

# An Efficient Tag Search Protocol in Large-Scale RFID Systems With Noisy Channel

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**Abstract**—Radio frequency identification (RFID) technology has many applications in inventory management, supply chain, product tracking, transportation, and logistics. One research issue of practical importance is to search for a particular group of tags in a large-scale RFID system. Time efficiency is a crucial factor that must be considered when designing a tag search protocol to ensure its execution will not interfere with other normal inventory operations. In this paper, we design a new technique called *filtering vector*, which can significantly reduce transmission overhead during search process, thereby shortening search time. Based on this technique, we propose an iterative tag search protocol. In each round, we filter out some tags and eventually terminate the search process when the search result meets the accuracy requirement. Furthermore, we extend our protocol to work under noisy channel. The simulation results demonstrate that our protocol performs much better than the best existing work.

**Index Terms**—Noisy channel, radio frequency identification (RFID), tag search, time efficiency.

## I. INTRODUCTION

RECENT years have witnessed the rapid development of radio frequency identification (RFID) technology. It is becoming increasingly utilized in various applications, such as inventory management, supply chain, product tracking, transportation, and logistics [1]–[10]. Generally speaking, an RFID system comprises three components: one or multiple RFID readers, a large set of RFID tags, and a back-end server. Each tag has a unique ID to identify the object to which it is attached. Equipped with an antenna, a tag is capable of transmitting and receiving radio signals, through which communications with the readers are achieved. Hence, the readers can collect the IDs and other useful information from tags located in their coverage areas, and then send the gathered data to the back-end server for further process.

This paper focuses on the *tag search problem* in large RFID systems. We use an example to illustrate the problem. Suppose a manufacturer finds that some of its products may be defective, but those products have already been distributed in different

warehouses. The manufacturer knows the IDs of tags attached to those suspected products and wants to recall them for further inspection. Thus, the manufacturer asks for a tag search in each warehouse: Given a set of *wanted* tag IDs, the problem is to search in the coverage area of a reader and identify the tags that belong to the set. Note that there may exist other tags in the area that do not belong to the set.

To meet the stringent delay requirements of real-world applications, time efficiency is a critical performance metric for the RFID tag search problem. In our example, it is highly desirable to make the search quick in a busy warehouse as a lengthy searching process may interfere with other activities that move things in and out of the warehouse. The only prior work studying this problem is called CATS [11], which however does not work well under some common conditions (e.g., if the size of the wanted set is much larger than the number of tags in the coverage area of the reader).

The main contribution of this paper is a fast tag search method based on a new technique called *filtering vectors*. A filtering vector is a compact one-dimension bit array constructed from tag IDs, which can be used not only for tag filtration, but also for parameter estimation. Using the filtering vectors, we design, analyze, and evaluate a novel iterative tag search protocol, which progressively improves the accuracy of search result and reduces the time of each iteration to a minimum by using the information learned from previous iterations. Given an accuracy requirement, the iterative protocol will terminate once the search result meets the accuracy requirement. We show that our protocol performs much better than the CATS protocol and other alternatives that we use for comparison. We then extend our protocol to work under noisy channel and demonstrate that the increase in its execution time due to channel error is modest.

The rest of this paper is organized as follows. Section II gives the system model and the problem statement. Section III briefly introduces the prior work. Section IV describes our new protocol in detail. Section VI evaluates the performance of our protocol by simulations. Section V addresses noisy wireless channel. Section VII discusses the related work. Section VIII draws the conclusion.

## II. SYSTEM MODEL AND PROBLEM STATEMENT

### A. System Model

We consider an RFID system of one or more readers, a back-end server, and a large number of tags. Each tag has a unique 96-bit ID according to the EPC global Class-1 Gen-2 (C1G2) standard [12]. A tag is able to communicate with the reader wirelessly and perform some computations such as hashing. The back-end server is responsible for data storage,

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information processing, and coordination. It is capable of carrying out high-performance computations. Each reader is connected to the back-end server via a high-speed wired or wireless link. If there are many readers (or antennas), we divide them into noninterfering groups, and the protocol proposed in this paper (or any prior protocol) can be performed for one group at a time, with the readers in that group executing the protocol in parallel. The readers in each group can be regarded as an integrated unit, still called a reader for simplicity. Many works regarding multireader coordination can be found in the literature [13]–[15].

In practice, the tag-to-reader transmission rate and the reader-to-tag transmission rate may be different and subject to the environment. For example, as specified in the EPC global Class-1 Gen-2 standard, the tag-to-reader transmission rate is 40–640 kb/s in the FM0 encoding format or 5–320 kb/s in the Miller modulated subcarrier encoding format, while the reader-to-tag transmission rate is about 26.7–128 kb/s. However, to simplify our discussions, we assume the tag-to-reader transmission rate and the reader-to-tag transmission rate are the same, and it is straightforward to adapt our protocol for asymmetric transmission rates.

### B. Time-Slots

The RFID reader and the tags in its coverage area use a framed slotted MAC protocol to communicate. We assume that clocks of the reader and all tags in the RFID system are synchronized by the reader’s signal. During each frame, the communication is initialized by the reader in a request-and-response mode, namely, the reader broadcasts a request with some parameters to the tags and then waits for the tags to reply in the subsequent time-slots.

Consider an arbitrary time-slot. We call it an *empty slot* if no tag replies in this slot, or a *busy slot* if one or more tags respond in this slot. Generally, a tag just needs to send one-bit information to make the channel busy such that the reader can sense its existence. The reader uses “0” to represent an empty slot with an idle channel and “1” for a busy slot with a busy channel. The length of a slot for a tag to transmit a one-bit short response is denoted as  $t_s$ . Note that  $t_s$  can be set larger than the time of one-bit data transmission for better tolerance of clock drift in tags. Some prior RFID work needs another type of slots for transmission of tag IDs, which will be introduced shortly.

### C. Problem Statement

Suppose we are interested in a known set of tag IDs  $X = \{x_1, x_2, x_3, \dots\}$ , where each  $x_i \in X$  is called a *wanted tag*. For example, the set may contain tag IDs on a certain type of products under recall by a manufacturer. Let  $Y = \{y_1, y_2, y_3, \dots\}$  be the set of tags within the coverage area of an RFID system (e.g., in a warehouse). Each  $x_i$  or  $y_i$  represents a tag ID. The *tag search problem* is to identify the subset  $W$  of wanted tags that are present in the coverage area. Namely,  $W \subseteq X$ . Since each tag in  $W$  is in the coverage area,  $W \subseteq Y$ . Therefore,  $W = X \cap Y$ . We define the *intersection ratio* of  $X$  and  $Y$  as

$$R_{\text{INTS}} = \frac{|W|}{\min\{|X|, |Y|\}}. \quad (1)$$

Exactly finding  $W$  can be expensive if  $X$  and  $Y$  are very large. It is much more efficient to find  $W$  approximately, allowing small bounded error [11]—all wanted tags in the

TABLE I  
NOTATIONS

| Symbols     | Descriptions  |
|-------------|---|
| $X$         | Set of wanted tags  |
| $Y$         | Set of tags in the RFID system  |
| $W$         | Intersection of $X$ and $Y$ , i.e., $W = X \cap Y$  |
| $X_i$       | Set of remaining candidate tags in $X$ , i.e., search result at the beginning of the $i^{\text{th}}$ round of our protocol; |
| $Y_i$       | Set of remaining candidate tags in $Y$ at the beginning of the $i^{\text{th}}$ round of our protocol                        |
| $U_i$       | Difference between $X_i$ and $W$ , i.e., $U_i = X_i - W$  |
| $V_i$       | Difference between $Y_i$ and $W$ , i.e., $V_i = Y_i - W$  |
| $ \cdot $   | Cardinality of the set  |
| $h(\cdot)$  | A uniform hash function   |
| $FV(\cdot)$ | Filtering vector of a set   |

coverage area must be identified, but a few wanted ones that are not in the coverage may be accidentally included.<sup>1</sup>

Our solution performs iteratively. Each round rules out some tags in  $X$  when it becomes certain that they are not in the coverage area (i.e.,  $Y$ ), and it also rules out some tags in  $Y$  when it becomes certain that they are not wanted ones in  $X$ . These ruled-out tags are called *non-candidate tags*. Other tags that remain possible to be in both  $X$  and  $Y$  are called *candidate tags*. At the beginning, the search result is initialized to all wanted tags  $X$ . As our solution is iteratively executed, the search result shrinks toward  $W$  when more and more non-candidates are ruled out.

Let  $W^*$  be the final search result. We have the following two requirements.

- 1) All wanted tags in the coverage area must be detected, namely,  $W \subseteq W^*$ .
- 2) A *false positive* occurs when a tag in  $X - W$  is included in  $W^*$ , i.e., a tag not in the coverage area is kept in the search result by the reader.<sup>2</sup> The *false-positive ratio* is the probability for any tag in  $X - W$  to be in  $W^*$  after the execution of a search protocol. We want to bound the false-positive ratio by a prespecified system requirement  $P_{\text{REQ}}$ , whose value is set by the user. In other words, we expect

$$\frac{|W^* - W|}{|X - W|} \leq P_{\text{REQ}}. \quad (2)$$

Notations used in the paper are given in Table I for quick reference.

## III. BACKGROUND

### A. Tag Identification

A straightforward solution for the tag search problem is identifying all existing tags in  $Y$ . After that, we can apply an intersection operation  $X \cap Y$  to compute  $W$ . EPC C1G2 standard assumes that the reader can only read one tag ID at a time. *Dynamic Framed Slotted ALOHA* (DFSA) [16]–[20] is implemented to deal with tag collisions, where each frame consists of a certain number of equal-duration slots. It is proved that the theoretical upper bound of identification throughput using DFSA is approximately  $\frac{1}{e}$  tags per slot ( $e$  is the natural constant), which

<sup>1</sup>If perfect accuracy is necessary, a post-step may be taken by the reader to broadcast the identified IDs. As the wanted tags in the coverage reply after hearing their IDs, those mistakenly included tags can be excluded due to non-response to these IDs.

<sup>2</sup>The nature of our protocol guarantees that all tags in  $Y - W$  are not included in  $W^*$ .

is achieved when the frame size is set equal to the number of unidentified tags [21]. As specified in EPC C1G2, each slot consists of the transmissions of a *QueryAdjust* or *QueryRep* command from the reader, one tag ID, and two 16-bit random numbers: one for the channel reservation (collision avoidance) sent by the tags, and the other for ACK/NAK transmitted by the reader. We denote the duration of each slot for tag identification as  $t_l$ . Therefore, the lower bound of identification time for tags in  $Y$  using DFSA is

$$T_{\text{DFSA}} = e \times |Y| \times t_l. \quad (3)$$

One limitation of the current DFSA is that the information contained in collision slots is wasted. A number of recent papers [22]–[27] focus on *collision recovery* (CR) techniques, which enable the resolution of multiple tag IDs from a collision slot. Benefiting from the CR techniques, the identification throughput can be dramatically improved up to 3.1 tags per slot in [26]. Suppose the throughput is  $v$  tags per slot after adopting the CR techniques. The lower bound for identification time is

$$T_{\text{CR}} = \frac{|Y|}{v} \times t_l. \quad (4)$$

Note that after employing the CR techniques, the real duration of each slot can be longer than  $t_l$ . The reason is that the reader may need to acknowledge multiple tags and the tags may need to send extra messages to facilitate collision recovery.

