mitigate both the RoFSO performance and coverage area, as explained above, we are using the recently-launched and unifying  $M$ -alaga-distribution model which is very accurate for weak to strong turbulence conditions. According to this versatile model, the turbulence-induced fading  $I_t$  (i.e., the normalized irradiance at the receiver of the DF relay due to turbulence conditions prevailing along the individual hop) is considered as a random variable with the following PDF, [79], [82]:

$$f_{I_t}(I_t) = A_{(\aleph \text{ or } \Re)} \sum_{(\aleph \text{ or } \Re)} a_{k(\aleph \text{ or } \Re)} I_t^{\frac{a+k-2}{2}} K_{a-k} \left( 2\sqrt{B_{(\aleph \text{ or } \Re)}} I_t \right), \quad (8)$$

where the subscripts  $\aleph$  or  $\Re$  correspond to the type of the parameter  $b$  i.e. being a natural or a real number, [24]. Thus, for  $b \in \aleph$ , the summation of the above PDF

expression, Eq. (3), corresponds to  $\sum_{(\aleph)} [\cdot] = \sum_{k=1}^b [\cdot]$  while,

$$A_{(\aleph)} = 2a^2 (bc)^{b+\frac{a}{2}} / \left[ c^{\frac{a+2}{2}} \Gamma(a)(bc+\Omega)^{b+\frac{a}{2}} \right], \quad B_{(\aleph)} = ab/(bc+\Omega)$$

$$a_{k(\aleph)} = \binom{b-1}{k-1} \left( \frac{(bc+\Omega)^{\frac{k}{2}}}{(k-1)!} \right) \left( \frac{\Omega}{c} \right)^{k-1} \left( \frac{a}{b} \right)^{\frac{k}{2}}. \text{ On the other hand,}$$

$$\text{for } b \in \Re, \quad A_{(\Re)} = [2a^{a/2} (bc)^b] / [c^{a+b/2} \Gamma(a)(bc+\Omega)^b],$$

$a_{k(\text{sr})} = (b)_{k-1} (ac)^{k/2} c^{1-k} (\Omega + cb)^{1-k} ((k-1)!)^{-2}$  and  $B_{(\text{sr})} = a/c$ , where  $(b)_k$  denotes the Pochhammer symbol, [79]. Moreover,  $K_\nu(\cdot)$  is the  $\nu$ th order modified Bessel function of second kind,  $\Gamma(\cdot)$  is the Gamma function,  $a$  is a positive parameter related to the effective number of large scale cells of the scattering and  $c = 2b_0(1-\rho)$ , [24]. The values of  $b_0$  and  $\rho$  depend on the total scatter components and terms, while  $\Omega$  is the average optical power of the coherent contributions which consists on the LOS and the coupled to the LOS scattering term, [24], [79], [82]. The parameter  $\rho$  indicates the relationship between the two scattering components of the *M-alaga* model mentioned above and represents the amount of scattering power coupled to the LOS component, while it ranges from zero to one, i.e.,  $0 \leq \rho \leq 1$ , [79], [82].

C. Nonzero Boresight Pointing Errors

The pointing errors effect consists of two components: the boresight and the jitter. The boresight is the fixed displacement between the beam center and the detector's center, while the jitter is the random offset of the beam center at the detector plane, [90], [95]. A general and realistic statistical distribution model which describes accurately the pointing errors effect taking into account the effect of beam width, the detector's size, the different jitters for the elevation, the horizontal displacement and the effect of non-zero boresight error is the Beckmann model which has the following PDF, [90], [94]:

$$f_R(R) = \frac{R}{2\pi\sigma_x\sigma_y} \times \int_0^{2\pi} \exp\left(-\frac{(R\cos\theta - \mu_x)^2}{2\sigma_x^2} - \frac{(R\sin\theta - \mu_y)^2}{2\sigma_y^2}\right) d\theta, \quad (9)$$

where  $\theta$  is the transmit divergence angle describing the increase in beam radius with distance  $z$  from the transmitter. Note that the beam width can be approximated as  $w_z \approx \theta z$  for relatively long distances. Additionally,  $R$  is the radial displacement that is expressed as  $R = |\vec{R}| = \sqrt{R_x^2 + R_y^2}$  where  $\vec{R} = [R_x, R_y]^T$  is the radial displacement vector with  $R_x$  and  $R_y$  representing the displacements located along the horizontal and elevation axes at the detector plane, respectively. These random variables are considered as nonzero mean Gaussian distributed random variables, i.e.,  $R_x \sim N(\mu_x, \sigma_x^2)$ ,  $R_y \sim N(\mu_y, \sigma_y^2)$  where the parameters  $\mu_x, \mu_y$  denote their mean values and  $\sigma_x, \sigma_y$ , the jitters for horizontal and elevation displacements respectively, [94]. The expression of Eq. (9) can be simplified, through the analysis performed in Ref. [94], and the Beckmann's distribution can accurately be approximated through the modified Rayleigh distribution, as follows, [94]:

$$f_R(R) = \frac{R}{\sigma_{\text{mod}}^2} \exp\left(-\frac{R^2}{2\sigma_{\text{mod}}^2}\right), \quad R \geq 0 \quad (10)$$

where  $\sigma_{\text{mod}}^2 = \left(\frac{3\mu_x^2\sigma_x^4 + 3\mu_y^2\sigma_y^4 + \sigma_x^6 + \sigma_y^6}{2}\right)^{1/3}$ .

