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# Investigation of Chaotic Image Encryption in Spatial and FrFT Domains for Cybersecurity Applications

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**ABSTRACT** The need for cybersecurity increases to protect the exchange of information for improving the data privacy. This paper presents an investigation of the encryption efficiency of the chaotic-based image block ciphering in the spatial and Fractional Fourier Transform (FrFT) domains. The main aim of this investigation is to examine the efficiency of different chaotic maps, while considering the parameters of the FrFT as additional keys for encryption and achieving reliable cybersecurity for robust image communication. In this paper, Cat, Baker, and Logistic map confusion approaches are applied in the spatial and FrFT domains to study and analyze the cybersecurity and ciphering efficiency of chaos-based image cryptosystems. The confusion features of the chaotic maps in spatial and FrFT domains are investigated using information entropy, differential analysis, histograms, visual observation, attack analysis, impact of noise, and encryption quality tests. Simulation results prove that the chaotic-based image encryption in the FrFT domain increases the efficiency of the confusion process and achieves a high nonlinear relation between the plainimage and the cipherimage in a symmetric ciphering approach. Moreover, the results demonstrate that the Cat-FrFT scheme is more susceptible to channel noise attacks than the Baker-FrFT and the Logistic-FrFT schemes. Hence, they can be implemented efficiently in the scenarios of noisy channels due to their high robustness to channel noise.

**INDEX TERMS** Arnold Cat map, chaotic Baker map, confusion, FrFT, Logistic map, image encryption.

# I. INTRODUCTION

Cybersecurity comprises data security, the applications, and infrastructure utilized for storing, processing, and transmitting information. It is known as the method that is employed for responding to, monitoring, and preventing cybersecurity events to protect the transmitted data and information. There is a strong focus on information exchange from the cyberse-

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curity perspective. However, current encryption methods are known to be unreliable for effective image encryption [1].

The sensitivity property to initial condition and control parameters that is inherent in chaotic methods can be used to achieve security requirements. The chaos-based framework proposed in [2] has two steps of confusion and diffusion processes. It is most frequently used as a base in current methods of chaotic image encryption [3], [4]. Image data is in general manipulated or processed either in spatial or transform domains. The security of an image ciphering algorithm is estimated based on Shannon's diffusion and confusion characteristics. Several image cryptosystems have been devised in both spatial and transform domains.

In the literature, several image encryption schemes have been introduced with diffusion and confusion mechanisms [4]–[27]. In [5], a ciphering scheme based on fractional cosine transform was proposed. In this scheme, the chaos is utilized to randomize the phases of the transmitted image in transformation and spatial domains. The results demonstrated the efficiency, validity, and robustness of this ciphering scheme against different attacks.

In [6], the authors introduced an image ciphering framework that employs spatial-temporal chaos maps. This framework has better ciphering features than those of the traditional Logistic map system. The bit-level pixel-based permutation is employed in this framework. In [7], an image ciphering scheme based on the deoxyribonucleic acid (DNA) and sine chaotic map was presented to encrypt the streamed images. The outcomes demonstrate that this encryption scheme performs sufficiently in the presence of different types of attacks due to the utilization of a large key space.

In [8], an image ciphering/deciphering scheme for color image transmission was presented. The original as well as the key main images are divided into RGB components. After that, the encrypted images are produced using the RGB components processed with XOR operation and scrambling. The statistical experimental tests on the ciphered and original images show an appreciated difference, but the approach was not robust to channel noise and different types of attacks. In addition, it was not appropriate for encrypting images of different dimensions.

In [9], a smooth affine transformation was implemented in the Gyrator Transform (GT) for encryption. The GT is utilized twice to enhance the encryption performance. The cipher keys are the affine and GT parameters. This study did not present a statistical security analysis. In [10], a cryptography scheme using one-time keys with chaotic maps was designed to achieve better security. The results introduced robust ciphered images in the presence of transmission noise and common multimedia attacks. The limitation of the works in [9] and [10] is the absence of a statistical security analysis.

In [11], an image ciphering scheme was presented based on chaotic Tent map. The statistical analysis revealed that the problems of the traditional Tent map technique are solved. In [12], a pixel shuffling operator was implemented to hide and mix the primary color components. This scheme is safe, key-sensitive, viable, and resistant to multimedia attacks.

In [13], the authors suggested an image ciphering framework based on the perceptron model within a neural network and Lorenz chaotic scheme. The experimental results show that this ciphering scheme has strong resistance and high security in the presence of multimedia attacks. In [14], a diffusion and confusion scheme for image ciphering based on DNA coding and chaotic maps was introduced. This scheme incurs confusion of the pixels through randomly transforming the nucleotide into its base pair. Moreover, it generates new keys based on the common keys and the plain image. The obtained results show that it achieves appreciated ciphering results, and it also has a large key space.

In [15], a ciphering technique based on the spatial/temporal lattice map was presented. It has some advantages and cryp-tography features compared to the traditional lattice map and the Logistic map. The experimental results demonstrated that this technique has a high efficiency and a good security performance compared to the traditional techniques. In [16], the authors suggested an image ciphering scheme that depends on a chaotic map and DNA coding. It utilizes the chaotic map to randomize the pixel positions. It also exploits the DNA coding to generate different ciphering rules. This technique enhances the ciphertext security, and the encoding performance. Moreover, it has a high key sensitivity and a large key space.

In [17], a double autonomous encryption method was suggested for the ciphering of color images based on a hybrid structure of a chaotic map and compressive sensing. The outcomes of this method assured reliable security. In [18], a color image cryptography approach depending on the chaos systems was presented. The chaotic maps are employed to cipher the color image components. The security is enhanced due to the reduction of the correlation values of the plain color image components. The results revealed high efficiency in the presence of multimedia attacks.

In [4], a ciphering system was implemented based on fractional chaotic methods for color images. The output results revealed uniform histograms, zero correlation, and high entropy results. In [19], a color image ciphering technique in the Fresnel zone was presented. The original color image is divided into three different masks using the Gerchberg phase Saxton iterative scheme. In [20], a color masking and shuffling encryption/decryption scheme was proposed. In order to improve the encryption performance, the fractional dual random masking and the chaotic Baker map were used. The experiments assured the success of this image communication scheme.