Readers may refer to Section VII for more information about tag identification and collision recovery.

### B. Polling Protocol

The polling protocol provides an alternative solution to the tag search problem. Instead of collecting all IDs in  $Y$ , the reader can broadcast the IDs in  $X$  one by one. Upon receiving an ID, each tag checks whether the received ID is identical to its own. If so, the tag transmits a one-bit short response to notify the reader about its presence; otherwise, the tag keeps silent. Hence, the execution time of the polling protocol is

$$T_{\text{Polling}} = |X| \times (t_{\text{id}} + t_s) \quad (5)$$

where  $t_{\text{id}}$  is the time cost for the reader to broadcast a tag ID.

The polling protocol is very efficient when  $|X|$  is small. However, it also has serious limitations. First, it does not work well when  $|X| \gg |Y|$ . Second, the energy consumption of tags (particularly when active tags are used) is significant because tags in  $Y$  have to continuously listen to the channel and receive a large number of IDs until its own ID is received.

### C. CATS Protocol

To address the problems of the tag identification and polling protocols, Zheng *et al.* propose a two-phase protocol named *Compact Approximator-based Tag Searching protocol* (CATS) [11], which is the most efficient solution for the tag search problem to date.

The main idea of the CATS protocol is to encode tag IDs into a Bloom filter and then transmit the Bloom filter instead of the IDs. In its first phase, the reader encodes all IDs of wanted tags in  $X$  into a  $L_1$ -bit Bloom filter, and then broadcasts this filter together with some parameters to tags in the coverage area. Having received this Bloom filter, each tag tests whether it belongs to the set  $X$ . If the answer is negative, the tag is a non-candidate and will keep silent for the remaining time. After

the filtration of phase one, the number of candidate tags in  $Y$  is reduced. During the second phase, the remaining candidate tags in  $Y$  report their presence in a second  $L_2$ -bit Bloom filter constructed from a frame of time-slots  $t_s$ . Each candidate tag transmits in  $k$  slots to which it is mapped. Listening to channel, the reader builds the Bloom filter based on the status of the time-slots: “0” for an idle slot where no tag transmits, and “1” for a busy slot where at least one tag transmits. Using this Bloom filter, the reader conducts filtration for the IDs in  $X$  to see which of them belong to  $Y$ , and the result is regarded as  $X \cap Y$ .

With a prespecified false-positive ratio requirement  $P_{\text{REQ}}$ , the CATS protocol uses the following optimal settings for  $L_1$  and  $L_2$ :

$$L_1 = |X| \log_{\phi} \left( -\frac{\alpha|X|}{\beta|Y| \ln P_{\text{REQ}}} \right) \quad (6)$$

$$L_2 = \frac{|X|}{\ln \phi} \left( \ln P_{\text{REQ}} - \frac{\alpha}{\beta} \right) \quad (7)$$

where  $\phi$  is a constant that equals 0.6185, and  $\alpha$  and  $\beta$  are constants pertaining to the reader-to-tag transmission rate and the tag-to-reader transmission rate, respectively. In CATS, the authors assume  $t_s$  is the time needed to delivering one-bit data, and  $\alpha = \beta$ , i.e., the reader-to-tag transmission rate and the tag-to-reader transmission rate are identical. Therefore, the total search time of the CATS protocol is

$$\begin{aligned} T_{\text{CATS}} &= (L_1 + L_2) \times t_s \\ &= |X| \left( \log_{\phi} \left( \frac{-|X|}{|Y| \ln P_{\text{REQ}}} \right) + \frac{\ln P_{\text{REQ}} - 1}{\ln \phi} \right) \times t_s. \end{aligned} \quad (8)$$

## IV. FAST TAG SEARCH PROTOCOL BASED ON FILTERING VECTORS

In this section, we propose an *Iterative Tag Search Protocol* (ITSP) to solve the tag search problem in large-scale RFID systems. We will ignore channel error for now and delay this subject to Section V.

### A. Motivation

Although the CATS protocol takes a significant step forward in solving the tag search problem, it still has several important drawbacks. First, when optimizing the Bloom filter sizes  $L_1$  and  $L_2$ , CATS approximates  $|X \cap Y|$  simply as  $|X|$ . This rough approximation may cause considerable overhead when  $|X \cap Y|$  deviates significantly from  $|X|$ .

Second, it assumes that  $|X| < |Y|$  in its design and formula derivation. In reality, the number of wanted tags may be far greater than the number in the coverage area of an RFID system. For example, there may be a huge number  $|X|$  of tagged products that are under recall, but as the products are distributed to many warehouses, the number  $|Y|$  of tags in a particular warehouse may be much smaller than  $|X|$ . Although CAT can still work under conditions of  $|X| \gg |Y|$ , it will become less efficient as our simulations will demonstrate.

Third, the performance of CATS is sensitive to the false-positive ratio requirement  $P_{\text{REQ}}$ . The performance deteriorates when the value of  $P_{\text{REQ}}$  is very small. While the simulations in [11] set  $P_{\text{REQ}} = 5\%$ , its value may have to be much smaller in some practical cases. For example, suppose  $|X| = 100\,000$ , and  $|W| = 1000$ . If we set  $P_{\text{REQ}} = 5\%$ , the number of wanted tags that are *falsely claimed* to be in  $Y$  by CATS will be up to

$|X - W| \times P_{\text{REQ}} = 4995$ , far more than the 1000 wanted tags that are actually in  $Y$ .

We will show that an iterative way of implementing Bloom filters is much more efficient than the classical way that the CATS protocol adopts.

### B. Bloom Filter

A Bloom filter is a compact data structure that encodes the membership for a set of items. To represent a set  $S = \{e_1, e_2, \dots, e_n\}$  using a Bloom filter, we need a bit array of length  $l$  in which all bits are initialized to zeros. To encode each element  $e \in S$ , we use  $k$  hash functions,  $h_1, h_2, \dots, h_k$ , to map the element randomly to  $k$  bits in the bit array, and set those bits to ones. For membership lookup of an element  $b$ , we again map the element to  $k$  bits in the array and see if all of them are ones. If so, we claim that  $b$  belongs to  $S$ ; otherwise, it must be true that  $b \notin S$ . A Bloom filter may cause false positive: A non-member element is falsely claimed as a member in  $S$ . The probability for a false positive to occur in a membership lookup is given as follows [28]:

$$P_B = \left(1 - \left(1 - \frac{1}{l}\right)^{kn}\right)^k \approx \left(1 - e^{-kn/l}\right)^k. \quad (9)$$

When  $k = \ln 2 \times \frac{l}{n}$ ,  $P_B$  is approximately minimized to  $\left(\frac{1}{2}\right)^k = \left(\frac{1}{2}\right)^{\ln 2 \frac{l}{n}}$ . In order to achieve a target value of  $P_B$ , the minimum size of the filter is  $-\frac{\ln P_B}{(\ln 2)^2} n$ .

CATS sends one Bloom filter from the reader to tags and another Bloom filter from tags back to the reader. Consider the first Bloom filter that encodes  $X$ . As  $n = |X|$ , the filter size is  $-\frac{\ln P_B}{(\ln 2)^2} |X|$ . As an example, to achieve  $P_B = 0.001$ , the size becomes  $14.4 \times |X|$  bits. Similarly, the size of the second filter from tags to the reader is also related to the target false-positive probability.

We show that the overall size of the Bloom filter can be significantly reduced by reconstructing it as filtering vectors and then *iteratively applying these vectors*.

### C. Filtering Vectors

A Bloom filter can also be implemented in a segmented way. We divide its bit array into  $k$  equal segments, and the  $i$ th hash function will map each element to a random bit in the  $i$ th segment, for  $i \in [1 \dots k]$ . We name each segment as a *filtering vector* (FV), which has  $l/k$  bits. The following formula gives the false-positive probability of a single filtering vector, i.e., the probability for a non-member to be hashed to a ‘‘1’’ bit in the vector:

$$P_{\text{FV}} = 1 - \left(1 - \frac{1}{l/k}\right)^n \approx 1 - e^{-kn/l}. \quad (10)$$

Since there are  $k$  independent segments, the overall false-positive probability of a segmented Bloom filter is

$$P_{\text{FP}} = (P_{\text{FV}})^k \approx \left(1 - e^{-kn/l}\right)^k \quad (11)$$

which is approximately the same as the result in (9). It means that the two ways of implementing a Bloom filter have similar performance. The value  $P_{\text{FP}}$  is also minimized when  $k = \ln 2 \times \frac{l}{n}$ . Hence, the optimal size of each filtering vector is

$$\frac{l}{k} = \frac{n}{\ln 2} \quad (12)$$

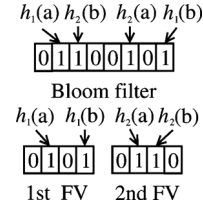


Fig. 1. Bloom filter and filtering vectors.

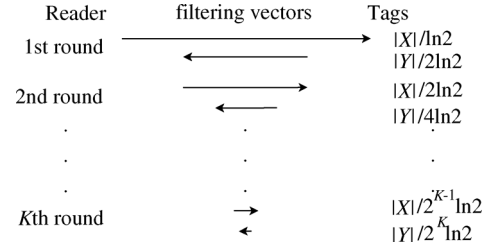


Fig. 2. Iterative use of filtering vectors. Each arrow represents a filtering vector, and the length of the arrow indicates the size of the filtering vector, which is specified to the right. As the size shrinks in subsequent rounds, the total amount of data exchanged between the reader and the tags is significantly reduced.

which results in

$$P_{\text{FV}} \approx \frac{1}{2}. \quad (13)$$

Namely, each filtering vector on average filters out half of non-members.

Fig. 1 illustrates the concept of filtering vectors. Suppose we have two elements  $a$  and  $b$ , two hash functions  $h_1$  and  $h_2$ , and an 8-bit bit array. First, suppose  $h_1(a) \bmod 8 = 1$ ,  $h_1(b) \bmod 8 = 7$ ,  $h_2(a) \bmod 8 = 5$ ,  $h_2(b) \bmod 8 = 2$ , and we construct a Bloom filter for  $a$  and  $b$  in the upper half of the figure. Next, we divide the bit array into two 4-bit filtering vectors and apply  $h_1$  to the first segment and  $h_2$  to the second segment. Since  $h_1(a) \bmod 4 = 1$ ,  $h_1(b) \bmod 4 = 3$ ,  $h_2(a) \bmod 4 = 1$ ,  $h_2(b) \bmod 4 = 2$ , we build the two filtering vectors in the lower half of the figure.