The PDF for the irradiance depending on the pointing errors effect,  $I_p$ , is approximated as, [94]:

$$f_{I_p}(I_p) = \frac{\psi^2}{(A_0 g)^{\psi^2}} I_p^{\psi^2-1}, \quad \text{for } 0 \leq I_p \leq gA_0 \quad (11)$$

where  $\psi = w_{z,\text{eq}}/2\sigma_{\text{mod}}$ ,  $\psi_x = w_{z,\text{eq}}/2\sigma_x$ ,  $\psi_y = w_{z,\text{eq}}/2\sigma_y$  and  $g = \exp\left(\frac{1}{\psi^2} - \frac{1}{\psi_x^2} - \frac{1}{\psi_y^2} - \frac{\mu_x^2}{2\sigma_x^2\psi_x^2} - \frac{\mu_y^2}{2\sigma_y^2\psi_y^2}\right)$ , [90], [94], [95].

We should recall here that any increase in the parameter  $\psi$  value translates into weaker amount of pointing mismatch, while  $w_{z,\text{eq}}$  represents the equivalent beam radius at the receiver, which is given as  $w_{z,\text{eq}} = \left[\sqrt{\pi}\text{erf}(v)w_z^2/2v\exp(-v^2)\right]^{1/2}$  where  $v = \sqrt{\pi}r_a/\sqrt{2}w_z$ ,  $r_a$  is the radius of the circular detection aperture and  $\text{erf}(\cdot)$  stands for the error function. Notice that  $A_0 = [\text{erf}(v)]^2$ , where  $A_0$  is the fraction of the collected power at  $r_a = 0$ , [12], [89], [94].

It is also notable that when the boresight displacement  $s = \sqrt{\mu_x^2 + \mu_y^2}$  is equal to zero, (i.e.,  $s = 0$  and thus  $\mu_x = \mu_y = 0$ ) and  $\sigma_x = \sigma_y$ , the Beckmann's distribution of the non-zero boresight pointing errors above specializes to the Rayleigh's distribution of the zero boresight, in [12]. Thus, in this case equation (10) reduces to [1, Eq (10)] and equation (11) reduces to [1, Eq (11)].

D. Combined Impact of Turbulence and Pointing Errors

Once we obtained the PDFs of the turbulence-induced fading  $I_t$  and the misalignment induced fading  $I_r$  we can now estimate their combined impact through their joint PDF of the random variable  $I = I_t I_r$ . Thus, the combined PDF,  $f_{\text{comb},I}(I)$ , for the normalized irradiance  $I$ , which arrives at the receiver's DF relay node side, is given through the following integral, [12], [16], [94]:

$$f_I(I) = \int f_{I|I_r}(I|I_r) f_{I_r}(I_r) dI_r, \quad (12)$$

where  $f_{I|I_r}(I|I_r)$  stands for the conditional probability given  $I_r$ . Thus, by using (8) and by following the analysis performed in [12], [26], [94] we get:

$$f_I(I) = \frac{\psi^2 A_{(\text{NorSR})}}{g^{\psi^2} A_0^{\psi^2}} I^{\psi^2-1} \times \sum_{(k(\text{NorSR}))} a_{k(\text{NorSR})} \int_{I/A_0}^{\infty} I_r^{\frac{\alpha+k-2\psi^2-2}{2}} K_{\alpha-k}\left(2\sqrt{B_{(\text{NorSR})}} I_r\right) dI_r. \quad (13)$$

The integral of (13) can be solved by representing the modified Bessel function in terms of Meijer's G-functions by using [123, Eq. (07.34.03.060.501)] and then, by using [123, Eq. (07.34.21.0085.01)]. Further, we apply [123, Eq. (07.34.17.0011.01)] and we conclude to the following closed-form expression for the combined

turbulence-induced and non-zero boresight misalignment-induced fading.

$$f_I(I) = \frac{\psi^2 A_{(N_{or\mathfrak{R}})} B_{(N_{or\mathfrak{R}})}}{2A_0 g} \sum_{(N_{or\mathfrak{R}})} a_{k(N_{or\mathfrak{R}})} B_{(N_{or\mathfrak{R}})}^{-\frac{a+k}{2}} \times G_{1,3}^{3,0} \left( \frac{B_{(N_{or\mathfrak{R}})}}{A_0 g} I \left| \begin{matrix} \psi^2 \\ \psi^2 - 1, a - 1, k - 1 \end{matrix} \right. \right), \quad (14)$$

where  $G_{p,q}^{m,n}[\cdot]$  stands for the Meijer-function that is a standard built in function which can be evaluated with most of the well known mathematical software packages, [124].

