

Steganalysis of LSB Matching Revisited for Consecutive Pixels Using B-Spline Functions

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Outline

- 1 Introduction
- 2 Overview of LSBMR for Consecutive Pixels and EALSBMR
- 3 Steganalyzing the LSBMR Algorithm for Consecutive Pixels
- 4 Experimental Results
- 5 Concluding Remarks



LSBM, LSBMR, AND EALSBMR

- Least significant bit matching steganography (**LSBM**) is a tough target for steganalyzers.
 - The HCF COM method (proposed by Harmsen and Pearlman) and its descendants.
 - Universal steganalytic algorithms, including Shi 78-D, Farid 72-D, Moulin 156-D, and Li 110-D.
 - **No detectors have yet proven universally reliable.**
- Using a pair of pixels as an embedding unit, the least significant bit matching revisited algorithm (**LSBMR**) **dramatically** reduces modification rate when the payload holds.
- The edge adaptive image steganography based on LSB matching revisited (**EALSBMR**) is one of the recent important achievements in this field.



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Overview of LSBMR for Consecutive Pixels

LSBMRCP: one of the LSBMR pixel pair selection schemes adopted by EALSBMR.

LSBMRCP embedding procedure

- Cover image \Rightarrow a serial I of embedding units (x_i, x_{i+1}) .
- Secret message \Rightarrow a serial M of bits (m_i, m_{i+1}) .
- After message embedding, (x_i, x_{i+1}) is modified as (x'_i, x'_{i+1}) .

$$x'_i = \text{LSB}(x_i) \oplus m_i$$

$$x'_{i+1} = \text{LSB}(x_{i+1}) \oplus m_{i+1}$$
- both an increase and a decrease of x_i or x_{i+1} by one will change the value of $f(x'_i, x'_{i+1})$.



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 - $m_i = \text{LSB}(x'_i)$.
 - $m_{i+1} = f(x'_i, x'_{i+1}) = \text{LSB}(\lfloor x'_i/2 \rfloor + x'_{i+1})$.
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LSBMR embedding algorithm for a pixel pair

- 1: **if** $m_i = \text{LSB}(x_j)$ **then**
 - 2: **if** $m_{i+1} \neq f(x_i, x_{i+1})$ **then**
 - 3: $x'_{i+1} = x_{i+1} \pm 1$
 - ▷ x_j remains untouched
 - ▷ x_{i+1} is modified
 - 4: **else**
 - 5: $x'_{i+1} = x_{i+1}$
 - ▷ x_{i+1} remains untouched
 - 6: **end if**
 - 7: $x'_i = x_i$
 - ▷ x_i is modified
- 8: **else**
 - 9: **if** $m_{i+1} = f(x_i - 1, x_{i+1})$ **then**
 - 10: $x'_i = x_i - 1$
 - 11: **else**
 - 12: $x'_i = x_i + 1$
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Overview of EALSBMR

- EALSBMR is a region adaptive spatial domain LSB steganography.
- It uses the absolute difference between two adjacent pixels as the criterion for region selection, and adopt LSBMRCP as the data hiding algorithm.
- Decision of threshold T :
 - $EU(t) = \{(x_i, x_{i+1}) \mid |x_i - x_{i+1}| \geq t, \forall (x_i, x_{i+1}) \in V\}$
 - $T = \operatorname{argmax}_t \{2 \times |EU(t)| \geq |M|\}$
- Cover image is first divided into blocks. Block size $Bz \in \{1, 4, 8, 12\}$. When $Bz > 1$, blocks are rotated with a random degree in the range of $\{0, 90, 180, 270\}$ in order to improve the security.



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Effect of LSBMRCP embedding

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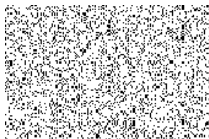
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Effect of LSBMRCP embedding

An illustration of the imbalance



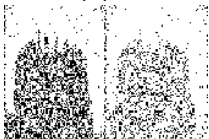
(a)



(b)



(c)



(d)



Steganalysis using B-spline Functions

- Data embedding \Leftrightarrow add additive noise to the cover image. The more pixels get modified, the more the power of the additive stegonnoise is added to the cover image.
- The power of the stegonnoise in $\{x_i\}$ should be larger than that in $\{x_{i+1}\}$.
- For a given stegonnoise series $\{\varepsilon_i\}$, its power is defined as its \mathcal{L}^2 norm:

$$\mathcal{IF} \triangleq \|\{\varepsilon_i\}\| = \left(\sum_{i=0}^n (\varepsilon_i^2) \right)^{\frac{1}{2}}$$



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- But, how to get the good estimation of the stegonnoise series for $\{x_i\}$ and $\{x_{i+1}\}$?