### D. Iterative Use of Filtering Vectors

In this work, we use filtering vectors in a novel iterative way: Bloom filters between the reader and tags are exchanged in rounds; one filtering vector is exchanged in each round, and the size of filtering vector is continuously reduced in subsequent rounds, such that the overall size of each Bloom filter is greatly reduced.

We use a simplified example to explain the idea, which is illustrated in Fig. 2: Suppose there is no wanted tag in the coverage area of an RFID reader, namely,  $X \cap Y = \emptyset$ . In round one, we first encode  $X$  in a filtering vector of size  $|X|/\ln 2$  through a hash function  $h_1$  and broadcast the vector to filter tags in  $Y$ . Using the same hash function, each candidate tag in  $Y$  knows which bit in the vector it is mapped to, and it only needs to check the value of that bit. If the bit is zero, the tag becomes a non-candidate and will not participate in the protocol execution further. The filtering vector reduces the number of candidate tags in  $Y$  to about  $|Y| \times P_{\text{FV}} \approx |Y|/2$ . Then, a filtering vector of size  $|Y|/(2 \ln 2)$  is sent from the remaining candidate tags in  $Y$  back to the reader in a way similar to [11]: Each candidate tag hashes its ID to a slot in a time frame and transmits one-bit response in that slot. By listening to the states of the slots in the time frame, the reader constructs the filtering vector, ‘‘1’’ for busy slots and

“0” for empty slots. The reader uses this vector to filter non-candidate tags from  $X$ . After filtering, the number of candidate tags remaining in  $X$  is reduced to about  $|X| \times P_{\text{FV}} \approx |X|/2$ . Only the candidate tags in  $X$  need to be encoded in the next filtering vector, using a different hash function  $h_2$ . Hence, in the second round, the size of the filtering vector from the reader to tags is reduced by half to  $|X|/(2 \ln 2)$ , and similarly the size of the filtering vector from tags to the reader is also reduced by half to  $|Y|/(4 \ln 2)$ . Repeating the above process, it is easy to see that in the  $i$ th round, the size of the filtering vector from the reader to tags is  $|X|/(2^{i-1} \ln 2)$ , and the size of the filtering vector from tags to the reader is  $|Y|/(2^i \ln 2)$ . After  $K$  rounds, the total size of all filtering vectors from the reader to tags is

$$\frac{1}{\ln 2} \sum_{i=1}^K \frac{|X|}{2^{i-1}} < \frac{2|X|}{\ln 2} \quad (14)$$

where  $\frac{2|X|}{\ln 2}$  is an upper bound, regardless of the number  $K$  of rounds (i.e., regardless of the requirement on the false-positive probability). It compares favorably to CATS, whose filter size,  $-\frac{\ln P_{\text{B}}}{(\ln 2)^2} |X|$ , grows inversely in  $P_{\text{B}}$ , and reaches  $14.4 \times |X|$  bits when  $P_{\text{B}} = 0.001$  in our earlier example.

Similarly, the total size of all filtering vectors from tags to the reader is

$$\frac{1}{\ln 2} \sum_{i=1}^K \frac{|Y|}{2^i} < \frac{|Y|}{\ln 2} \quad (15)$$

and  $P_{\text{FP}} = (P_{\text{FV}})^K \approx (\frac{1}{2})^K$ . We can make  $P_{\text{FP}}$  as small as we like by increasing  $n$ , while the total transmission overhead never exceeds  $\frac{1}{\ln 2} (2|X| + |Y|)$  bits. The strength of filtering vectors in bidirectional filtration lies in their ability to reduce the candidate sets during each round, thereby diminishing the sizes of filtering vectors in subsequent rounds and thus saving time. Its power of reducing subsequent filtering vectors is related to  $|X - W|$  and  $|Y - W|$ . The more the numbers of tags outside of  $W$ , the more they will be filtered in each round, and the greater the effect of reduction.

### E. Generalized Approach

Unlike the CATS protocol, our iterative approach divides the bidirectional filtration in tag search process into multiple rounds. Before the  $i$ th round, the set of candidate tags in  $X$  is denoted as  $X_i (\subseteq X)$ , which is also called the search result after the  $(i - 1)$ th round. The final search result is the set of remaining candidate tags in  $X$  after all rounds are completed. Before the  $i$ th round, the set of candidate tags in  $Y$  is denoted as  $Y_i (\subseteq Y)$ . Initially,  $X_1 = X$  and  $Y_1 = Y$ . We define  $U_i = X_i - W$  and  $V_i = Y_i - W$ , which are the tags to be filtered out. Because  $W$  is always a subset of both  $X_i$  and  $Y_i$ , we have

$$\begin{aligned} |U_i| &= |X_i| - |W| \\ |V_i| &= |Y_i| - |W|. \end{aligned} \quad (16)$$

Instead of exchanging a single filtering vector at a time, we generalize our iterative approach by allowing multiple filtering vectors to be sent consecutively. Each round consists of two phases. In phase one of the  $i$ th round, the RFID reader broadcasts a number  $m_i$  of filtering vectors, which shrink the set of remaining candidate tags in  $Y$  from  $Y_i$  to  $Y_{i+1}$ . In phase two of the  $i$ th round, one filtering vector is sent from the remaining candidate tags in  $Y_{i+1}$  back to the reader, which uses the received

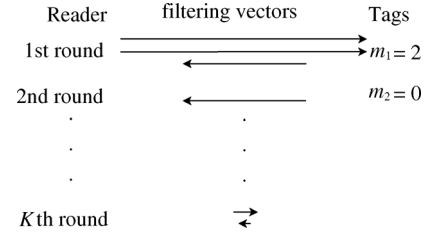


Fig. 3. Generalized approach. Each round has two phases. In phase one, the reader transmits zero, one, or multiple filtering vectors. In phase two, the tags send exactly one filtering vector to the reader. In the example shown by the figure,  $m_1 = 2$  and  $m_2 = 0$ , which means there are two filtering vectors sent by the reader in the first round, and no filtering vector from the reader during the second round.

filtering vector to shrink its set of remaining candidates from  $X_i$  to  $X_{i+1}$ , setting the stage for the next round. This process continues until the false-positive ratio meets the requirement of  $P_{\text{REQ}}$ .

The values of  $m_i$  will be determined in Section IV-F. If  $m_i > 0$ , multiple filtering vectors will be sent consecutively from the reader to tags in one round. If  $m_i = 0$ , no filtering vector is sent from the reader in this round. When this happens, it essentially allows multiple filtering vectors to be sent consecutively from tags to the reader (across multiple rounds). An illustration is given in Fig. 3.

### F. Values of $m_i$

Let  $K$  be the total number of rounds. After all  $K$  rounds, we use  $X_{K+1}$  as our search result. There are in total  $K$  filtering vectors sent from tags to the reader. We know from Section IV-C that each filtering vector can filter out half of non-members (in our case, tags in  $X - W$ ). To meet the false-positive ratio requirement  $P_{\text{REQ}}$ , the following constraint should hold:

$$(P_{\text{FV}})^K \approx \left(\frac{1}{2}\right)^K \leq P_{\text{REQ}}. \quad (17)$$

Hence, the value of  $K$  is set to  $\lceil -\frac{\ln P_{\text{REQ}}}{\ln 2} \rceil$ . (We will discuss how to guarantee meeting the requirement  $P_{\text{REQ}}$  in Section IV-A.)

Next, we discuss how to set the values of  $m_i$ ,  $1 \leq i \leq K$ , in order to minimize the execution time of each round. We use  $FV(\cdot)$  to denote the filtering vector of a set. In phase one of the  $i$ th round, the reader builds  $m_i$  filtering vectors, denoted as  $FV_{i1}(X_i), FV_{i2}(X_i), \dots, FV_{im_i}(X_i)$ , which are consecutively broadcast to the tags. From (12), we know the size of each filtering vector is  $|X_i|/\ln 2$ . After the filtration based on these vectors, the number of remaining candidate tags in  $Y_{i+1}$  is on average

$$\begin{aligned} |Y_{i+1}| &\approx |V_i| \times (P_{\text{FV}})^{m_i} + |W| \\ &\approx |V_i| \times (1/2)^{m_i} + |W| \\ &= |V_i|/2^{m_i} + |W|. \end{aligned} \quad (18)$$

In phase two of the  $i$ th round, the tags in  $Y_{i+1}$  use a time frame of  $\frac{1}{\ln 2} \times |Y_{i+1}|$  slots to report their presence. After receiving the responses, the reader builds a filtering vector, denoted as  $FV_i(Y_{i+1})$ . After the filtration based on  $FV_i(Y_{i+1})$ , the size of the search result  $X_{i+1}$  is on average

$$\begin{aligned} |X_{i+1}| &\approx |U_i| \times P_{\text{FV}} + |W| \\ &\approx |U_i|/2 + |W| \\ &= (|X_i| + |W|)/2. \end{aligned} \quad (19)$$

We denote the transmission time of the  $i$ th round by  $f(m_i)$ . To make a fair comparison to CATS, we utilize the parameter setting that conforms with [11]. Therefore,  $f(m_i) = \frac{1}{\ln 2} \times m_i \times |X_i| \times t_s + \frac{1}{\ln 2} \times |Y_{i+1}| \times t_s$ , which is set to be

$$f(m_i) = \frac{t_s}{\ln 2} (m_i |X_i| + |V_i|/2^{m_i} + |W|). \quad (20)$$

To find the value of  $m_i$  that minimizes  $f(m_i)$ , we take the first-order derivative and set the right side to zero

$$\frac{df(m_i)}{dm_i} = \frac{t_s}{\ln 2} (|X_i| - \ln 2 |V_i|/2^{m_i}) = 0. \quad (21)$$

Hence, the value of  $f(m_i)$  is minimized when

$$m_i = \frac{\ln(\ln 2 |V_i|/|X_i|)}{\ln 2}. \quad (22)$$

Because  $m_i$  cannot be a negative number, we reset  $m_i = 0$  if  $\frac{\ln(\ln 2 |V_i|/|X_i|)}{\ln 2} < 0$ . Furthermore,  $m_i$  must be an integer. If  $\frac{\ln(\ln 2 |V_i|/|X_i|)}{\ln 2}$  is not an integer, we round  $m_i$  either to the ceiling or to the floor, depending on which one results in a smaller value of  $f(m_i)$ .