Additionally, the expected value of the random variable  $I$  can be estimated by solving the following integral, [84]:

$$E[I] = \int_0^\infty I f_I(I) dI. \quad (15)$$

Thus, by substituting (14) into (15), and after some calculations, [81], the expected value of the random variable  $I$  is obtained as follows:

$$E[I] = A_0 g (c + \Omega) / (\psi^2 + 1). \quad (16)$$

### III. AVERAGE BER OF THE L-QAM ROFSO SYSTEM

#### A. ABER for Each Individual OFDM RoFSO Link

One of the most well-known and crucial metric for the performance estimation of every communication system is the Bit Error Rate (BER), [18], [122], [125]. For our examined RoFSO system, we will first estimate the average BER (ABER) of each one of the  $h = 0, 1, 2, \dots, H$ , individual hops (for instance the ABER of the first hop, i.e., the nearest to the initial transmitter as mentioned above). Next, through the derived ABER expression of each individual link, the total ABER of the whole DF relayed multi-hop system will be estimated.

Assuming that Gray-coded mapping is used at the initial transmitter side and Gaussian distributed total noise in (6) as re-assumed above, the accurate ABER expression of an  $N$ -subcarriers  $L$ -QAM OFDM individual RoFSO link can be derived by averaging over all the  $N$  OFDM subcarriers, i.e., [9], [24], [125]:

$$P_{b,av}^{L-QAM} = \frac{4(1-L^{-1/2})}{N \log_2(L)} \times \sum_{n=0}^{N-1} \left\{ Q \left( \sqrt{\frac{3CNDR_n(I)}{L-1}} \right) - (1-L^{-1/2}) Q^2 \left( \sqrt{\frac{3CNDR_n(I)}{L-1}} \right) \right\} f_I(I) dI, \quad (17)$$

where  $Q(\cdot)$  stands for the well-known Q-function and as mentioned above  $L$  corresponds to the modulation index of the QAM format [125].

In order to solve the integral of Eq. (17) we are using the recently presented following approximation,  $Q^2(x) \approx [\exp(-x^2/2) + 4\exp(-11x^2/20) + 5\exp(-2x^2)]^2 / 576$ , [126]. After these substitutions, we represent both the

exponential and the complementary error function quantities in terms of Meijer-G functions by using [123, Eq. (07.34.03.0228.01)] and [123, Eq. (07.34.03.0282.01)]. Thus, by substituting also (14) into (17), we obtain integrals that entail products of two Meijer-G functions as factors. This kind of integrals can be solved by using [123, Eq. (07.34.21.0013.01)]. Next, by performing all these cumbersome calculations and by using when feasible [123, Eq. (07.34.03.0001.01)] for simplification reasons, we conclude to the following closed form mathematical expression for the ABER of each  $L$ -QAM OFDM RoFSO individual link of our examined system under  $M$ -turbulent and non-zero boresight misalignment fading conditions:

$$P_{b,av}^{L-QAM} = \frac{4(1-L^{-1/2})}{576N \log_2(L)} \times \sum_{n=0}^{N-1} \sum_{(N_{or\mathfrak{R}})} \left[ \frac{144}{\sqrt{\pi}} \frac{\xi}{(1-L^{-1/2})} \varphi^{-\xi \zeta} \left( \frac{1008}{20} \right) - \xi \zeta (120) - \xi \zeta \left( \frac{2448}{20} \right) - \frac{1}{2} \xi \zeta (48) - \frac{1}{2} \xi \zeta \left( \frac{1056}{20} \right) - \frac{1}{2} \xi \zeta (192) \right], \quad (18)$$

$$\text{where } \varphi = G_{6,3}^{2,5} \left( \frac{24A_0^2 g^2 \gamma}{(L-1) B_{(N_{or\mathfrak{R}})}^2} \left| \begin{matrix} \frac{2-\psi^2}{2}, \frac{1-a}{2}, \frac{2-a}{2}, \frac{1-k}{2}, \frac{2-k}{2}, 1 \\ 0, \frac{1}{2}, \frac{-\psi^2}{2} \end{matrix} \right. \right),$$

$$\zeta(x) = G_{5,2}^{1,5} \left( x \beta \left| \begin{matrix} \frac{2-\psi^2}{2}, \frac{1-a}{2}, \frac{2-a}{2}, \frac{1-k}{2}, \frac{2-k}{2} \\ 0, \frac{-\psi^2}{2} \end{matrix} \right. \right),$$

$$\xi = \frac{\psi^2 A_{(N_{or\mathfrak{R}})} 2^{a+k-2} a_{k(N_{or\mathfrak{R}})} B_{(N_{or\mathfrak{R}})}^{-\frac{a+k}{2}} (1-L^{-1/2})}{2\pi}, \quad \beta = \frac{A_0^2 g^2 \gamma}{B_{(N_{or\mathfrak{R}})}^2 (L-1)}$$

and thus,  $\gamma = \frac{m_n^2 \eta^2 L_{tot} P_t^2}{2([\mathcal{N}_0/T_s]_{AV} + [\sigma_{MD,n}^2]_{AV})}$ , which from Eqs (7)

and (16) it ends up to the mathematical expression,

$$\gamma = \frac{CNDR_{n,EX}}{(E[I])^2} = \frac{(1+\psi^2)^2}{A_0^2 g^2 (c + \Omega)^2} CNDR_{n,EX}. \text{ In this context, we}$$