In [21], an image cryptography scheme depending on a chaotic map and DNA operations was introduced. This scheme comprises an XOR operation on the plainimage pixels based on the spatial/temporal chaotic map. After that, the DNA operation is applied to further confuse the plainimage. The tests showed that this scheme can resist the transmission multimedia attacks, efficiently. In [22], a hybrid structure comprising Double Random Phase Encoding (DRPE) and Baker map encryption was implemented. The Discrete Wavelet Transform (DWT) is performed to divide the original input image into approximate and detail components. Then, the chaotic Baker map is employed to encrypt the detail components. After that, to minimize the auto-correlation between the encrypted pixels, the DRPE is performed. The output results demonstrated appreciated key sensitivity and robustness to channel noise.

In [23], a color image ciphering algorithm based on a high-dimension chaotic map framework and a bit-level spatial permutation technique was investigated. In this algorithm, the scrambling is performed with a Piece-Wise Linear Chaotic Map (PWLCM) due to its ciphering efficiency. The security analysis results prove robustness, and large key space to resist different types of common attacks.

In [24], a dynamic random growth-based hybrid chaotic maps block image ciphering scheme was proposed. In this scheme, the Cat map is utilized as another security key to improve the suggested scheme security performance and efficiency. The simulation outcomes prove that this ciphering scheme is more robust and secure against different types of attacks.

In [25], a cybersecurity technique was presented for the purpose of intrusion detection. It proved efficiency for stopping and mitigating the serious malicious activities. This technique introduced an accuracy of 94.50%.

In [26], the authors introduced a chaos-based selective image cryptosystem to achieve minimization of the communication overhead, low computational cost, and an efficient security performance in the presence of different types of multimedia attacks. This cryptosystem is based on employing the skew Tent chaotic map. The simulation results demonstrated efficient selective image ciphering, higher security, good correlation, diffusion, good histograms, and large entropy.

In [27], a fast and parallel-processing image cryptosystem was presented. It exploits the image permutation process to achieve and guarantee an efficient permutation performance, low space, and less complexity. A parallel image diffusion process is implemented to ensure the utmost parallelism of the diffusion in order to guarantee robust subjective and objective results.

It is known that the most serious issue of image communication through wireless networks is the problem of security. Hence, in this paper, the encryption efficiency of the different confusion chaotic maps in the spatial and FrFT domains is studied. The objective is the selection of the most appropriate, suitable, convenient, and proper chaotic maps for encrypting images in the spatial and FrFT domains for communication scenarios. The influence of the FrFT parameters as additional encryption keys is also investigated. The Cat, Baker, and Logistic maps are considered in the spatial and FrFT domains.

The main advantage of employing the proposed image cryptosystem in the FrFT domain is to achieve more permutation, high cipher key sensitivity, and more immunity to transmission noise. The security performance of the suggested image cryptography scheme is carefully investigated through information entropy, differential analysis, visual inspection, attacks analysis, histograms, ciphering quality analysis, and effect of channel noise. The whole experimental outcomes ensure that the proposed image cryptography scheme in this paper is robust and secure compared to the ordinary techniques. Therefore, it can be utilized for robust and secure multimedia transmission applications and systems. The main contribution of this work is investigating and combining the main advantages of the FrFT and chaotic map encryption schemes for efficient transmission of digital images, securely. The paper sections are arranged as follows. Section II explores and discusses the FrFT basics and different types of chaotic maps. Section III gives in detail the explanation of the suggested image ciphering technique. The simulation and performance tests are introduced in section IV. In section V, the communication noise impact on the decryption mechanism is investigated. The effect and influence of the FrFT angles upon the encryption process is tested in section VI. In section VII, a comparative study amongst the suggested technique and peer-reviewed and recent previous techniques is given. Finally, the conclusions are summarized in section VIII.

### **II. RELATED PRELIMINARY BASICS**

#### A. FRACTIONAL FOURIER TRANSFORM (FrFt)

The FrFT can be considered as a linear transformation, which rotates, in the counterclockwise direction, the input signal with spatial coordinates (t, w) to new coordinates (u, v) by an angle  $\alpha = a\pi/2, 0 \le a \le 1$ , in the continuous time-frequency plane. The FrFT is named rotational FT or angular FT. It is formulated with the aid of a transform kernel as follows [28]:

$$K_{\alpha}(t,u) = \begin{cases} \sqrt{\frac{1-j\cot\alpha}{2\pi}} \cdot \exp(j\frac{t^2+u^2}{2}\cot\alpha - j\frac{tu}{\sin\alpha}) \\ & \text{if } \alpha \neq n\pi \\ \delta(u-t) & \text{if } \alpha = n\pi \\ \delta(u+t) & \text{if } \alpha = (2n+1)\pi \end{cases}$$
(1)

If there is a given x(t), its FrFT is given by  $X_{\alpha}(u)$  as in Eq. 2. The free variable u is treated as a joint frequency/time variable.

$$X_{\alpha}(u) = \int_{-\infty}^{\infty} x(t) K_{\alpha}(t, u) dt$$
 (2)

Similarly, a function f(x) has the following form of transformation:

$$f_a(u) = F^a[f(x)]$$

$$= C_\alpha \int f(x) \exp[j\pi \frac{u^2 + x^2}{\tan \alpha} - 2j\pi \frac{ux}{\sin \alpha}]dx$$

$$\alpha = \frac{a\pi}{2}, \text{ and } C_\alpha = \frac{\exp[-j(\frac{\pi . sign(\sin(\alpha))}{4} - \frac{\alpha}{2})]}{|\sin \alpha|^{1/2}} \quad (3)$$

where *a* defines the transform fractional order and  $F^{\alpha}$  represents the FrFT. The FrFT has a period of 4, and the transformation magnitude lies in [-2, 2].

The FrFT has one degree of freedom more than the conventional FT as it has an angle in both x and y directions.