Steganalysis using B-spline Functions

- For a given suspected stego image, good estimation of the stegonoise series \Rightarrow good estimation of the original pixel series from the suspected stego one.
- Let the approximation of the original pixel series be a polynomial spline which can be constructed from a weighted sum of shifted B-splines.
- The polynomial spline establishes a sort of compromise between approximation and smoothness, which is controlled by an intuitive parameter S and can be calibrated depending on the variance of stegonoise σ^2 .



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- The polynomial spline establishes a sort of compromise between approximation and smoothness, which is controlled by an intuitive parameter S and can be calibrated depending on the variance of stegonoise σ^2 .
- Unfortunately, the theoretical calibration formula is infeasible in practice. But we put forward a computable approximation.



Steganalytic Feature

- The power of the noise introduced during the image capture and post-processing procedure is usually distributed evenly over the spatial domain. Cover image: $IF_1 \approx IF_2$.
- Stego image generated by LSBMRCP: $IF_1 > IF_2$.



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Discriminator for the presence of LSBMRCP steganography

$IF_1/IF_2 \approx 1$ for a cover image,

$IF_1/IF_2 > 1$ for a LSBMRCP stego image.



Estimation of Embedding Rate

- When calculating \mathcal{IF}_1 and \mathcal{IF}_2 ,
embedding rate $\nearrow \Rightarrow \sigma^2 \nearrow \Rightarrow S \nearrow$.
- Suppose the result smoothing B-spline based on S_c represents the original cover image.
- Given a LSBMR stego image, calculate $\mathcal{IF}_1/\mathcal{IF}_2$ using a progressively increasing S which starts from 0.
 - $S < S_c$, the result spline still contains stegonoise, $\mathcal{IF}_1 > \mathcal{IF}_2$.
 - $S > S_c$, $\mathcal{IF}_1 \approx \mathcal{IF}_2$.
- The critical point S_c lies in the interval in which the value of $\mathcal{IF}_1/\mathcal{IF}_2$ falls from larger than 1 to approximately equal to 1.
- $S_c \Rightarrow \sigma^2 \Rightarrow$ the estimation of embedding rate.



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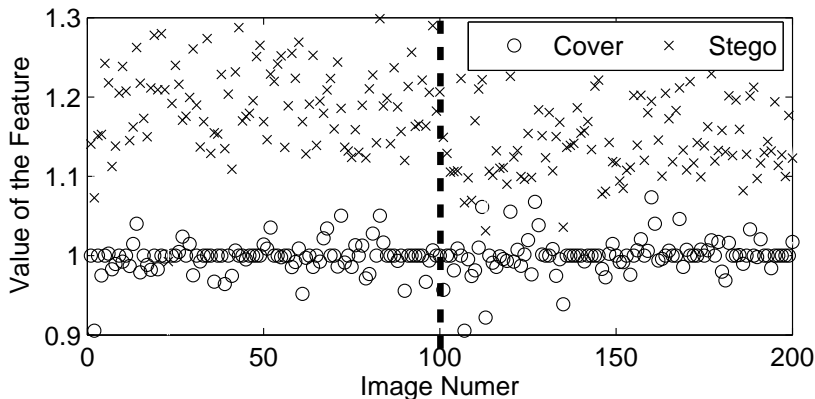
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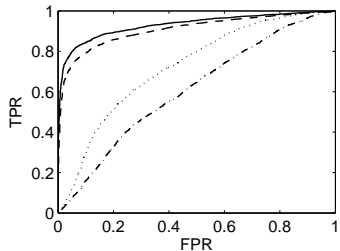
Plot of Steganalytic features

Steganalytic features of 200 cover images and the corresponding LSBMRCP stego images (Left half, with 50% embedding rate), and EALSBMR stego images (Right half, with 50% embedding rate, $B_z=1$).