correspondingly obtain the following equivalent expressions

$$\varphi = G_{6,3}^{2,5} \left( \frac{24(1+\psi^2)^{-2} CNDR_{n,EX}}{(L-1)(c + \Omega)^2 B_{(N_{or\mathfrak{R}})}^2} \left| \begin{matrix} \frac{2-\psi^2}{2}, \frac{1-a}{2}, \frac{2-a}{2}, \frac{1-k}{2}, \frac{2-k}{2}, 1 \\ 0, \frac{1}{2}, \frac{-\psi^2}{2} \end{matrix} \right. \right),$$

$$\beta = \frac{(1+\psi^2)^{-2} CNDR_{n,EX}}{(L-1)(c + \Omega)^2 B_{(N_{or\mathfrak{R}})}^2},$$

$$\zeta(x) = G_{5,2}^{1,5} \left( \frac{(1+\psi^2)^{-2} CNDR_{n,EX}}{(L-1)(c + \Omega)^2 B_{(N_{or\mathfrak{R}})}^2} x \left| \begin{matrix} \frac{2-\psi^2}{2}, \frac{1-a}{2}, \frac{2-a}{2}, \frac{1-k}{2}, \frac{2-k}{2} \\ 0, \frac{-\psi^2}{2} \end{matrix} \right. \right).$$

#### B. Total ABER for the Multi-hop L-QAM OFDM RoFSO System

The total average BER of the RoFSO system under consideration with the  $H$  individual hops, connected with



the (H-1) DF relay nodes that are connected both serially and equidistantly is expressed as [23], [106]

$$P_{b,av,TOTAL}^{L-QAM} = \sum_{i=1}^H \left[ P_{b,av,i}^{L-QAM} \prod_{j=i+1}^H (1 - 2P_{b,av,j}^{L-QAM}) \right], \quad (19)$$

which is a closed-form expression by substituting (18) into (19).

#### IV. OUTAGE PROBABILITY ESTIMATION

##### A. Outage Probability for Each Individual Link

Another very significant metric for the availability and performance of any RoFSO communication system is the outage probability (OP), [18], [21], [24], [52], [120]. This metric shows the probability of the CNDR at the receiver falls below a specific threshold value  $CNDR_{th}$ , which represents the lower limit for receiver's acceptable operation [9], [18], [52]. Consequently, the outage probability for each individual RoFSO hop should be

$$P_{out} = \frac{1}{N} \sum_{n=0}^{N-1} P_{out,n} = \frac{1}{N} \sum_{n=0}^{N-1} \Pr(I_n < I_{n,th}) = \frac{1}{N} \sum_{n=0}^{N-1} F_{I_n}(I_{n,th}), \quad (20)$$

where  $F_{I_n}(\cdot)$  stands for the CDF.

Therefore, in order to estimate the outage probability of each individual link of the investigated OFDM RoFSO multi-hop system, we need to obtain the CDF of the random variable  $I$  by averaging its PDF given by (14). Hence,

$$F_{I_n}(I_{n,th}) = \int_0^{I_{n,th}} f_{I_n}(I_{n,th}) dI_n = \frac{\psi^2 A_{(NOR\mathfrak{R})} B_{(NOR\mathfrak{R})}}{2A_0 g} \sum_{(NOR\mathfrak{R})} a_{k(NOR\mathfrak{R})} B_{(NOR\mathfrak{R})}^{\frac{a+k}{2}} \times \int_0^{I_{n,th}} G_{1,3}^{3,0} \left( \frac{B_{(NOR\mathfrak{R})}}{A_0 g} I_{n,th} \left| \begin{matrix} \psi^2 \\ \psi^2 - 1, a - 1, k - 1 \end{matrix} \right. \right) dI_n. \quad (21)$$

The integral of Eq. (21) is solved by using [123, Eq. (07.34.21.0084.01)], and thus, the expression (21) is written as:

$$F_{I_n}(I_{n,th}) = \frac{\psi^2 A_{(NOR\mathfrak{R})}}{2} \sum_{(NOR\mathfrak{R})} a_{k(NOR\mathfrak{R})} B_{(NOR\mathfrak{R})}^{\frac{a+k}{2}} \times G_{2,4}^{3,1} \left( \frac{B_{(NOR\mathfrak{R})}}{A_0 g} I_{n,th} \left| \begin{matrix} 1, \psi^2 + 1 \\ \psi^2, a, k, 0 \end{matrix} \right. \right). \quad (22)$$

Taking into account the Eqs (6), (7) and (16), for  $I=I_n=I_{n,th}$ , and thus, we get:

$$I_{n,th} = \frac{A_0 g (c + \Omega)}{1 + \psi^{-2}} \sqrt{\frac{CNDR_n(I_{n,th})}{CNDR_{n,EX}}}. \quad (23)$$

Hence, from (20), (22) and (23) the OP of each L-QAM OFDM RoFSO individual link impaired by both  $M$ -alaga turbulence-induced and non-zero boresight

misalignment-induced fading, can be expressed by the following closed-form expression:

$$P_{out} = \frac{\psi^2 A_{(NOR\mathfrak{R})}}{2N} \sum_{n=0}^{N-1} \sum_{(NOR\mathfrak{R})} a_{k(NOR\mathfrak{R})} B_{(NOR\mathfrak{R})}^{\frac{a+k}{2}} \times G_{2,4}^{3,1} \left( \frac{B_{(NOR\mathfrak{R})} (c + \Omega)}{1 + \psi^{-2}} \sqrt{\frac{CNDR_n(I_{n,th})}{CNDR_{n,EX}}} \left| \begin{matrix} 1, \psi^2 + 1 \\ \psi^2, a, k, 0 \end{matrix} \right. \right). \quad (24)$$

##### B. Total Outage Probability for the Multi-hop System

In serial DF relaying, an outage occurs when any of the intermediate individual links fails [114], [119], [121], [122], i.e., falls below the critical specific threshold which determines its proper operation.