For now, we assume that we know  $|W|$  and  $|Y|$  in our computation of  $m_i$ . Later, we will show how to estimate these values on the fly in the execution of each round of our protocol. Initially,  $|X_1|$  ( $= |X|$ ) is known.  $|V_1|$  can be calculated from (16). Hence, the value of  $m_1$  can be computed from (22). After that, we can estimate  $|Y_2|$ ,  $|X_2|$ , and  $|V_2|$  based on (18), (19), and (16), respectively. From  $|X_2|$  and  $|V_2|$ , we can calculate the value  $m_2$ . Following the same procedure, we can iteratively compute all values of  $m_i$  for  $1 \leq i \leq K$ .

We find it often happens that the  $m_i$  sequence has several consecutive zeros at the end, that is,  $\exists p < K$ ,  $m_i = 0$  for  $i \in [p, K]$ . In this case, we may be able to further optimize the value of  $m_p$  with a slight adjustment. We first explain the reason for  $m_p = 0$ : It costs some time for the reader to broadcast a filtering vector in phase one of the  $p$ th round. It is true that this filtering vector can reduce set  $Y_p$ , thereby reducing the frame size of phase two in the  $p$ th round. However, if the time cost of sending the filtering vector cannot be compensated by the time reduction of phase two, it will be better off to remove this filtering vector by setting  $m_p = 0$ . (This situation typically happens near the end of the  $m_i$  sequence because the number of unwanted tags in the remaining candidate set  $Y_p$  is already very small.) However, if all values of  $m_i$  in the subsequent rounds (after  $m_p$ ) are zeros, increasing  $m_p$  to a nonzero value  $m'_p$  may help reduce the transmission time of phase two of all subsequent rounds, and the total time reduction may compensate more than the time cost of sending those  $m'_p$  filtering vectors.

Consider the transmission time of these  $(K - p + 1)$  rounds as a whole, denoted by  $G(m'_p, p)$ . It is easy to derive

$$G(m'_p, p) = \left( \frac{m'_p}{\ln 2} |X_p| + \frac{K - p + 1}{\ln 2} \left( \frac{|V_p|}{2^{m'_p}} + |W| \right) \right) t_s. \quad (23)$$

To minimize  $G(m'_p, p)$ , we have

$$m'_p = \begin{cases} 0, & \text{if } \gamma < 0 \\ \gamma, & \text{if } \gamma \geq 0 \end{cases} \quad (24)$$

where  $\gamma = \frac{\ln(\ln 2 (K - p + 1) |V_p|/|X_p|)}{\ln 2}$ . As a result,  $m_p$  is updated to  $m'_p$ , while other  $m_i$ ,  $i \neq p$ , remains unchanged.

TABLE II  
INITIAL VALUES OF  $m_i$

| $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 3     | 1     | 0     | 1     | 0     | 1     | 0     | 0     | 0     | 0        |

TABLE III  
OPTIMIZED VALUES OF  $m_i$

| $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 3     | 1     | 0     | 1     | 0     | 1     | 2     | 0     | 0     | 0        |

Here, we give an example to illustrate how to calculate the values of  $m_i$ . Suppose  $|X| = 5000$ ,  $|Y| = 50\,000$ ,  $|W| = 500$ , and  $P_{\text{REQ}} = 0.001$ , so  $K = \lceil \frac{-\ln 0.001}{\ln 2} \rceil = 10$ . Using (22), we can calculate the values from  $m_1$  to  $m_{10}$ . The result is listed in Table II. There is a sequence of zeros from  $m_7$  to  $m_{10}$ . Thus, we can make an improvement using (24), and the optimized result is shown in Table III.

### G. Iterative Tag Search Protocol

Having calculated the values of  $m_i$ , we can present our iterative tag search protocol (ITSP) based on the generalized approach in Section IV-E. The protocol consists of  $K$  iterative rounds. Each round consists of two phases. Consider the  $i$ th round, where  $1 \leq i \leq K$ .

1) *Phase One*: The RFID reader constructs  $m_i$  filtering vectors for  $X_i$  using  $m_i$  hash functions. According to (12), we set the size  $L_{X_i}$  of each filtering vector as

$$L_{X_i} = \frac{1}{\ln 2} \times |X_i|. \quad (25)$$

The RFID reader then broadcasts those filtering vectors one by one. Once receiving a filtering vector, each tag in  $Y_i$  maps its ID to a bit in the filtering vector using the same hash function that the reader uses to construct the filter. The tag checks whether this bit is "1." If so, it remains a candidate tag; otherwise, it is excluded as a non-candidate tag and drops out of the search process immediately. The set of remaining candidate tags is  $Y_{i+1}$ .

If the filtering vectors are too long, the reader divides each vector into blocks of a certain length (e.g., 96 bits) and transmits one block after another. Knowing which bit it is mapped to, each tag only needs to record one block that contains its bit.

From (13), we know that the false-positive probability after using  $m_i$  filtering vectors is  $(P_{\text{FV}})^{m_i} \approx (1/2)^{m_i}$ . Therefore,  $|Y_{i+1}| \approx |V_i| \times (P_{\text{FV}})^{m_i} + |W| \approx |V_i|/2^{m_i} + |W|$ .

2) *Phase Two*: The reader broadcasts the frame size  $L_{Y_{i+1}}$  of phase two to the tags, where

$$L_{Y_{i+1}} = \frac{1}{\ln 2} (|V_i|/2^{m_i} + |W|). \quad (26)$$

After receiving  $L_{Y_{i+1}}$ , each tag in  $Y_{i+1}$  randomly maps its ID to a slot in the time frame using a hash function and transmits a one-bit short response to the reader in that slot. Based on the observed state (busy or empty) of the slots in the time frame, the reader builds a filtering vector, which is used to filter non-candidates from  $X_i$ .

The overall transmission time of all  $K$  rounds in the ITSP is

$$T_{\text{ITSP}} = \sum_{i=1}^K (m_i \times L_{X_i} + L_{Y_{i+1}}) \times t_s. \quad (27)$$

## H. Cardinality Estimation

Recall from Section IV-F that we must know the values of  $|X_i|$ ,  $|W|$ , and  $|V_i|$  to determine  $m_i$ ,  $L_{X_i}$ , and  $L_{Y_{i+1}}$ . It is trivial to find the value of  $|X_i|$  by counting the number of tags in the search result of the  $(i-1)$ th round. Meanwhile, we know  $|V_i| \approx |V_{i-1}|/2^{m_i-1}$ , and  $|V_1| = |Y_1| - |W|$ . Therefore, we only need to estimate  $|W|$  and  $|Y_1|$ .

Besides serving as a filter, a filtering vector can also be used for cardinality estimation, a feature that is not exploited in [11]. Since no filtering vector is available at the very beginning, the first round of the ITSP should be treated separately: We may use the efficient cardinality estimation protocol ART proposed in [29] to estimate  $|Y|$  (i.e.,  $|Y_1|$ ) if its value is not known at first. As for  $|W|$ , it is initially assumed to be  $\min\{|X|, |Y|\}$ .

Next, we can take advantage of the filtering vector received by the reader in phase two of the  $i$ th ( $i \geq 1$ ) round to estimate  $|W|$  without any extra transmission expenditure. The estimation process is as follows: First, counting the actual number of “1” bits in the filtering vector, denoted as  $N_1^*$ , we know the *actual* false-positive probability of using this filtering vector, denoted by  $P_i^*$ , is

$$P_i^* = N_1^*/L_{Y_{i+1}} \quad (28)$$

because an arbitrary unwanted tag has a chance of  $N_1^*$  out of  $L_{Y_{i+1}}$  to be mapped to a “1” bit, where  $L_{Y_{i+1}}$  is the size of the vector. Meanwhile, we can record the number of tags in the search results before and after the  $i$ th round, i.e.,  $|X_i|$  and  $|X_{i+1}|$ , respectively. We have  $|X_i| = |U_i| + |W|$ ,  $|X_{i+1}| = |U_{i+1}| + |W|$ , and  $|U_{i+1}| \approx |U_i| \times P_i^*$ . Therefore

$$|W| \approx \frac{|X_{i+1}| - |X_i| \times P_i^*}{1 - P_i^*}. \quad (29)$$

For the purpose of accuracy, we may estimate  $|W|$  after every round, and obtain the average value.

### I. Additional Filtering Vectors

Estimation may have error. Using the values of  $m_i$  and  $L_{Y_i}$  computed from estimated  $|W|$  and  $|Y_i|$ , a direct consequence is that the actual false-positive ratio, denoted as  $P_T$ , can be greater than the requirement  $P_{REQ}$ . Fortunately, from (28), the reader is able to compute the actual false-positive ratio  $P_i^*$ ,  $1 \leq i \leq k$ , of each filtering vector received in phase two of the ITSP. Thus, we have

$$P_T = \prod_{i=1}^K P_i^*. \quad (30)$$

If  $P_T > P_{REQ}$ , our protocol will automatically add additional filtering vectors to further filter  $X_{K+1}$  until  $P_T \leq P_{REQ}$  (as described in Section IV-D).

### J. Hardware Requirement

The proposed protocol cannot be supported by off-the-shelf tags that conform to the EPC Class-1 Gen-2 standard [12], whose limited hardware capability constrains the functions that can be supported. By our design, most of the ITSP protocol’s complexity is on the reader side, but tags also need to provide certain hardware support. Besides the mandatory commands of C1G2 (e.g., Query, Select, Read), in order for a tag to execute the ITSP protocol, we need a new command defined in the set of optional commands, asking each awake tag to listen to the reader’s filtering vector, hash its ID to a certain slot of the vector for its bit value, keep silent and go sleep if the value is

zero, and respond in a hashed slot (by making a transmission to make the channel busy) if the value is one. Note that the tag does not need to store the entire filtering vector, but instead only needs to count to the slot it is hashed to, and retrieve the value (0/1) carried in that slot.

Hardware-efficient hash functions [30]–[32] can be found in the literature. A hash function may also be derived from the pseudo-random number generator required by the C1G2 standard. To keep the complexity of a tag’s circuit low, we only use one uniform hash function  $h(\cdot)$ , and use it to simulate multiple independent hash functions: In phase one of the  $i$ th round, we use  $h(\cdot)$  and  $m_i$  unique hash seeds  $\{s_1, s_2, \dots, s_{m_i}\}$  to achieve  $m_i$  independent hash outputs. Thus, a tag  $id$  is mapped to bit locations  $(h(id \oplus s_1) \bmod L_{X_i})$ ,  $(h(id \oplus s_2) \bmod L_{X_i})$ ,  $\dots$ ,  $(h(id \oplus s_{m_i}) \bmod L_{X_i})$  in the  $m_i$  filtering vectors, respectively. Each hash seed, together with its corresponding filtering vector, will be broadcast to the tags. In phase two of the  $i$ th round, the reader generates a new hash seed  $s'$  and sends it to the tags. Each candidate tag in  $Y_{i+1}$  maps its  $id$  to the slot of index  $(h(id \oplus s') \bmod L_{Y_{i+1}})$ , and then transmits a one-bit short response to the reader in that slot.