The mathematical model of the general discrete FrFT is discussed as follows. Assume f(x) is a function with a

period  $\Delta_0$ , the FrFT with  $p^{\text{th}}$  order of f(x) is computed using Eq. (4) [28]:

$$f_p = \sum_{k=0}^{N-1} f\left(k\frac{\Delta_0}{N}\right) \sum_{n=-\infty}^{\infty} k_p\left(x, \left(n+\frac{k}{N}\right)\Delta_0\right) \quad (4)$$

So, the forward and inverse 2D discrete FrFT of the signal are obtained as [28]:

$$F_{\alpha,\beta}(m,n) = \sum_{p=0}^{M-1} \sum_{q=0}^{N-1} f(p,q) K_{\alpha,\beta}(p,q;m,n)$$
(5)

$$f_{\alpha,\beta}(p,q) = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} F_{\alpha,\beta}(m,n) K_{-\alpha,-\beta}(p,q;m,n)$$
(6)

where  $(\alpha, \beta)$  denotes the 2D discrete FrFT order,  $K_{\alpha,\beta}(p,q;m,n) = K_{\alpha} \otimes K_{\beta}$  represents the transformation kernel, and  $K_{\alpha}, K_{\beta}$  denote the 1D discrete FrFT kernels.

The 2D FrFT has many applications in signal processing. One of the most important and common applications of the 2D FrFT is the encryption process. For the encryption of an image, we may multiply the image with a random phase, followed by applying the 2D FrFT and the resulting intensity is then stored. The extra degree of freedom possessed by the FrFT makes the hacking on the encrypted image more difficult. Thus, in this paper, we consider the parameters of the 2D FrFT as additional keys for an efficient encryption process.

## **B. CHAOTIC MAP ENCRYPTION**

A diversity of chaotic maps can be used for image encryption. They are highly sensitive to their initial conditions. The sensitivity to initial conditions of chaotic systems is usually referred to as the butterfly effect. When utilizing different initial values, the chaotic system is operated in various orbits that are difficult to be analyzed and computed. Therefore, the data obtained from chaotic systems are well-conditioned to obey diffusion and confusion criteria. Arnold's Cat map, Baker map, and Logistic map are three examples of confusion chaotic maps [16].

# C. ARNOLD CAT MAP

Arnold Cat map can directly be iterated to confuse and rearrange the pixel positions of the image without changing their values. The results of the randomization and scrambling process are different for different iterations. Thence, this map can be employed for achieving image ciphering. The generalized 2D-Arnold Cat map is represented as follows [18]:

$$\begin{bmatrix} x'\\ y' \end{bmatrix} = A \begin{bmatrix} x\\ y \end{bmatrix} \pmod{n}$$

$$A = \begin{bmatrix} 1 & p\\ q & pq+1 \end{bmatrix}$$
(7)

The inverse 2D Arnold Cat map is expressed as follows [18]:

$$\begin{bmatrix} x \\ y \end{bmatrix} = A^{-1} \begin{bmatrix} x' \\ y' \end{bmatrix} \pmod{n}$$

$$A^{1} = \begin{bmatrix} pq+1 & -p \\ -q & 1 \end{bmatrix}$$
(8)

where *p* and *q* are two positive constant control variables, *n* is the number of iterations. The indices *x* and *y* refer to the pixel position in the original  $N \times N$  image. Both *x*, and *y*  $\in \{0, 1, 2, \dots, N-1\}$ , and x' and y' refer to the pixel position after confusion.

The main important features of the Arnold Cat map are the periodicity and repeatability. The original image can be reconstructed after iterating the Cat map up to a certain number of rounds R. The number of iterations is known as the periodicity value, and this value depends on the image size. By altering the control variables p, q, and the image size, the image is reconstructed after a certain number of iterations. Thence, the parameters p, q, and the image size can be exploited as three different types of cipher keys to perform image encryption with the Arnold Cat map. Moreover, the angle of the suggested FrFT in this paper can be considered as an additional secret key.

### D. 2-D CHAOTIC BAKER MAP

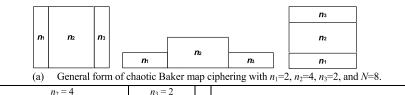
The chaotic Baker map is utilized to scramble a square unit using a 2-D mapping mechanism. The chaotic Baker map operation comprises two processes of breaking the input square unit into identical parts, and then the two divided halves are accumulated along one another. The description of the Baker map (B) is formulated as follows:

$$B(x, y) = (2x, y/2), \quad 0 = < x < 0.5$$
  
$$B(x, y) = (2x - 1, y/2 + 1/2), \quad 0.5 = < x <= 1 \quad (9)$$

The process of dividing the input square unit to two separate identical and similar rectangles is not recommended in the process of random scrambling and distribution because of its simplicity. Therefore, there are two other types of chaotic Baker map utilizing a U operator as a secret key for the splitting process. The U operator consists of k different elements, where the square unit is split into k different vertical rectangles. The discretized chaotic Baker map mechanism is summarized as:

- 1. Divide the input square unit with size  $N \times N$  into a number of *k* different vertical rectangles of width  $n_i$  and height *N*, where  $N = n_1 + n_2 + ... + n_k$ .
- 2. Stretch the vertically divided rectangles into horizontal rectangles.
- 3. Rearrange the reformatted rectangles to put the right rectangle at the top and the left rectangle at the bottom.

Therefore, the Baker map moves each pixel within the input square unit to a new location within the square in a bijective manner. The 2D discretized chaotic Baker map is symbolized