The probability of at least one of the  $H$  individual links interrupts the whole examined system, is expressed as:

$$P_{out,TOTAL} = 1 - \prod_{h=1}^H (1 - P_{out}). \quad (25)$$

Hence, by substituting Eq. (24) into (25) we obtain the following closed-form expression of the outage probability of the total DF relayed multi-hop L-QAM OFDM RoFSO examined system:

$$P_{out,TOTAL} = 1 - \prod_{h=1}^H \left\{ 1 - \frac{\psi^2 A_{(NOR\mathfrak{R})}}{2N} \sum_{n=0}^{N-1} \sum_{(NOR\mathfrak{R})} a_{k(NOR\mathfrak{R})} B_{(NOR\mathfrak{R})}^{\frac{a+k}{2}} \times G_{2,4}^{3,1} \left( \frac{B_{(NOR\mathfrak{R})} (c + \Omega)}{1 + \psi^{-2}} \sqrt{\frac{CNDR_n(I_{n,th})}{CNDR_{n,EX}}} \left| \begin{matrix} 1, \psi^2 + 1 \\ \psi^2, a, k, 0 \end{matrix} \right. \right) \right\}. \quad (26)$$

#### V. NUMERICAL RESULTS

##### A. RoFSO System under Assumption

In this section by using the closed-form expressions derived above, (18), (19), (26), we present performance results by means of both quantities, i.e. average BER and outage probability. The RoFSO system under consideration may operate either with or without DF relays in multi-hop L-QAM OFDM configurations. The number of OFDM subcarriers is fixed at  $N=1000$ , while three values for the QAM signal constellation  $L$  are assumed, i.e.  $L=4, 16$  or  $64$ . The operational wavelength of the system is fixed at  $\lambda=1.55 \mu\text{m}$ , while its receiver's aperture diameter,  $D$ , is set at  $0.1 \text{ m}$ . Furthermore, each of the  $h=1, 2 \dots H$  hops are assumed to have the same, equal to  $1 \text{ km}$ , link length. When  $H=1$  the system is not a relay-assisted one but a regular line of sight link. In the examined RoFSO links below, the number of relays ( $H-1$ ), is varying from 0 to 10. In all investigated cases, the operation of this RoFSO system is assumed to be impaired by the combined influence of turbulence-induced and non-zero boresight misalignment-induced fading. In this context, a wide range of weak to strong turbulence conditions is assumed, modeled through the accurate  $M$ -alaga distribution model. More precisely, we examine the following  $M$ -parameter values,  $a=3, b=3, \rho=0.95$  for strong and  $a=8, b=4, \rho=0.95$  for weak

turbulence conditions. In addition, in all cases we will present below, the average optical power of each RoFSO link is normalized, i.e.,  $\Omega + 2b_0 = 1, \Omega = 0.5, b_0 = 0.25$ . Note that this simplification for the average optical power holds true, without loss of generality. As regards the pointing mismatch, we assume normalized beam width value  $w_z/r = 10$ , as well as the normalized boresight error values are fixed at  $(\mu_x/r, \mu_y/r) = (1, 2)$ , while different normalized jitter values,  $(\sigma_x/r, \sigma_y/r) = (1.2, 0.9)$ ,  $(\sigma_x/r, \sigma_y/r) = (2.6, 1.4)$  and  $(\sigma_x/r, \sigma_y/r) = (3.6, 2.7)$  are investigated that correspond to  $\psi = 3.5$ ,  $\psi = 2.0$  and  $\psi = 1.5$ , respectively, i.e., to weak, moderate and strong amount of non-zero boresight pointing mismatch respectively. Moreover, the corresponding Monte Carlo simulations are presented by solid dots, which validate the results obtained. Note that in order to avoid excessively long simulation runtimes, we do not generate results for values lower than  $10^{-6}$ .

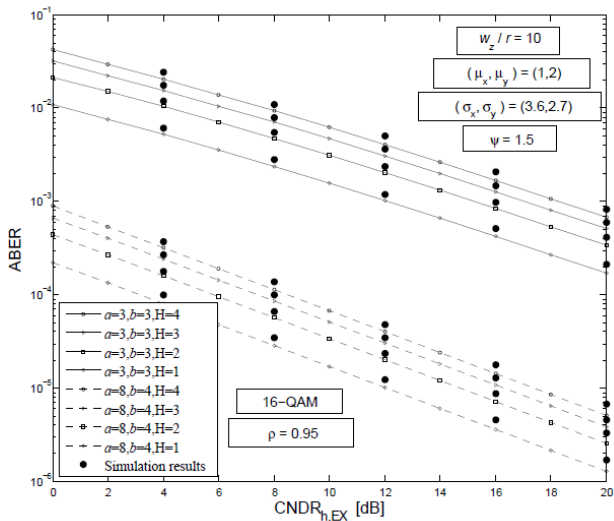


Fig. 1. Average BER of 16-QAM OFDM signals versus a wide range of CNDR for various number of RoFSO hops over weak to strong turbulence  $\mathcal{M}$ (alaga)-channels along with strong non-zero boresight misalignment-induced fading.