## V. ITSP OVER NOISY CHANNEL

So far, the ITSP assumes that the wireless channel between the RFID reader and tags is reliable. Note that the CATS protocol does not consider channel error, either. However, it is common in practice that the wireless channel is far from perfect due to many different reasons, among which interference noise from nearby equipment, such as motors, conveyors, robots, wireless LANs, and cordless phones, is a crucial one. Therefore, our next goal is to enhance ITSP making it robust against noise interference.

### A. ITSP With Noise on Forward Link

The reader transmits at a power level much higher than the tags (which after all backscatter the reader’s signals in the case of passive tags). It has been shown that the reader may transmit more than one million times higher than tag backscatter [33]. Hence, the forward link (reader to tag) communication is more resilient against channel noise than the reverse link (tag to reader). To provide additional assurance against noise for forward link, we may use CRC code for error detection. The C1G2 standard requires the tags to support the computation of CRC-16 (16-bit CRC)[12], which therefore can also be adopted by future tags modified for ITSP. Each filtering vector built by the reader can be regarded as a combination of many small segments with fixed size of  $l_S$  bits (e.g.,  $l_S = 80$ ). For each segment, the reader computes its 16-bit CRC and appends it to end of that segment. Those segments are then concatenated and transmitted to tags. When a tag receives a filtering vector, it first finds the segment it hashes to and computes the CRC of that segment. If the calculated CRC matches the attached one, it will determine its candidacy by checking the bit in the segment to which it maps. For mismatching CRC, the tag knows that the segment has been corrupted, and it will remain as a candidate tag regardless of the value of the bit to which it maps.

Suppose we let  $l_S = 80$ , then

$$L_{X_i} = \frac{1}{\ln 2} \times |X_i| \times (l_S + 16) = \frac{1.2|X|}{\ln 2}. \quad (31)$$

We assume the probability that the noise corrupts each segment is  $P_S$  ( $P_S$  is expected to be very small as explained above).

A corrupted segment can be thought as consisting of all “1”s. Hence, the false-positive probability for a filtering vector sent by reader, denoted by  $P_{\text{RT}}$ , is roughly

$$P_{\text{RT}} \approx \frac{\frac{L_{X_i}}{96} \times P_S \times l_S + \frac{L_{X_i}}{96} \times (1 - P_S) \times l_S \times P_{\text{FV}}}{\frac{L_{X_i}}{96} \times l_S} = \frac{1 + P_S}{2}. \quad (32)$$

We can also get

$$|Y_{i+1}| \approx |V_i| \times (P_{\text{RT}})^{m_i} + |W| \quad (33)$$

and now (20) can be rewritten as

$$f(m_i) = \frac{t_s}{\ln 2} \left( 1.2m_i |X_i| + \left( \frac{1 + P_{\text{RT}}}{2} \right)^{m_i} |V_i| + |W| \right). \quad (34)$$

Therefore,  $f(m_i)$  is optimized when

$$m_i = \frac{\ln[(\ln 2 - \ln(1 + P_{\text{RT}}))|V_i|/1.2|X_i|]}{\ln 2 - \ln(1 + P_{\text{RT}})}. \quad (35)$$

### B. ITSP With Noise on Reverse Link

Now let us study the noise on the reverse link and its effect on the ITSP. Since the backscatter from a tag is much weaker than the signal transmitted by the reader, the reverse link is more likely to be impacted by noise.

First, channel noise may corrupt a would-be empty slot into a busy slot. The original empty slot is supposed to be translated into a “0” bit in the filtering vector by the reader; if a candidate tag is mapped to that bit, it is ruled out immediately. However, if that slot is corrupted and becomes a busy slot, the corresponding bit turns into “1”; a tag mapped to that bit will remain a candidate tag, thereby increasing the false-positive probability of the filtering vector.

Second, noise may also occur during a busy slot. Although the noise and the transmissions from tags may partially cancel each other in a slot if they happen to reach the reader in opposite phase, it is extremely unlikely that they will exactly eliminate each other. As long as the reader can still detect some energy, regardless of its source (it may even come from the noise), that slot will be correctly determined as a busy slot, and the corresponding bit in the filtering vector is set to “1” just as it is supposed to be. However, if we take the propagation path loss, including reflection loss, attenuation loss, and spreading loss [34], into account, there is still a chance that a busy slot may not be detected by the reader. This may happen in a time varying channel where the reader may fail in receiving a tag’s signal during a deeply faded slot when the tag transmits. We stress that this is not a problem unique to ITSP, but all protocols that require communications from tags to readers will suffer from this problem if it happens that the reader cannot hear the tags. ITSP is not robust against this type of error. However, there exist ways to alleviate this problem—for instance, each filtering vector from tags to the reader is transmitted twice. As long as a slot is busy in one of two transmissions, the slot is considered to be busy.

Next, we will investigate the reverse link with noise interference for ITSP under two error models.

1) *ITSP Under Random Error Model (ITSP-rem)*: The random error model is characterized by a parameter called *error rate*  $P_{\text{ERR}}$ , which means every slot independently has a probability  $P_{\text{ERR}}$  to be corrupted by the noise. Influenced by the channel noise, the reader can detect more busy slots as some empty slots turn into busy ones, which raises the false-positive

probability of phase-two filtering vectors. Suppose the frame size of phase two in a certain round is  $l$ , and the original number of busy slots is about  $l \times P_{\text{FV}} \approx l/2$ . At the reader’s side, however, the number of busy slots averagely increases to  $l/2 + l/2 \times P_{\text{ERR}} = \frac{(1+P_{\text{ERR}}) \times l}{2}$ . After encoding the slot status into a filtering vector, the false-positive probability of that filtering vector is

$$P'_{\text{FV}} \approx \frac{\frac{(1+P_{\text{ERR}}) \times l}{2}}{l} = \frac{1 + P_{\text{ERR}}}{2}. \quad (36)$$

To satisfy the false-positive ratio requirement,  $(P'_{\text{FV}})^K \leq P_{\text{REQ}}$  should hold. Therefore, the search process of ITSP-rem contains at least

$$K = \left\lceil \frac{\ln P_{\text{REQ}}}{\ln[(1 + P_{\text{ERR}})/2]} \right\rceil \quad (37)$$

rounds. Also, we can derive

$$|X_{i+1}| \approx |U_i| \times P'_{\text{FV}} + |W| \approx |U_i|(1 + P_{\text{ERR}})/2 + |W|. \quad (38)$$

With  $K$ ,  $|X_i|$ ,  $|Y_i|$ , and  $m_i$ ,  $1 \leq i \leq K$ , the search time of ITSP-rem can be calculated using (31), (26), and (27).

2) *ITSP Under Burst Error Model (ITSP-bem)*: In telecommunication, a burst error is defined as a consecutive sequence of received symbols, where the first and last symbols are in error, and there exists no continuous subsequence of  $m$  ( $m$  is a specified parameter called the *guard band* of the error burst) correctly received symbols within the error burst [35]. A burst error model describes the number of bursts during an interval and the number of incorrect symbols in each burst error, which differs greatly from the random error model.

According to the burst error model presented in [36], both the number of bursts in an interval and the number of errors in each burst have Poisson distributions. Assuming the expected number of bursts in an  $l$ -bit interval is  $\eta$ , the probability distribution function for the number of bursts can be expressed as

$$h(x) = \sum_{i=0}^{\infty} \frac{\eta^i}{i!} e^{-\eta} \delta_{xi} \quad (39)$$

where  $\delta_{xi}$  is the Kronecker delta function [37]. Meanwhile, if the mean value of errors due to a burst in the  $l$  bits is  $\tau$ , then the probability distribution function of the number of error is given by

$$g(y) = \sum_{j=0}^{\infty} \frac{\tau^j}{j!} e^{-\tau} \delta_{yj}. \quad (40)$$

Therefore, the probability of having  $w$  errors in an interval of  $l$  bits is

$$P_l(w) = e^{-\eta} \frac{\tau^w}{w!} \sum_{i=0}^{\infty} \frac{i^w}{i!} \eta^i e^{-i\tau}. \quad (41)$$

In other words, for a frame with  $l$  slots, the probability that  $w$  slots will be corrupted by the burst noise is  $P_l(w)$ .

Now we evaluate the ITSP under the burst error model, denoted as ITSP-bem. Given a filtering vector with size of  $l$  bits, recall from (41) that the probability of having  $w$  errors in this  $l$ -bit vector is  $P_l(w)$ . In this case, each original “0” bit has a probability  $\frac{w}{l}$  to be corrupted by the errors and becomes a “1” bit. Consequently, the false-positive probability of the filtering vector is expected to be

$$P'_{\text{FV}} \approx \frac{1}{2} + \frac{1}{2} \sum_{w=0}^l P_l(w) \times \frac{w}{l}. \quad (42)$$



TABLE IV

PERFORMANCE COMPARISON OF TAG SEARCH PROTOCOLS, WHERE DFSA REPRESENTS A TAG IDENTIFICATION PROTOCOL WITH DFSA, AND CR REPRESENTS A TAG IDENTIFICATION PROTOCOL WITH COLLISION RECOVERY TECHNIQUES.  $|Y| = 50\,000$ ,  $P_{REQ} = 0.001$

| $ X $   | ITSP           |                |                |                |                | CATS       | Polling    | DFSA       | CR        |
|---------|----------------|----------------|----------------|----------------|----------------|------------|------------|------------|-----------|
|         | $R_{INTS}=0.1$ | $R_{INTS}=0.3$ | $R_{INTS}=0.5$ | $R_{INTS}=0.7$ | $R_{INTS}=0.9$ |            |            |            |           |
| 5,000   | 61,463         | 96,989         | 105,828        | 108,346        | 124,553        | 126,370    | 485,000    | 18,620,231 | 1,427,083 |
| 10,000  | 108,017        | 145,553        | 206,709        | 199,586        | 231,236        | 238,313    | 970,000    | 18,620,231 | 1,427,083 |
| 20,000  | 185,204        | 255,898        | 335,426        | 397,462        | 403,954        | 447,772    | 1,940,000  | 18,620,231 | 1,427,083 |
| 40,000  | 304,767        | 467,433        | 512,156        | 598,718        | 678,066        | 837,837    | 3,880,000  | 18,620,231 | 1,427,083 |
| 80,000  | 414,686        | 590,150        | 656,426        | 721,347        | 721,347        | 1,560,259  | 7,760,000  | 18,620,231 | 1,427,083 |
| 160,000 | 472,677        | 630,669        | 721,347        | 721,347        | 721,347        | 2,889,689  | 15,520,000 | 18,620,231 | 1,427,083 |
| 320,000 | 529,835        | 668,794        | 721,347        | 721,347        | 721,347        | 5,317,715  | 31,040,000 | 18,620,231 | 1,427,083 |
| 640,000 | 573,270        | 696,015        | 721,347        | 721,347        | 721,347        | 10,533,732 | 62,080,000 | 18,620,231 | 1,427,083 |