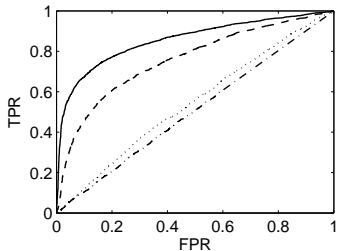


Comparisons of ROC curves

The different curves stand for: our proposed method against LSBMRCP (solid), and EALSBMR ($Bz = 1$) (dashed); Li-1D against LSBMRCP (dotted), and EALSBMR ($Bz = 1$) (dash-dot). (a) 50% embedding rate. (b) 25% embedding rate.



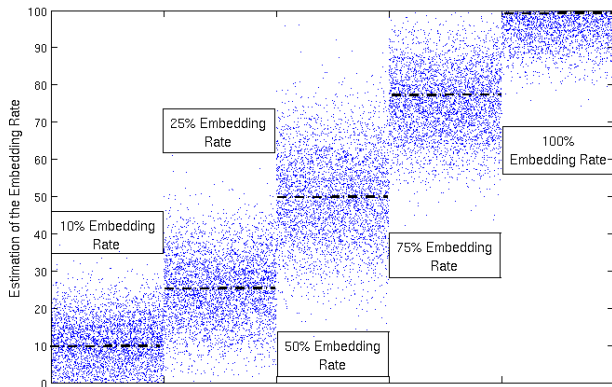
(a)



(b)

Estimation of embedding rate

Estimated value of the embedding rate for LSBMRCP stego images with embedding rate of 10%, 25%, 50%, 75% and 100%.



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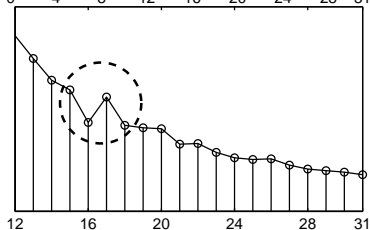
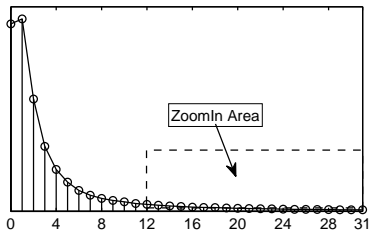
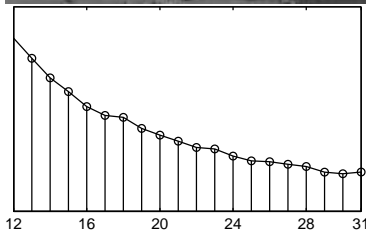


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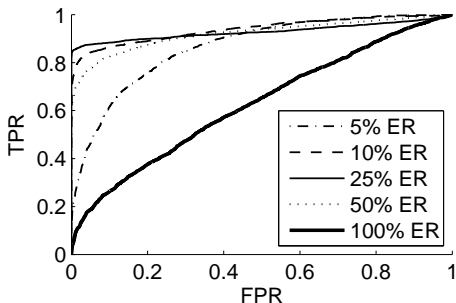


Steganalysis of EALSBMR using B-spline fitting

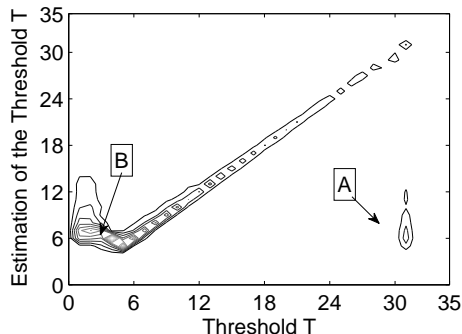


Steganalysis of EALSBMR using B-spline fitting

Comparison of ROC curves:



The contour graph of the number of the EALSBMR stego images:



★ Has been submitted to IEEE Signal Processing Letters. ★

Future work

- "The embedding units located at the sharper regions have better hiding characteristics than those at the smoother/flat regions." \Rightarrow "make full use of the sharper edges in a cover image as far as possible".
- Is it a good steganographic scheme? \Rightarrow target steganalysis of existing edge adaptive steganographic methods.
- Most steganographic/steganalytic algorithms are derived within a purely discrete framework. Can we do some research in this field based on a real-valued picture function defined over the real plane \mathbb{R}^2 ?



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 - Application of B-spline technology in steganalysis.
 - Steganalytic algorithm derived directly from a real-valued picture function.



The End

Q & A