Fig. 1 illustrates the evolution of the ABER expressions (18) and (19) as a function of a wide range of expected CNDR at the receiver's side, of different number 16-QAM OFDM RoFSO links, under different  $M$ -turbulence conditions along with the same strong non-zero boresight misalignment-induced fading. Thus, the detrimental impact of atmospheric turbulence effect is highlighted in this figure. Indeed, as the atmospheric turbulence is getting weaker, i.e. as the parameters  $a$  and  $b$  obtain larger values -cases of  $a=8, b=4$  that are visualized in dashed line style- it is clearly shown that decreased ABER values are obtained and thus, significant RoFSO performance improvements are depicted in this weak turbulence regime in comparison with the strong turbulence one i.e. cases of  $a=3, b=3$ . In each turbulence regime, four different hop-configurations are illustrated.

As we can see, the increase of the number of hops  $H$  leads to longer RoFSO total link lengths. More specifically, each additional hop increases the total link length by 1 km but at the expense of increased ABER values, which translates into performance degradations in comparison with the initial shorter link. However, especially for high CNDR values, which significantly mitigate the ABER, the performance degradations due to DF relays employment are not proved to be so destructive to make the RoFSO system unreliable. In short, Fig. 1 reveals that the performance of a typical 16-QAM OFDM RoFSO DF relayed multi-hop system is significantly degraded by atmospheric turbulence, by decreased expected CNDR values and by employing a large number of DF relays connected in series, despite the far broadened coverage area they provide.

Fig. 2 depicts the evolution of the ABER expressions (18) and (19) as a function of the same wide range of expected CNDR at the receiver's side. The assumptions for the RoFSO system's characteristics are the same as in Fig. 1, but the parameter  $\psi$  in now fixed at a larger value that corresponds to a weaker amount non-zero boresight misalignment-induced fading. As we can observe, all the corresponding to Fig. 1 ABER values are significantly reduced. As a result, Fig. 2 compared to Fig. 1, demonstrates the performance-destructive impact of non-zero boresight pointing errors on RoFSO systems.

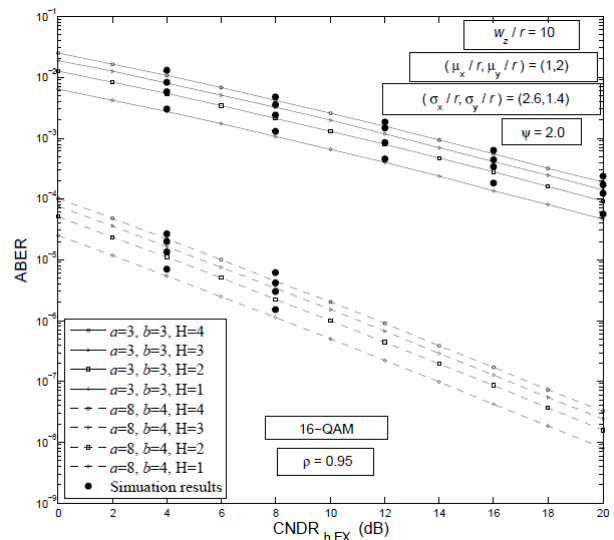


Fig. 2. Average BER of 16-QAM OFDM signals versus a wide range of CNDR for various number of RoFSO hops over weak to strong turbulence  $\mathcal{M}$ (alaga)-channels along with moderate non-zero boresight misalignment-induced fading.

Fig. 3 visualize the evolution of the ABER expressions (18) and (19) as a function of a wide range of the expected CNDR at the receiver's under strong  $M$ -alaga turbulence and moderate non-zero boresight pointing errors for different  $L$ -QAM formats, i.e.  $L=4, 16$  or  $64$ . The  $L$ -QAM OFDM RFSO system is considered to be a multi-hop one that may employ either 4 or 10 serially connected DF relays, which create  $H=5$  or  $H=10$  intermediate individual links, respectively. As it should

be expected from the above, we unsurprisingly observe that the  $H=5$  configuration, which is illustrated by dashed lines, outperforms in terms of ABER to the  $H=10$  one. However, the latter configuration has the advantage of broader coverage area. Additionally in both multi-hop configurations it becomes evident that the lower order QAM schemes lead to significant performance enhancement. Thus, 4-QAM offers better ABER performance results than 16-QAM scheme, which outperforms, in turn, to 64-QAM format.