TABLE V

PERFORMANCE COMPARISON OF TAG SEARCH PROTOCOLS, WHERE DFSA REPRESENTS A TAG IDENTIFICATION PROTOCOL WITH DFSA, AND CR REPRESENTS A TAG IDENTIFICATION PROTOCOL WITH COLLISION RECOVERY TECHNIQUES.  $|X| = 10\,000$ ,  $P_{REQ} = 0.001$

| $ Y $  | ITSP           |                |                |                |                | CATS    | Polling | DFSA       | CR        |
|--------|----------------|----------------|----------------|----------------|----------------|---------|---------|------------|-----------|
|        | $R_{INTS}=0.1$ | $R_{INTS}=0.3$ | $R_{INTS}=0.5$ | $R_{INTS}=0.7$ | $R_{INTS}=0.9$ |         |         |            |           |
| 1,250  | 13,047         | 17,364         | 18,033         | 18,033         | 18,033         | 164,589 | 970,000 | 465,506    | 35,677    |
| 2,500  | 24,289         | 33,337         | 36,067         | 36,067         | 36,067         | 175,960 | 970,000 | 931,012    | 71,354    |
| 5,000  | 42,835         | 62,862         | 68,528         | 72,134         | 72,134         | 190,387 | 970,000 | 1,862,023  | 142,708   |
| 10,000 | 73,909         | 109,281        | 119,022        | 137,056        | 144,269        | 204,814 | 970,000 | 3,724,046  | 285,417   |
| 20,000 | 95,833         | 132,546        | 169,065        | 167,713        | 192,960        | 219,241 | 970,000 | 7,448,092  | 570,833   |
| 40,000 | 111,904        | 152,606        | 174,926        | 228,215        | 232,904        | 233,668 | 970,000 | 14,896,184 | 1,141,667 |

After obtaining the value of  $P'_{FV}$ , the ITSP-bem can use (37) and (38) to determine the values of other necessary parameters.

## VI. PERFORMANCE EVALUATION

### A. Performance Metric

We compare our protocol ITSP to CATS [11], the polling protocol (Section III-B), the optimal DFSA, and a tag identification protocol with collision recovery [27], denoted as CR, which identifies 4.8 tags per slot on average, about 13 times the speed of the optimal DFSA. For ITSP and CATS, their Bloom filters (or filtering vectors) constitute most of the overall transmission overhead, while other transmission cost, such as transmission of hash seeds, is comparatively negligible. Both protocols need to estimate the number of tags in the system,  $|Y|$ , as a pre-protocol step. According to the results presented in [11], the time for estimating  $|Y|$  takes up less than 2% of the total execution time of CATS. Hence, we do not count the estimation time of  $|Y|$  in the simulation results because it is relatively small and does not affect fair comparison as both protocols need it. Consequently, the key metric concerning the time efficiency is the total size of Bloom filters or filtering vectors, and then (8) can be used for calculating the search time required by CATS, while (27) for ITSP.

After the search process is completed, we will calculate the false-positive ratio  $P_{FP}$  using  $P_{FP} = \frac{|W^* - W|}{|X - W|}$ , where  $W^*$  is the set of tags in the search result and  $W$  is the actual set of wanted tags in the coverage area.  $P_{FP}$  will be compared to  $P_{REQ}$  to see whether the search result meets the false-positive ratio requirement.

### B. Performance Comparison

We evaluate the performance of our protocol and compare it to the CATS protocol. In the first set of simulations, we set  $P_{REQ} = 0.001$ , fix  $|Y| = 50\,000$ , vary  $|X|$  from 5000 to 64000, and let  $R_{INTS} = 0.1, 0.3, 0.5, 0.7, 0.9$ . In the second

set of simulations, we set  $P_{REQ} = 0.001$ , fix  $|X| = 10\,000$ , vary  $|Y|$  from 1250 to 40000 to investigate the scalability of ITSP with tag population from a large range, and let  $R_{INTS} = 0.1, 0.3, 0.5, 0.7, 0.9$ . For simplicity, we assume  $t_{id} = 96t_s$ , and  $t_l = 137t_s$ , in which a 9-bit *QueryAdjust* or a 4-bit *QueryRep* command, a 96-bit ID, and two 16-bit random numbers can be transmitted. Tables IV and V show the number of  $t_s$  slots needed by the protocols under different parameter settings. Each data point in these tables or other figures/tables in the rest of the section is the average of 500 independent simulation runs with  $\pm 5\%$  or less error at 95% confidence level.

From the tables, we observe that when  $R_{INTS}$  is small (which means  $|W|$  is small), the ITSP performs much better than the CATS protocol. For example, in Table IV, when  $R_{INTS} = 0.1$ , the ITSP reduces the search time of the CATS protocol by as much as 90.0%. As we increase  $R_{INTS}$  (which implies larger  $|W|$ ), the gap between the performance of the ITSP and the performance of the CATS gradually shrinks. In particular, the CATS performs poorly when  $|X| \geq |Y|$ . However, the ITSP can work efficiently in all cases. In addition, the ITSP is also much more efficient than the polling protocol and any tag identification protocol with/without CR techniques. Even in the worst case, the ITSP only takes about half of the execution time of a tag identification protocol with CR techniques. (Note that the identification process actually takes much more time since the throughput 4.8 tags per slot may not be achievable in practice and the duration of each slot is longer.) In practice, the wanted tags may be spatially distributed in many different RFID systems (e.g., warehouses in the example we use in Section I), and thus  $R_{INTS}$  can be small. The ITSP is a much better protocol for solving the tag search problem in these practical scenarios.

Another performance issue we want to investigate is the relationship between the search time and  $P_{REQ}$ . The polling protocol, DFSA, and CR do not have false positive. Our focus will be on ITSP and CATS. We set  $|X| = 5000, 20\,000, \text{ or } 80\,000$ ,  $|Y| = 50\,000$ , vary  $R_{INTS}$  from 0.1 to 0.9, and vary  $P_{REQ}$  from

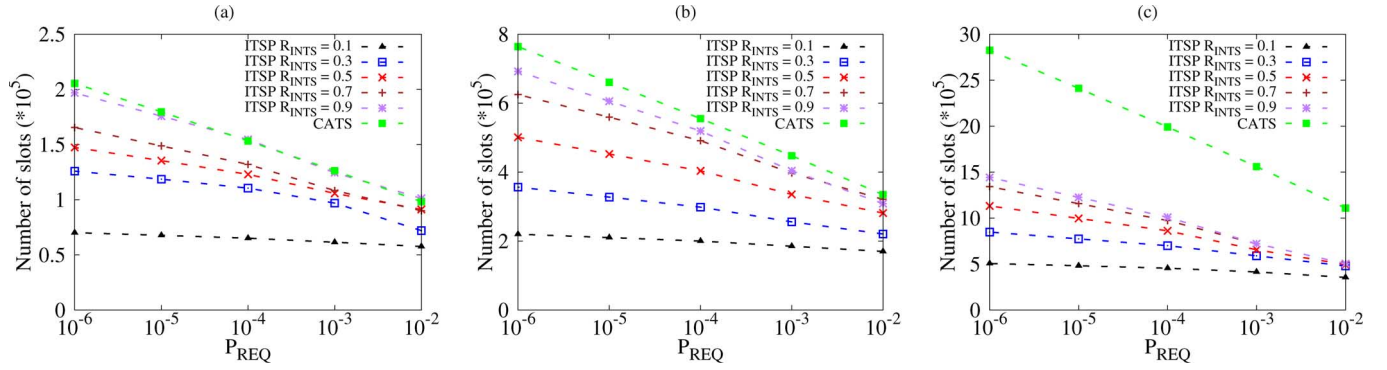


Fig. 4. Relationship between search time and  $P_{REQ}$ . Parameter setting:  $|Y| = 50\,000$ ; (a)  $|X| = 5000$ ; (b)  $|X| = 20\,000$ ; (c)  $|X| = 80\,000$ .

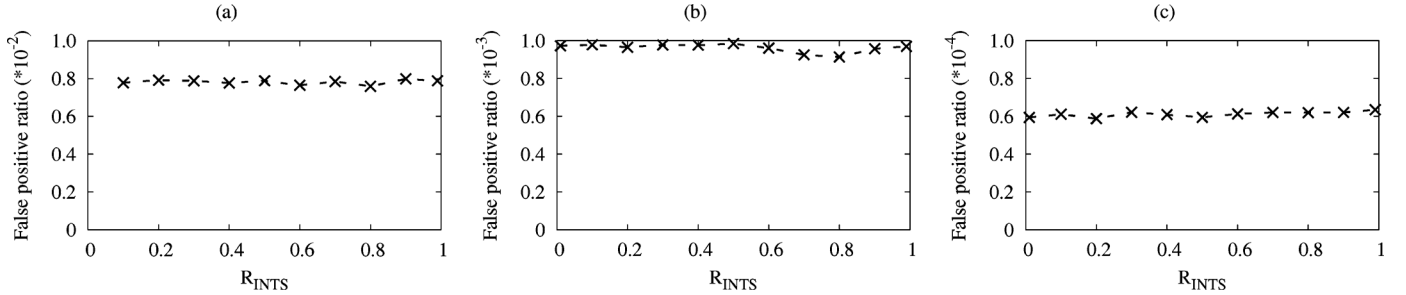


Fig. 5. False-positive ratio after running the ITSP. (a)  $|X| = 5000$ ,  $|Y| = 50\,000$ ,  $P_{REQ} = 10^{-2}$ . (b)  $|X| = 20\,000$ ,  $|Y| = 50\,000$ ,  $P_{REQ} = 10^{-3}$ . (c)  $|X| = 80\,000$ ,  $|Y| = 50\,000$ ,  $P_{REQ} = 10^{-4}$ .

$10^{-6}$  to  $10^{-2}$ . Fig. 4 compares the search times required by the CATS and the ITSP under different false-positive ratio requirements. Generally speaking, the gap between the search time required by the ITSP and the search time by the CATS keeps getting larger with the decrease of  $P_{REQ}$ , particularly when  $R_{INTS}$  is small. For example, in Fig. 4(c), when  $P_{REQ} = 10^{-2}$  and  $R_{INTS} = 0.1$ , the search time by the ITSP is about one third of the time by the CATS; when we reduce  $P_{REQ}$  to  $10^{-6}$ , the time by the ITSP becomes about one fifth of the time by the CATS. The reason is as follows: When  $R_{INTS}$  is small,  $|W|$  is small, and most tags in  $X$  and  $Y$  are non-candidates. After several ITSP rounds, as many non-candidates are filtered out iteratively, the size of filtering vectors decreases exponentially, and therefore subsequent ITSP rounds do not cause much extra time cost. This merit makes the ITSP particularly applicable in cases where the false-positive ratio requirement is very strict, requiring many ITSP rounds. On the contrary, the CATS protocol does not have this capability of exploiting low  $R_{INTS}$  values.