| $n_1$     | = 2       |           | $n_2$     | = 4       |           | $n_3$     | = 2       |           |           |           |           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| $PL_1$    | $PL_2$    | $PL_3$    | $PL_4$    | $PL_5$    | $PL_6$    | $PL_7$    | $PL_8$    | $PL_{31}$ | $PL_{23}$ | $PL_{15}$ | $PL_7$    | $PL_{32}$ | $PL_{42}$ | $PL_{16}$ | $PL_8$    |
| $PL_9$    | $PL_{10}$ | $PL_{11}$ | $PL_{12}$ | $PL_{13}$ | $PL_{14}$ | $PL_{15}$ | $PL_{16}$ | $PL_{63}$ | $PL_{55}$ | $PL_{47}$ | $PL_{39}$ | $PL_{64}$ | $PL_{56}$ | $PL_{48}$ | $PL_{40}$ |
| $PL_{17}$ | $PL_{18}$ | $PL_{19}$ | $PL_{20}$ | $PL_{21}$ | $PL_{22}$ | $PL_{23}$ | $PL_{24}$ | $PL_{11}$ | $PL_3$    | $PL_{12}$ | $PL_4$    | $PL_{13}$ | $PL_5$    | $PL_{14}$ | $PL_6$    |
| $PL_{25}$ | $PL_{26}$ | $PL_{27}$ | $PL_{28}$ | $PL_{29}$ | $PL_{30}$ | $PL_{31}$ | $PL_{32}$ | $PL_{27}$ | $PL_{19}$ | $PL_{28}$ | $PL_{20}$ | $PL_{29}$ | $PL_{21}$ | $PL_{30}$ | $PL_{22}$ |
| $PL_{33}$ | $PL_{34}$ | $PL_{35}$ | $PL_{36}$ | $PL_{37}$ | $PL_{38}$ | $PL_{39}$ | $PL_{40}$ | $PL_{43}$ | $PL_{35}$ | $PL_{44}$ | $PL_{36}$ | $PL_{45}$ | $PL_{37}$ | $PL_{46}$ | $PL_{38}$ |
| $PL_{41}$ | $PL_{42}$ | $PL_{43}$ | $PL_{44}$ | $PL_{45}$ | $PL_{46}$ | $PL_{47}$ | $PL_{48}$ | $PL_{59}$ | $PL_{51}$ | $PL_{60}$ | $PL_{52}$ | $PL_{61}$ | $PL_{53}$ | $PL_{32}$ | $PL_{54}$ |
| $PL_{49}$ | $PL_{50}$ | $PL_{51}$ | $PL_{52}$ | $PL_{53}$ | $PL_{54}$ | $PL_{55}$ | $PL_{56}$ | $PL_{25}$ | $PL_{17}$ | $PL_9$    | $PL_1$    | $PL_{26}$ | $PL_{18}$ | $PL_{10}$ | $PL_2$    |
| PL57      | $PL_{58}$ | $PL_{59}$ | $PL_{60}$ | $PL_{61}$ | $PL_{62}$ | $PL_{63}$ | $PL_{64}$ | $PL_{57}$ | $PL_{49}$ | $PL_{41}$ | $PL_{33}$ | $PL_{58}$ | $PL_{50}$ | $PL_{42}$ | $PL_{34}$ |

(b) In-detail form of 2D discretized chaotic Baker map ciphering.

FIGURE 1. The chaotic Baker map ciphering process of an 8 × 8 image.

as  $B(n_1, n_2, ..., n_k)$ . The k integers sequence  $(n_1, n_2, ..., n_k)$ is selected so that every integer  $n_i$  divides N, and  $N_i = n_1 + ... + n_i$ . Each pixel at location (r, s) with  $0 \le s < N$  and  $N_i \le r < N_i + n_i$  is mapped to:

$$B_{(n_1,\dots,n_k)}(r,s) = \left[\frac{N}{n_i} (r-N_i) + s \mod\left(\frac{N}{n_i}\right), \frac{n_i}{N} \times \left(s - s \mod\left(\frac{N}{n_i}\right)\right) + N_i\right] \quad (10)$$

Therefore, the general operation of the chaotic Baker map is that each input  $N \times N$  square array is divided into k vertical different rectangles of width  $n_i$  and height N. After that, each vertical rectangle with dimensions  $N \times n_i$  is further divided into  $n_i$  small boxes, where each box has N points. Each small box is mapped into a row of pixels in a column-by-column form, where the right box is mapped at the top and the left box is mapped at the bottom. For example, the permutation process of an  $8 \times 8$  input square image is shown in Fig. 1. The B operator works with a key (2, 4, 2), where  $n_1 = 2$ ,  $n_2 = 4$ ,  $n_3 = 2$ , and N = 8. Fig. 1(a) demonstrates the general form of the Baker map ciphering process of the Baker map.

#### E. CHAOTIC LOGISTIC MAP

The 2D Logistic map may be considered as an expansion of the 1D Logistic map. It is utilized to overcome the problems of the 1D Logistic map. The 2D Logistic map F(x, y) is defined as:

$$x_{i+1} = \alpha_1 x_i (1 - x_i) + \beta_1 N_i^2 \tag{11}$$

$$y_{i+1} = \alpha_2 y_i (1 - y_i) + \beta_2 (x_i^2 + x_i y_i)$$
(12)

where  $\alpha_1$ ,  $\beta_1$ ,  $\alpha_2$ ,  $\beta_2$ ,  $N_i$  are control parameters, and *i* varies as 0, 1, 2..., and so on. The  $x_0$  and  $y_0$  are initial conditions. In this paper, we focus on the parameters that make the system chaotic. The ranges of the control parameters are  $2.75 \le \alpha_1 \le 3.4, 0.15 \le \beta_1 \le 0.21, 2.7 \le \alpha_2 \le 3.45,$  $0.13 \le \beta_2 \le 0.15$ . The large key space makes it hard to predict the secret information.

## **III. THE PROPOSED ENCRYPTION SCHEME**

In the suggested ciphering scheme, we employ three different types of chaotic maps, which have different characteristics to investigate the confusion efficiency in the spatial and transform domains. The suggested ciphering scheme comprises two different sections. Firstly, the FrFT is employed on the input image. Secondly, the suggested confusion technique using Arnold Cat map, 2D chaotic Baker map, or 2D Logistic map is performed, separately.

Therefore, the confusion process is performed in the FrFT domain, in which the angle works as an additional cipher key, and this presents a high degree of scrambling and randomization. The framework of the suggested ciphering/deciphering scheme is given as follows.

The steps of the ciphering technique are summarized as follows:

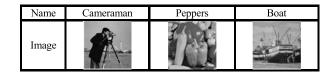
- 1. Read the input image.
- 2. Apply the FrFT on the input image.
- 3. Apply chaotic map ciphering (Cat, Baker, or Logistic).
- 4. Apply the inverse FrFT on the output of step 3.
- 5. Transmit the encrypted image to the receiver side through a communication channel.