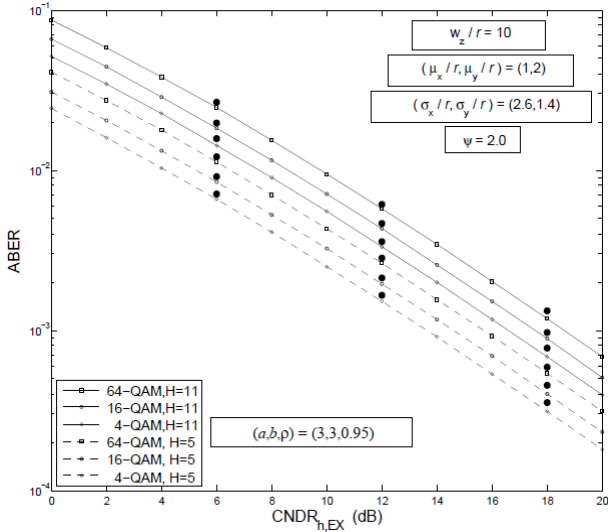


Fig. 3. Average BER of 4, 16, 64-QAM OFDM signals versus a wide range of CNDR for various number of RoFSO hops over strong turbulence  $\mathcal{M}$ (alaga)-channel along with moderate non-zero boresight misalignment-induced fading.

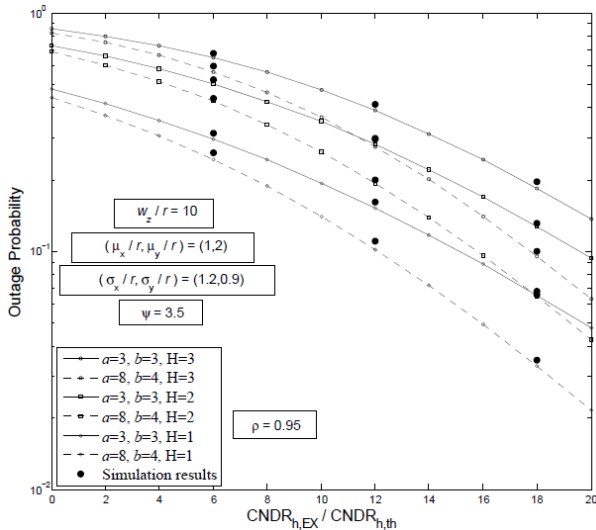


Fig. 4. Outage Probability estimation of single and multi-hop OFDM RoFSO systems over weak to strong turbulence  $\mathcal{M}$ (alaga)-channels along with weak non-zero boresight misalignment-induced fading.

Fig. 4 shows the OP results obtained by using (26) for a single-hop, a dual-hop and a triple-hop RoFSO OFDM system. This performance-metric is presented as a function of the normalized expected carrier to noise plus distortion,  $CNDR_{h,EX}/CNDR_{h,th}$ , at each DF receiver. Similarly to the ABER metric, the OP is showed to

increase its value as the number of individual hops, or equivalently, as the number of DF relays employed increases. Once again, the increase of turbulence strength leads to further performance degradation, i.e. to further increase of the OP value. Consequently, especially under weak turbulence conditions, the single-hop system outperforms in terms of OP, while the triple-hop system outperforms in terms of coverage area.

Fig. 5 illustrates the OP results obtained by using (26) for the same RoFSO OFDM systems with Fig. 4, operating under the same turbulence conditions again, but under the presence of strong non-zero boresight pointing errors this time, as indicates the decrease of  $\psi$  parameter from 3.5 in Fig. 4, to 1.5 in Fig. 5. The comparison between these two figures reveals the detrimental impact of non-zero boresight pointing errors in terms of RoFSO outage probability.

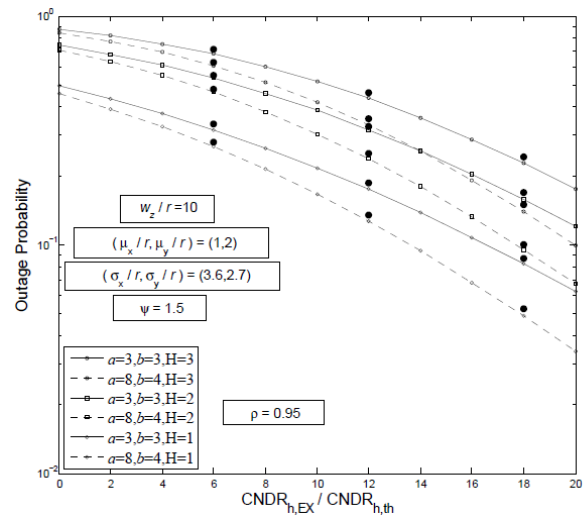


Fig. 5. Outage Probability estimation of single and multi-hop OFDM RoFSO systems over weak to strong turbulence  $\mathcal{M}$ (alaga)-channels along with strong non-zero boresight misalignment-induced fading.

### B. Practical RoFSO System

In order to verify our proposed performance analysis on a practical level, we present here some numerical results derived by (26), but by adopting some experimental data measurements of a real optical wireless link, performed in University of Waseda, Japan, on the 15th October, 2009, as it was presented in [82]. This practical link operates with optical wavelength  $\lambda = 785$  nm and receiver's aperture diameter of 0.1m. Its length, i.e. the wireless FSO propagation distance from source to destination is  $d_{SD} = 1$  km. Additionally, it is established at a height of 25 m above the sea level, while the optical power transmitted is 11.5 dBm with a responsivity of 0.8 A/W, [82].