### C. False-Positive Ratio

Next, we examine whether the search results after execution of the ITSP will indeed meet the requirement of  $P_{REQ}$ . In this simulation, we set the false-positive ratio requirement based on the following formula:

$$P_{REQ} \leq \frac{|W|}{\lambda(|X| - |W|)} \quad (43)$$

where  $\lambda$  is a constant. We use an example to give the rationale: Consider an RFID system with  $|X| = 20\,000$ . If  $|W| = 10\,000$ ,  $P_{REQ} = 0.01$  may be good enough because the number of false positives is about  $(|X| - |W|) \times P_{REQ} = 100$ , which is much fewer than  $|W|$ . However, if  $|W| = 10$ ,  $P_{REQ} = 0.01$  may become unacceptable since  $(|X| - |W|) \times P_{REQ} \approx 200 \gg |W|$ . Therefore, it is desirable to set the value of  $P_{REQ}$  such that the number of false positives in the search result is much smaller

than  $|W|$ , namely,  $(|X| - |W|) \times P_{REQ} \leq \frac{1}{\lambda}|W|$ . Let  $\lambda = 10$ , and we test the ITSP under three different parameter settings.

- (a)  $|X| = 5000$ ,  $|Y| = 50\,000$ , and  $R_{INTS}$  varies from 0.1 to 0.9, i.e.,  $|W|$  varies from 500 to 4500.  $P_{REQ} \leq \frac{500}{10 \times (5000 - 500)} \approx 0.01111$ . We set  $P_{REQ} = 10^{-2}$ .
- (b)  $|X| = 20\,000$ ,  $|Y| = 50\,000$ , and  $R_{INTS}$  varies from 0.01 to 0.9, i.e.,  $|W|$  varies from 200 to 18 000.  $P_{REQ} \leq \frac{200}{10 \times (20\,000 - 200)} \approx 0.00101$ . We set  $P_{REQ} = 10^{-3}$ .
- (c)  $|X| = 80\,000$ ,  $|Y| = 50\,000$ , and  $R_{INTS}$  varies from 0.01 to 0.9, i.e.,  $|W|$  varies from 500 to 45 000.  $P_{REQ} \leq \frac{500}{10 \times (80\,000 - 500)} \approx 0.00063$ . We set  $P_{REQ} = 10^{-4}$ .

For each parameter setting, we repeat the simulation 500 times to obtain the average false-positive ratio.

Fig. 5 shows the simulation results. In Fig. 5(a)–(c), we can see that the average  $P_{FP}$  is always smaller than the corresponding  $P_{REQ}$ . Hence, the search results using the ITSP meet the prescribed requirement of false-positive ratio in the average sense.

If we look into the details of individual simulations, we find that a small fraction of simulation runs have  $P_{FP}$  beyond  $P_{REQ}$ . For example, Fig. 6 depicts the results of 500 runs with  $|X| = 5000$ ,  $|Y| = 50\,000$ ,  $|W| = 500$ , and  $P_{REQ} = 10^{-2}$ . There are about 5% runs having  $P_{FP} > P_{REQ}$ , but that does not come as a surprise because the false-positive ratio in the context of filtering vectors (ITSP) or Bloom filters (CATS) is defined in a probability way: The probability for each tag in  $X - W$  to be misclassified as one in  $W$  is no greater than  $P_{REQ}$ . This *probabilistic* definition enforces a requirement  $P_{REQ}$  in an average sense, but not *absolutely* for each individual run.

### D. Performance Evaluation Under Channel Error

1) *Performance of ITSP-rem and ITSP-bem*: We evaluate the performance of ITSP-rem and ITSP-bem. To simulate the error rate  $P_{ERR}$  in ITSP-rem, we employ a pseudo-random number

TABLE VI  
PERFORMANCE COMPARISON.  $|Y| = 50\,000$ ,  $R_{INTS} = 0.1$ ,  $P_{REQ} = 0.001$

| $ X $   | ITSP    | ITSP-rem        |                  | ITSP-bem |
|---------|---------|-----------------|------------------|----------|
|         |         | $P_{ERR} = 5\%$ | $P_{ERR} = 10\%$ |          |
| 5,000   | 61,463  | 74,288          | 75,812           | 72,144   |
| 10,000  | 108,017 | 129,995         | 133,022          | 125,779  |
| 20,000  | 185,204 | 241,026         | 247,824          | 238,962  |
| 40,000  | 304,767 | 361,242         | 398,198          | 358,361  |
| 80,000  | 414,686 | 441,365         | 458,433          | 437,256  |
| 160,000 | 472,677 | 504,565         | 545,338          | 499,058  |
| 320,000 | 529,835 | 567,403         | 630,174          | 560,456  |
| 640,000 | 573,270 | 626,379         | 690,400          | 618,913  |

TABLE VII  
PERFORMANCE COMPARISON.  $|Y| = 50\,000$ ,  $R_{INTS} = 0.5$ ,  $P_{REQ} = 0.001$

| $ X $   | ITSP    | ITSP-rem        |                  | ITSP-bem |
|---------|---------|-----------------|------------------|----------|
|         |         | $P_{ERR} = 5\%$ | $P_{ERR} = 10\%$ |          |
| 5,000   | 105,828 | 160,481         | 166,469          | 153,838  |
| 10,000  | 206,709 | 211,513         | 221,771          | 210,805  |
| 20,000  | 335,426 | 371,974         | 391,983          | 370,557  |
| 40,000  | 512,156 | 577,305         | 617,196          | 577,305  |
| 80,000  | 656,426 | 735,592         | 789,874          | 735,592  |
| 160,000 | 721,347 | 793,482         | 865,617          | 793,482  |
| 320,000 | 721,347 | 793,482         | 865,617          | 793,482  |
| 640,000 | 721,347 | 793,482         | 865,617          | 793,482  |

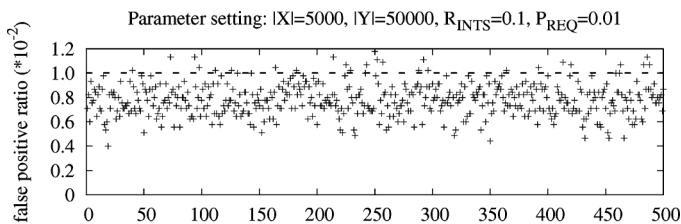


Fig. 6. False-positive ratio by the ITSP of 500 runs.

generator, which generates random real numbers uniformly in the range  $[0, 1]$ . If a bit in the filtering vector is “0” and the generated random number is in  $[0, P_{ERR}]$ , that bit is flipped to “1.”  $P_S$  can be simulated in a similar way. As for the burst error in ITSP-bem, we first calculate the values of  $P_l(w)$  with different  $w$  for a given  $l$ . Then, each  $w$  is assigned with a nonoverlapping range in  $[0, 1]$ , whose length is equal to the value of  $P_l(w)$ . For each interval, we generate a random number and check which range the number locates, thereby determining the number of errors in that interval.

We set  $P_{REQ} = 0.001$ ,  $P_S = 0.01$ , and  $R_{INTS} = 0.1, 0.5, 0.9$ , respectively. The values of  $|X|$  and  $|Y|$  are the same as those in Tables IV and V.  $l_s$  is set to 80 bits, and a 16-bit CRC is appended to each segment on forward link for integrity check. For ITSP-rem, we consider two cases with  $P_{ERR} = 5\%$  and  $10\%$ , respectively. For ITSP-bem, the prescribed parameters are set to be the following:  $\eta = 0.135$ ,  $\tau = 7.10$  with each interval to be 96 bits [36].

Tables VI–XI show the number of  $t_s$  slots needed under each parameter setting. The second column presents the results of ITSP when the channel is perfectly reliable. The third and fourth columns present the results of ITSP-rem with an error rate of 5% or 10%. The fifth column presents the results of ITSP-bem. It is not surprising that the search process under noisy channel generally takes more time due to the use of CRC and the higher false-positive probability of filtering vectors, and the execution time of the ITSP-rem is usually longer in a channel with a higher

TABLE VIII  
PERFORMANCE COMPARISON.  $|Y| = 50\,000$ ,  $R_{INTS} = 0.9$ ,  $P_{REQ} = 0.001$

| $ X $   | ITSP    | ITSP-rem        |                  | ITSP-bem |
|---------|---------|-----------------|------------------|----------|
|         |         | $P_{ERR} = 5\%$ | $P_{ERR} = 10\%$ |          |
| 5,000   | 124,553 | 156,041         | 163,718          | 155,972  |
| 10,000  | 231,236 | 275,394         | 290,493          | 275,256  |
| 20,000  | 403,954 | 454,929         | 486,150          | 454,929  |
| 40,000  | 678,066 | 752,753         | 814,890          | 752,753  |
| 80,000  | 721,347 | 793,482         | 865,617          | 793,482  |
| 160,000 | 721,347 | 793,482         | 865,617          | 793,482  |
| 320,000 | 721,347 | 793,482         | 865,617          | 793,482  |
| 640,000 | 721,347 | 793,482         | 865,617          | 793,482  |

TABLE IX  
PERFORMANCE COMPARISON.  $|X| = 10\,000$ ,  $R_{INTS} = 0.1$ ,  $P_{REQ} = 0.001$ .

| $ Y $  | ITSP    | ITSP-rem        |                  | ITSP-bem |
|--------|---------|-----------------|------------------|----------|
|        |         | $P_{ERR} = 5\%$ | $P_{ERR} = 10\%$ |          |
| 1,250  | 13,047  | 14,868          | 15,898           | 14,174   |
| 2,500  | 24,289  | 26,626          | 28,617           | 25,283   |
| 5,000  | 42,835  | 46,994          | 50,863           | 44,393   |
| 10,000 | 73,909  | 76,807          | 84,135           | 75,983   |
| 20,000 | 95,833  | 103,255         | 106,693          | 102,121  |
| 40,000 | 111,904 | 133,043         | 137,348          | 130,382  |

TABLE X  
PERFORMANCE COMPARISON.  $|X| = 10\,000$ ,  $R_{INTS} = 0.5$ ,  $P_{REQ} = 0.001$

| $ Y $  | ITSP    | ITSP-rem        |                  | ITSP-bem |
|--------|---------|-----------------|------------------|----------|
|        |         | $P_{ERR} = 5\%$ | $P_{ERR} = 10\%$ |          |
| 1,250  | 18,033  | 19,837          | 21,640           | 19,837   |
| 2,500  | 36,067  | 39,674          | 43,280           | 39,674   |
| 5,000  | 68,528  | 77,021          | 82,448           | 77,021   |
| 10,000 | 119,022 | 134,208         | 143,261          | 134,208  |
| 20,000 | 169,065 | 202,891         | 212,105          | 202,467  |
| 40,000 | 174,926 | 214,563         | 224,227          | 213,970  |