The steps of the deciphering technique are summarized as follows:

- 1. Receive the encrypted image.
- 2. Apply the FrFT on the encrypted image.
- 3. Apply chaotic map deciphering (Cat, Baker, or Logistic).
- 4. Apply the inverse FrFT on the decrypted image.

Therefore, the proposed image encryption scheme applies FrFT on the input plainimage. Then, the resulting image coefficients are scrambled by applying different types of chaotic maps. The efficiency and security of the suggested scheme are studied considering the effect of noise, information entropy, visual inspection, histograms, attacks, differential and encryption quality metrics. All numerical results confirm that the suggested image encryption scheme preserves a good confusion property.

#### TABLE 1. Different samples of source images.



## **IV. SIMULATION RESULTS**

To evaluate the proposed encryption scheme, it is tested on the standard Cameraman, Peppers, and Boat images of  $256 \times 256$  pixels as shown in Table 1. The obtained results are evaluated depending on entropy, visual results, histograms, ciphering quality, and differential analysis [29]–[31].

## A. VISUAL RESULTS

The visual results are the most remarkable factor in evaluating the ciphered image, where a greatly hidden ciphered image means that the suggested ciphering technique is better and recommended. The resulting ciphered images in the spatial and FrFT domains utilizing various chaotic maps are shown in Table 2 for the Cameraman, Peppers, and Boat images. From the introduced results, ciphering using the suggested technique succeeded in hiding the main distinctive features of the input plain images.

# **B. ENTROPY ANALYSIS**

The structural features of the main image must not be seen in an enciphered image. Entropy is a measure of the degree of unpredictability of structural characteristics. The formula used to calculate the entropy value E(x) for a cipherimage x is [32]:

$$E(x) = -\sum_{i=1}^{2^{N}-1} P(x_{i}) \log_{2} P(x_{i})$$
(13)

where  $P(x_i)$  is the probability of occurrence of symbol  $x_i$  in the cipher image x, N is the number of bits for the symbol  $x_i$  and  $\log_2$  is used to compute the entropy as a function of bits. The resulting pixel values are in the interval [0, 255]. It is a fact that the most desirable entropy value for an enciphered image is 8. The closer it gets to 8, the more secure is the cryptosystem.

The entropy values of the enciphered images in the spatial and FrFT domains using different confusion chaotic maps are introduced in Table 3. It is clear from the presented results that the entropies of the enciphered images tend to 8, which is the optimal entropy value. Consequently, the information leakage during the ciphering can be neglected. Thus, the proposed confusion-based image encryption scheme is robust to entropy attack.

## C. HISTOGRAM ANALYSIS

The image histogram is used to count and graph the pixels at each gray intensity level. The results of histogram test for the source images and also for the enciphered images using the proposed chaotic maps in the spatial and FrFT domains are presented in Table 4. In the histogram results, the horizontal axis shows the possible intensity values, and the vertical axis shows the number of pixels for each of these intensity values.

As the proposed ciphering technique involves permutation only, there is no change in the pixel values. Hence, we can see from the histogram results presented in Table 4 that the histograms of enciphered images in the spatial and FrFT domains using different chaotic maps are identical to the histograms of the corresponding source images. Thus, the statistical metrics of an enciphered image are identical to those of the corresponding source image.

# D. ENCRYPTION QUALITY ANALYSIS

In this section, we evaluate the suggested image encryption scheme by investigating the most commonly used ciphering quality parameters like the correlation coefficient  $(r_{xy})$ between the source and the enciphered images, histogram deviation  $(D_H)$  between the source and the enciphered images, and the irregular deviation  $(D_I)$  of the enciphered image. They are utilized to present a comparison between the proposed chaotic maps in the spatial and FrFT domains.

The correlation coefficient  $(r_{xy})$  between the source and the enciphered images can be computed if they are transformed to 1D sequences using Eq. (14) [33]:

$$r_{xy} = \frac{\operatorname{cov}(x, y)}{\sqrt{D(x)}\sqrt{D(y)}},\tag{14}$$

where *x* is the main image and *y* is the enciphered image,

$$cov(x, y) = \frac{1}{L} \sum_{i=l}^{L} (x(i) - E(x))(y(i) - E(y)),$$
$$D(x) = \frac{1}{L} \sum_{i=l}^{L} (x(i) - E(x))^{2},$$
$$D(y) = \frac{1}{L} \sum_{i=l}^{L} (y(i) - E(y))^{2},$$

and L defines the pixel count in the image. The main target is to achieve low values of correlation amongst the enciphered and source images. The correlation values between the source and enciphered images are tabulated in Table 5.

The histogram deviation  $(D_H)$  estimates the suggested ciphering scheme quality by measuring how it increases the deviation between the source and enciphered images [34]. So, it is calculated as the difference between the areas under the histogram curves, and thus it can be estimated using the formula:

$$D_H = \frac{\left(\sum_{i=0}^{255} d(i)\right)}{W \times H},\tag{15}$$

where d(i) defines the histogram difference between the source and enciphered images with pixel level *i*. The original or the enciphered image dimensions are denoted by



|           | Er  | Enciphering with different chaotic maps in spatial and FrFT domains |          |          |             |               |  |  |  |
|-----------|-----|---|----------|----------|-------------|---------------|--|--|--|
| Images    | S   | spatial Doma  | in       |          | FrFT Domain | ı             |  |  |  |
| mages     | Cat | Baker   | Logistic | Cat-FrFT | Baker-FrFT  | Logistic-FrFT |  |  |  |
| Cameraman |     |   |          |          |             |               |  |  |  |
| Peppers   |     |   |          |          |             |               |  |  |  |
| Boat      |     |   |          |          |             |               |  |  |  |

TABLE 2. Encryption results of the test images using the different proposed chaotic maps in spatial and FrFT domains.