We ought to recall here that the atmospheric turbulence is dependent on the Rytov variance, defined as  $\sigma_R^2 = 1.23C_n^2 (2\pi/\lambda)^{7/6} d_{SD}^{11/6}$ , which is constant and takes a value  $\sigma_R^2 = 0.36$  for the refractive index structure

parameter  $C_n^2 = 8.3 \times 10^{-15} \text{ m}^{-2/3}$  (which was measured on the 15th October 2009, at time 23:10), FSO propagation distance  $d_{SD} = 1 \text{ km}$  and employed  $\lambda = 785 \text{ nm}$ . Considering that *M-alaga* distribution is a very accurate unifying model, the latter experimental-measured turbulence state for this specific practical link entirely corresponds to  $(a, b, \rho) = (10, 5, 1)$  *M*-parameter values, as it is reported in Ref. [82]. Thus, this *M*-turbulent state  $(a, b, \rho) = (10, 5, 1)$  will be used in our numerical results below. Similarly, another stronger *M*-turbulent state that results from experimental data and could be used below, is the state with  $(a, b, \rho) = (10, 5, 0.25)$  that fully corresponds to a value  $\sigma_R^2 = 1.2$  and  $C_n^2 = 2.8 \times 10^{-14} \text{ m}^{-2/3}$  (which was measured on the 15th October 2009, near midday, [82]). Moreover, the non-zero boresight misalignment fading is fixed to be moderate and equal to all the examined cases. As a final remark, all cases that will be shown below were obtained, once again and without loss on generality, by employing the same normalized average optical power, i.e.  $\Omega + 2b_0 = 1$ , where  $\Omega = 0.5$  and  $b_0 = 0.25$ .

In view of the above, Fig. 6 depicts three different OFDM RoFSO realizations of the investigated practical link. The most performance-effective in terms of outage probability is the original link's configuration over weak measured turbulence conditions, i.e. with  $(a, b, \rho) = (10, 5, 1)$  and total link length equal to 1 km, without any DF relay employment. The same single-hop link, but under stronger turbulence conditions, i.e.,  $(a, b, \rho) = (10, 5, 0.25)$  and longer link length equal to 2 km is shown to obtain increased corresponding OP values compared to the immediately above case. This is due to the fact that stronger turbulent channels lead to more significant availability and performance RoFSO degradations, as well as, the increase of the propagation distance (without using relays) brings about stronger turbulence induced-fading at the receiver side. Finally, the third configuration, represented by a dashed line, is assumed to have also an extended total length of 2 km, but employs a DF relay which is assumed to be placed in the middle of the total link (i.e., dual-hop configuration with hop lengths equal to 1 km). The use of DF relay enables the dual-hop system to deal with a weaker amount of turbulence-induced fading in each hop than the second mentioned configuration, which despite having the same total link length of 2km it has to deal with a stronger amount of turbulence-induced fading at the receiver's side. This explains the better performance results that may offer the dual-hop scheme, compared to the second-mentioned configuration, provided that the receiver of the DF relay has the proper *CNDR* sensitivity limit. Consequently, apart from increasing the coverage RoFSO area, DF relays, may also be used as a fading-

mitigation tool to combat the combined impact of turbulence and pointing errors.

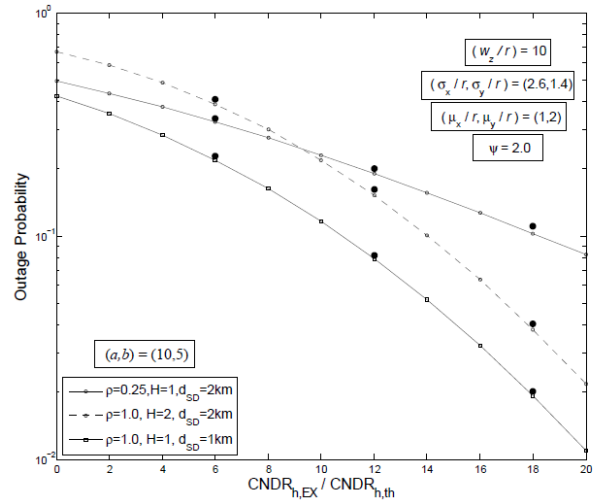


Fig. 6. Outage Probability estimation of three different configurations of a practical OFDM RoFSO system over weak to strong turbulence *M*(alaga)-channels along with moderate non-zero boresight misalignment-induced fading.

## VI. CONCLUSIONS

In this work, the combined impact of both *M*-alaga modeled turbulence and non-zero boresight pointing errors effect on the performance of a multi-hop DF relayed with *N*-subcarriers *L*-QAM OFDM RoFSO system is investigated. Thus, accurate enough closed-form expressions are derived for the fundamental ABER and the outage probability performance metrics of such RoFSO configurations. It was demonstrated that DF relays connected in series can significantly broaden the RoFSO coverage area, but at the expense of increased ABER and OP values, in comparison with the corresponding ABER and OP values of the initial shorter RoFSO link. Additionally, it was shown that by inserting serially connected DF relays in a RoFSO link we may improve its initial performance, since the resulting intermediate individual hops are shorter, and thus, they have to deal with a weaker amount of combined turbulence-induced and non-zero boresight misalignment-induced fading.

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