TABLE XI  
PERFORMANCE COMPARISON.  $|X| = 10\,000$ ,  $R_{INTS} = 0.9$ ,  $P_{REQ} = 0.001$

| $ Y $  | ITSP    | ITSP-rem        |                  | ITSP-bem |
|--------|---------|-----------------|------------------|----------|
|        |         | $P_{ERR} = 5\%$ | $P_{ERR} = 10\%$ |          |
| 1,250  | 18,033  | 19,837          | 21,640           | 19,837   |
| 2,500  | 36,067  | 39,674          | 43,280           | 39,674   |
| 5,000  | 72,134  | 79,348          | 86,561           | 79,348   |
| 10,000 | 144,269 | 158,696         | 173,123          | 158,696  |
| 20,000 | 192,960 | 217,245         | 232,272          | 217,245  |
| 40,000 | 232,904 | 261,277         | 277,300          | 261,173  |

error rate. An important positive observation is that the performance of the proposed protocol gracefully degrades in all simulations. The increase in execution time for both ITSP-rem and ITSP-bem is modest, compared to ITSP with a perfect channel. For example, even when the error rate is 10%, the execution time of ITSP-rem is about 10% ~ 30% higher than that of ITSP. This modest increase demonstrates the practicality of our protocol under noisy channel.

2) *False-Positive Ratio of ITSP-rem and ITSP-bem*: We use the same parameter settings in Section VI-C to examine the accuracy of search results by ITSP-rem and ITSP-bem. Meanwhile, for ITSP-rem, we set  $P_{ERR} = 5\%$  or  $10\%$ . For ITSP-bem, the required input parameter setting is  $\eta = 0.135$  and  $\tau = 7.10$ , with each 96-bit interval. Simulation results are delineated in Fig. 7, where the error rate is given between the parentheses after ITSP-bem. Clearly, the false-positive ratio in

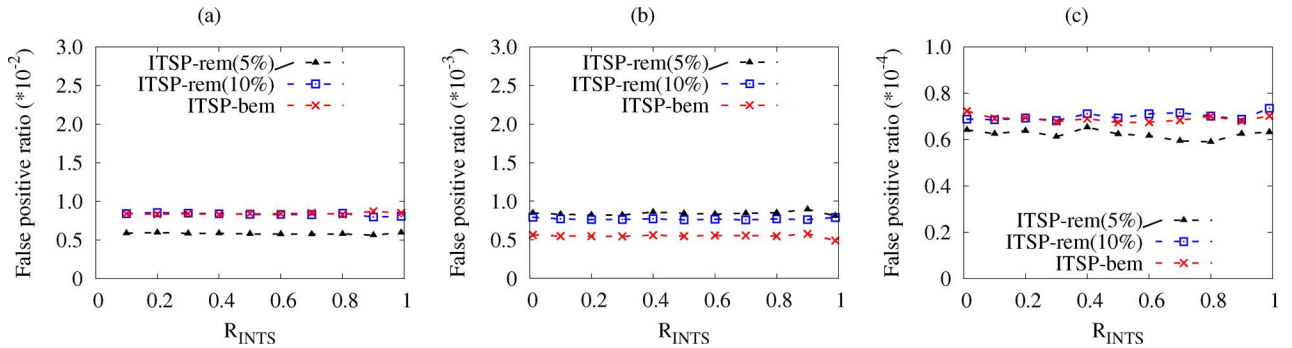


Fig. 7. False-positive ratio after running ITSP-rem, ITSP-bem, and CATS. (a)  $|X| = 5000$ ,  $|Y| = 50\,000$ ,  $P_{REQ} = 10^{-2}$ . (b)  $|X| = 20\,000$ ,  $|Y| = 50\,000$ ,  $P_{REQ} = 10^{-3}$ . (c)  $|X| = 80\,000$ ,  $|Y| = 50\,000$ ,  $P_{REQ} = 10^{-4}$ .

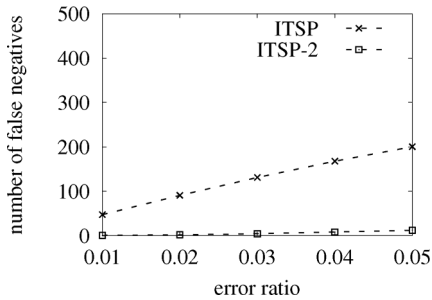


Fig. 8. False negatives due to signal loss in time-varying channel.

the search results after executing ITSP-rem or ITSP-bem is always within the bound of  $P_{REQ}$ . These results confirm that the false-positive ratio requirement is met under noisy channel.

3) *Signal Loss Due to Fading Channel*: We consider the scenario of a time-varying channel in which it may happen that a signal from a tag is not received by the reader in a deep fading slot. Although we consider this condition is relatively rare in an RFID system that is configured to work stably, we acknowledge in Section V-B that ITSP (or CATS) is not robust against this type of error. However, the problem can be alleviated by the tags transmitting each filtering vector twice. Fig. 8 shows the simulation results under parameters  $|X| = 10\,000$ ,  $|Y| = 5000$ ,  $|W| = 500$ , and  $P_{REQ} = 0.01$ . The horizontal axis shows the error rate, which is defined as the fraction of slots in deep fading, causing complete signal loss. ITSP-2 denotes the approach of transmitting each filtering vector from tags to the reader twice. When a wanted tag in  $W$  is not identified, we call it a *false negative*. The simulation results show that ITSP incurs significant false negatives when the error rate becomes large. For example, when the error rate is 2%, the average number of false negatives is 90.7. ITSP-2 works very well in reducing this number. When the error rate is 2%, its number of false negatives is just 1.95.

## VII. RELATED WORK

### A. Prior RFID Research

In the past, much RFID research concentrated on two fronts: 1) physical-layer technologies for transmitting IDs from tags to a reader more reliably, over a longer distance, and using less energy; 2) MAC-layer technologies for improving the rate at which a reader can collect IDs from tags. Tag identification protocols, which read IDs from all tags in an RFID system, mainly fall into two categories. One is *tree-based* [38]–[42], and the

other is *ALOHA-based* [43]–[46]. The tree-based protocols organize all IDs in a tree of ID prefixes [38]–[41]. Each in-tree prefix has two child nodes that have one additional bit, “0” or “1.” The tag IDs are leaves of the tree. The reader walks through the tree and requires tags with matching prefixes to transmit their IDs. The ALOHA-based protocols work as follows: The reader broadcasts a query request. With a certain probability, each tag chooses a time-slot in the current frame to transmit its ID. If there is a collision and the reader does not acknowledge positively, the tag will continue participating in the next frame. This process repeats until all tag IDs are read successfully. Unlike the basic ALOHA-based protocols where the frame size is fixed, RFID systems with DFSA [16]–[20] dynamically adjust the frame size in each round to improve throughput.

Another related research topic is cardinality estimation in an RFID system. Kodialam and Nandagopal [47] estimate the number of tags based on the probabilistic counting methods [48]. The same authors propose a nonbiased follow-up work in [49]. Han *et al.* [50] improve the performance of [47]. Qian *et al.* [51] present the Lottery-Frame (LoF) scheme for estimating the number of tags in a multiple-reader scenario. The work in [52] uses the maximum likelihood method. Sheng *et al.* design two probabilistic algorithms to identify large tag groups [3].

### B. Tag Identification With Collision Recovery Techniques

Collision recovery embodies an emerging direction for RFID technology, which aims at resolving tag IDs from collided signals, thereby improving the identification throughput.

Fyhn *et al.* [22] develop a theoretic model to resolve multiple tags from collisions. They take advantage of the channel fading, the difference in delay, and the frequency dispersion of tags to separate the collided signals. Meanwhile, by using the technique of successive interference cancellation (SIC), more tag IDs can be decoded from collisions that contain no more than five tags. This approach brings about 16% throughput gain compared to conventional tag identification protocols.

In [23], the Interframe SIC (ISIC) protocol is proposed to improve the collision recovery capability. In contrast to the traditional DFSA, where the tags randomly select slots within each frame to transmit their IDs, ISIC employs a deterministic pseudo-random function for slot selection. Hence, the tags do not need to explicitly inform the reader about the selected slots in different frames. A throughput improvement to about 1.2 tags per slot can be observed in ISIC. In the follow-up work [24], the authors find that the throughput gain of ISIC depends

on the signal format. A new technique called Interframe Soft Combining (ISoC) is introduced. The idea of ISoC originates from the observation that the reader may only recover a few bits of a tag ID from a single collision slot. Therefore, combining the bits recovered across multiple slots selected by the tag can increase the probability of successful decoding. ISoC is more efficient in terms of memory and computation when compared to ISIC, but its throughput gain is much smaller.

Based on rateless coding [53], a flameless slotted ALOHA is presented in [25]. Each frame is terminated when the instantaneous throughput of SIC is maximized. This protocol gives a throughput around 0.9 tags per slot. The problem is that since the frame sizes are not predetermined, a tag can hardly know its selected slots in other frames.

A theoretical upper bound of throughput in multiantenna RFID systems with collision recovery is derived in [26]. The reader is assumed to have perfect channel knowledge, and it can decode and acknowledge up to eight tags per slot using four receiving antennas. In addition, the tags are modified by adding *post-preambles* to responses to facilitate collision recovery. As a result, the maximal theoretical throughput is 3.1 tags per slot. In the follow-up work [27], the received signal is post-processed by a beamformer to further improve collision recovery. With this strategy, the maximal throughput is increased to 4.8 tags per slot using four receiving antennas.

## VIII. CONCLUSION

This paper studies the tag search problem in large-scale RFID systems. To improve time efficiency and eliminate the limitation of prior solutions, we propose an iterative tag search protocol (ITSP) based on a new technique that iteratively applies filtering vectors. Moreover, we extend the ITSP to work under noisy channel. The main contributions of our work are summarized as follows.

- 1) The iterative method of ITSP based on filtering vectors is very effective in reducing the amount of information to be exchanged between tags and the reader, and consequently saves time in the search process.
- 2) The ITSP performs much better than the existing solutions.
- 3) The ITSP works well under all system conditions, particularly in situations of  $|X| \gg |Y|$  when CATS works poorly.
- 4) The ITSP is improved to work effectively under noisy channel.

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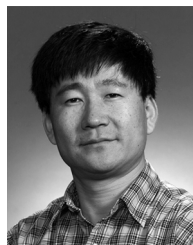
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