**TABLE 3.** Entropy of the enciphered images using the proposed chaotic maps in spatial and FrFT domains.

|           | Enciphering scheme |            |          |              |                |                   |  |  |  |
|-----------|--------------------|------------|----------|--------------|----------------|-------------------|--|--|--|
| т         | S                  | patial Dom | ain      |              | FrFT Domain    |                   |  |  |  |
| Image     | Image Cat Baker    |            | Logistic | Cat-<br>FrFT | Baker-<br>FrFT | Logistic-<br>FrFT |  |  |  |
| Cameraman | 7.0097             | 7.0097     | 7.0229   | 7.0097       | 7.0097         | 7.0097            |  |  |  |
| Peppers   | 7.5937             | 7.5937     | 7.5807   | 7.5937       | 7.6056         | 7.6068            |  |  |  |
| Boat      | 7.1238             | 7.1238     | 7.0944   | 7.1238       | 7.1238         | 7.1237            |  |  |  |

 $W \times H$ . The main target is to achieve higher values of  $D_H$ . The histogram deviation values between the source and enciphered images are tabulated in Table 6.

The proposed ciphering scheme quality can be ascertained using the estimated irregular deviation  $(D_I)$  [30]. It is used to measure the amount of irregular deviations resulting from ciphering of the main source image. The  $D_I$  value can be estimated by Eq. (16) as:

$$D_I = \frac{\left|\sum_{i=0}^{255} h_d(i)\right|}{W \times H},\tag{16}$$

$$h_d(i) = |h(i) - M|,$$
 (17)

where the enciphered image histogram at intensity value *i* is h(i), and *M* is the average of a pre-supposed histogram with a uniform distribution for an ideally enciphered image. The main target is to achieve lower values of  $D_I$ . The irregular deviation results for the enciphered images are introduced in Table 7. It is noticed from the introduced results that the efficiency of the suggested chaotic maps for ciphering of images in the FrFT domain is more appreciated and recommended than that of ciphering of images in the spatial domain.

## E. DIFFERENTIAL ANALYSIS

The working principle behind the differential attack is changing a pixel or a bit in the main image and then enciphering to discover the difference between the two enciphered images. Therefore, the resistance of proposed confusion-based image ciphering scheme to differential attacks is studied using values of the Number of Pixel Change Rate (NPCR) and the Unified Averaged Changed Intensity (UACI). These results are estimated to check the sensitivity efficiency of the proposed

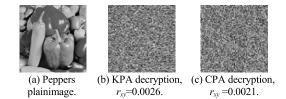


FIGURE 2. The resistance of the proposed FrFT-Logistic image cryptosystem to KPA and CPA.

ciphering scheme. Let us consider two enciphered images  $C_1$  and  $C_2$  for two source images  $SI_1$  and  $SI_2$ , which have a size of  $H \times W$ . If the pixel values for any component of the enciphered images  $C_1$  and  $C_2$  at position (i, j) are different, then D(i, j) = 1. The UACI and NPCR values are calculated for the enciphered images  $C_1$  and  $C_2$  utilizing Eq. (18) and (19) [35]–[37]:

$$NPCR = \frac{\sum_{i,j} D(i,j)}{W \times H} \times 100\%, \tag{18}$$

$$UACI = \frac{1}{W \times H} \left[ \sum_{i,j} \frac{C_1(i,j) - C_2(i,j)}{255} \right] \times 100\%,$$
(19)

It is observed from the introduced results in Tables 8 and 9 that the Logistic-FrFT scheme offers the highest NPCR score, and the UACI score is zero for all tested images. This proves that the suggested encryption scheme is a highly sensitive to little variations in the source images, and thus it is robust to differential attacks.

# F. KPA AND CPA ANALYSIS

The resistance of the proposed image cryptosystem is examined to both Known Plaintext Attack (KPA) and Chosen Plaintext Attack (CPA). Fig. 2(a) depicts the Peppers plainimage. The deciphering outcomes of both KPA and CPA are shown in Fig. 2(b) and Fig. 2(c). The correlation values of KPA and CPA results are 0.0026 and 0.0021, respectively. These correlation coefficient values ensure the immunity of the proposed Logistic-FrFT scheme to both KPA and CPA.

## **V. EFFECT OF NOISE**

The PSNR, SSIM, and FSIM are computed for the purpose of evaluation of the visual quality of the decrypted images

### TABLE 4. Histogram results of the source images and enciphered images using the different proposed chaotic maps in the spatial and FrFT domains.

|           |        |     |                | Encipheri | ng scheme |             |                   |  |  |
|-----------|--------|-----|----------------|-----------|-----------|-------------|-------------------|--|--|
| Image     | Source |     | Spatial Domain |           |           | FrFT Domain |                   |  |  |
| image     | image  | Cat | Baker          | Logistic  | Cat-FrFT  | Baker-FrFT  | Logistic-<br>FrFT |  |  |
| Cameraman |        |     |                |           |           |             |                   |  |  |
| Peppers   |        | 4   | 1              |           | 11        |             | 5                 |  |  |
| Boat      | 5      |     |                | 3         | A         |             |                   |  |  |

### TABLE 5. The correlation values between the source and enciphered images using the different proposed chaotic maps in the spatial and FrFT domains.

|           | Enciphered image      |            |           |             |            |               |  |  |  |  |
|-----------|-----------------------|------------|-----------|-------------|------------|---------------|--|--|--|--|
| Image     | Sp                    | atial Doma | in        | FrFT Domain |            |               |  |  |  |  |
|           | Cat                   | Baker      | Logistic  | Cat-FrFT    | Baker-FrFT | Logistic-FrFT |  |  |  |  |
| Cameraman | 0.0031                | 0.0359     | 0.0011453 | -0.0029     | -0.0025    | 0.002036      |  |  |  |  |
| Peppers   | -0.0031               | 0.0080     | -0.000167 | -0.0039     | 0.0115     | 0.00362       |  |  |  |  |
| Boat      | 5.22×10 <sup>-4</sup> | -0.0213    | 0.000776  | 0.0085      | 0.0234     | -0.000811     |  |  |  |  |

#### TABLE 6. Histogram deviation between source and enciphered images using the different proposed chaotic maps in the spatial and FrFT domains.

|           | Enciphered image |           |          |             |            |               |  |  |  |
|-----------|------------------|-----------|----------|-------------|------------|---------------|--|--|--|
| Image     | Sp               | atial Don | nain     | FrFT Domain |            |               |  |  |  |
|           | Cat              | Baker     | Logistic | Cat-FrFT    | Baker-FrFT | Logistic-FrFT |  |  |  |
| Cameraman | 0                | 0         | 0        | 0           | 0.0681     | 0.0680        |  |  |  |
| Peppers   | 0                | 0         | 0        | 0           | 0.4517     | 0.4516        |  |  |  |
| Boat      | 0                | 0         | 0        | 0           | 0.4591     | 0.4590        |  |  |  |

### TABLE 7. Irregular deviation between source and enciphered images using the different proposed chaotic maps in the spatial and FrFT domains.

|           | Enciphered image   |        |             |            |               |        |  |  |  |
|-----------|--------------------|--------|-------------|------------|---------------|--------|--|--|--|
| Image     | Cat Baker Logistic |        | FrFT Domain |            |               |        |  |  |  |
|           |                    |        | Cat-FrFT    | Baker-FrFT | Logistic-FrFT |        |  |  |  |
| Cameraman | 0.7166             | 0.7139 | 0.00180     | 0.7125     | 0.7299        | 0.7176 |  |  |  |
| Peppers   | 0.8232             | 0.8296 | 0.000208    | 0.7623     | 0.7623        | 0.7579 |  |  |  |
| Boat      | 0.8010             | 0.8017 | 0.000203    | 0.7711     | 0.7711        | 0.7645 |  |  |  |

#### TABLE 8. NPCR values between the two encrypted images using the different proposed chaotic maps in the spatial and FrFT domains.

|           | Enciphering scheme |             |          |             |            |               |  |  |  |  |
|-----------|--------------------|-------------|----------|-------------|------------|---------------|--|--|--|--|
| Image     | SI                 | patial Doma | in       | FrFT Domain |            |               |  |  |  |  |
|           | Cat                | Baker       | Logistic | Cat-FrFT    | Baker-FrFT | Logistic-FrFT |  |  |  |  |
| Cameraman | 99.0601            | 98.8461     | 99.3518  | 99.9105     | 98.9429    | 98.9665       |  |  |  |  |
| Peppers   | 99.4175            | 99.4221     | 99.4720  | 99.4286     | 99.5262    | 99.5032       |  |  |  |  |
| Boat      | 99.0589            | 99.0467     | 99.1470  | 99.0383     | 99.1734    | 99.1761       |  |  |  |  |

# TABLE 9. UACI values between the two encrypted images using the different proposed chaotic maps in the spatial and FrFT domains.

|           | Enciphering scheme |             |          |             |               |         |  |  |  |  |
|-----------|--------------------|-------------|----------|-------------|---------------|---------|--|--|--|--|
| Image     | SI                 | patial Doma | in       | FrFT Domain |               |         |  |  |  |  |
|           | Cat Baker Logistic |             | Cat-FrFT | Baker-FrFT  | Logistic-FrFT |         |  |  |  |  |
| Cameraman | 27.8645            | 25.8819     | 24.6636  | 28.0218     | 25.9371       | 25.1708 |  |  |  |  |
| Peppers   | 24.2452            | 24.0829     | 22.0482  | 24.4607     | 24.2046       | 22.2943 |  |  |  |  |
| Boat      | 21.8402            | 22.0848     | 20.2863  | 21.7849     | 22.3703       | 20.3304 |  |  |  |  |

| Imaga     | Cipher        | PSNR (dB) |         |         |         |        |  |  |  |
|-----------|---------------|-----------|---------|---------|---------|--------|--|--|--|
| Image     | Cipilei       | 0.01      | 0.05    | 0.1     | 0.15    | 0.20   |  |  |  |
|           | Cat-FrFT      | 9.8348    | 8.9174  | 8.2511  | 7.8289  | 7.5321 |  |  |  |
| Cameraman | Baker-FrFT    | 20.3842   | 13.8885 | 11.5520 | 10.3371 | 9.5591 |  |  |  |
|           | Logistic-FrFT | 20.3791   | 13.9026 | 11.5322 | 10.2972 | 9.5437 |  |  |  |
|           | Cat-FrFT      | 9.9372    | 8.9437  | 8.2709  | 7.8607  | 7.5646 |  |  |  |
| Peppers   | Baker-FrFT    | 18.8286   | 13.6450 | 11.4502 | 10.3256 | 9.6391 |  |  |  |
|           | Logistic-FrFT | 18.8387   | 13.6338 | 11.4813 | 10.3611 | 9.6252 |  |  |  |
|           | Cat-FrFT      | 9.3670    | 8.5187  | 7.9358  | 7.5784  | 7.3166 |  |  |  |
| Boat      | Baker-FrFT    | 19.5130   | 13.7715 | 11.5617 | 10.4126 | 9.6832 |  |  |  |
|           | Logistic-FrFT | 19.5278   | 13.7582 | 11.5371 | 10.4276 | 9.6639 |  |  |  |

TABLE 10. PSNR results of the deciphered images in the existence of channel noise for various chaotic maps in the FrFT domain.

and to measure the performance efficiency of the proposed confusion-based ciphering scheme in the existence of channel noise (with zero mean ( $\mu$ ) and different noise variances ( $\sigma^2$ )) during the deciphering mechanism.

## A. PEAK SIGNAL-TO-NOISE RATIO

The deciphering mechanism efficiency is tested by the PSNR between the original and decrypted images based on pixel differences. It is formulated as [38]:

$$PSNR = 10 \log \frac{(255)^2}{\sum_{i=0}^{W-1} \sum_{j=0}^{H-1} [f_1(i,j) - f_2(i,j)]^2}$$
(20)

where  $f_1(i, j)$  and  $f_2(i, j)$  are, respectively, the gray level values of the pixels at the  $i^{\text{th}}$  row and  $j^{\text{th}}$  column of the  $W \times H$  original and decrypted images. For the decrypted images, a higher value of the PSNR is needed for utmost noise invulnerability. The PSNR values for several decrypted images with respect to their corresponding images have been calculated. The PSNR computed results of the three test images are introduced in Tables 10 and 11, where the parameters  $\mu$  and  $\sigma^2$  in the presented tables are the mean and variance of the existing noise, respectively. The PSNR results for the deciphered images are decreased, when the noise variance values are increased for all chaotic maps. The PSNR values for the Baker-FrFT and the Logistic-FrFT schemes are greater than the those for the Cat-FrFT scheme. The test results demonstrate that the Cat-FrFT scheme is more susceptible to channel noise. Therefore, it may be suitable for the channel-noise-free case. The Baker-FrFT and the Logistic-FrFT schemes can work efficiently in the noisy channel state due to their high robustness to channel noise.

## **B. THE STRUCTURAL SIMILARITY INDEX**

The structural similarity (SSIM) index is widely used to measure the similarity between two images and for evaluating the performance efficiency of the deciphered process. The resultant SSIM index is a decimal value in [-1,1], where 1 means identical images. It is computed as follows [38]:

$$SSIM_{R/G/B}(x, y \mid w) = \frac{(2\bar{w}_x \bar{w}_y + C_1)(2\sigma_{w_x w_y} + C_2)}{(\bar{w}_x^2 + \bar{w}_y^2 + C_1)(\sigma_{w_x}^2 + \sigma_{w_y}^2 + C_2)}$$
(21)

where  $\bar{w}_x$  represents the mean value of  $w_x$  region, while  $\bar{w}_y$  is the mean value of  $w_y$  region.  $C_1$  and  $C_2$  are constants.  $\sigma_{w_x w_y}$ denotes the covariance between the two regions,  $\sigma_{w_x}^2$  denotes the variance of  $\sigma_{w_y}^2$ .

For the decrypted images, a higher SSIM value is preferred, which is a mandatory requirement for better noise immunity. The computed results of SSIM for the test images are introduced in Table 12. In all test cases, it was found that the SSIM results for the deciphered images are decreased when the variance values are increased for all chaotic maps, but the results are still accepted at different noise variances. Therefore, the introduced results confirm the performance efficiency of the suggested confusion-based image ciphering scheme in the existence of channel noise. The SSIM values for the Baker-FrFT and the Logistic-FrFT schemes are greater than the those for the Cat-FrFT scheme. Thus, the Baker-FrFT and the Logistic-FrFT schemes are highly efficient in the existence of channel noise. Thence, they may be used efficiently over a noisy channel.

### C. FEATURE SIMILARITY INDEX

To calculate the local similarity between the main and deciphered images, the FSIM can be utilized. It is calculated as follows [38]:

$$FSIM_{R/G/B} = \frac{\sum_{x \in \Omega} S_L(x) \cdot PC_m(x)}{\sum_{x \in \Omega} PC_m(x)}$$
(22)

where  $S_L(x)$  defines the estimated similarity between the two images.  $\Omega$  denotes the spatial domain for the image, while  $PC_m(x)$  is an estimate for the phase congruency.

For the decrypted images, a larger FSIM value is preferred, which is a mandatory requirement for better noise immunity. The computed results of FSIM for the test images are introduced in Table 13. In all test cases, it is found that the FSIM results for all deciphered images are accepted at different noise variances. It is also found that the FSIM values for the deciphered images are decreased, when the variance values are increased for all chaotic maps, but the results are still accepted at different noise variances. The FSIM values for the Baker-FrFT and the Logistic-FrFT schemes are greater than the FSIM values for the Cat-FrFT scheme. It is observed that the results ensure again that the suggested Baker-FrFT and Logistic-FrFT ciphering schemes are not affected greatly

| Image     | Cipher        |      | Ι    | Deciphered imag                       | ge   |      |
|-----------|---------------|------|------|---------------------------------------|------|------|
| mage      | Cipiter       | 0.01 | 0.05 | 0.1                                   | 0.15 | 0.20 |
|           | Cat-FrFT      |      | -    | -                                     |      | -    |
| Cameraman | Baker-FrFT    |      | -    | -                                     | -    |      |
|           | Logistic-FrFT |      |      |                                       |      | A    |
|           | Cat-FrFT      |      |      |                                       |      | 121  |
| Peppers   | Baker-FrFT    |      |      |                                       |      |      |
|           | Logistic-FrFT |      |      |                                       |      | 1Ť   |
|           | Cat-FrFT      |      |      | A A A                                 |      |      |
| Boat      | Baker-FrFT    |      |      | A A A A A A A A A A A A A A A A A A A |      |      |
|           | Logistic-FrFT |      |      |                                       |      |      |

## TABLE 11. Deciphered images in the existence of channel noise for different chaotic maps in the FrFT domain.

| TABLE 12. SSIM results of the deciphered images in the existence of |
|---|
| channel noise for various chaotic maps in the FrFT domain.          |

| Image     | Scheme        | SSIM   |        |        |        |        |  |
|-----------|---------------|--------|--------|--------|--------|--------|--|
|           | Scheme        | 0.01   | 0.05   | 0.1    | 0.15   | 0.20   |  |
| Cameraman | Cat-FrFT      | 0.1325 | 0.0533 | 0.0361 | 0.0286 | 0.0229 |  |
|           | Baker-FrFT    | 0.5660 | 0.3151 | 0.2381 | 0.2003 | 0.1733 |  |
|           | Logistic-FrFT | 0.5641 | 0.3164 | 0.2384 | 0.1973 | 0.1717 |  |
| Peppers   | Cat-FrFT      | 0.1084 | 0.0454 | 0.0316 | 0.0257 | 0.0228 |  |
|           | Baker-FrFT    | 0.5987 | 0.3376 | 0.2490 | 0.2047 | 0.1782 |  |
|           | Logistic-FrFT | 0.5999 | 0.3381 | 0.2494 | 0.2065 | 0.1781 |  |
| Boat      | Cat-FrFT      | 0.0829 | 0.0384 | 0.0309 | 0.0235 | 0.0206 |  |
|           | Baker-FrFT    | 0.6281 | 0.3802 | 0.2849 | 0.2355 | 0.2078 |  |
|           | Logistic-FrFT | 0.6296 | 0.3804 | 0.2848 | 0.2395 | 0.2061 |  |

by channel noise. Therefore, they may be implemented sufficiently in severe channel noise states.

## **VI. EFFECT OF FRFT ANGLES**

The FrFT angles are considered as additional keys for encryption. So, we tested the encryption process with different FrFT angles. Table 14 shows the simulation results of the encryption quality metrics for the Logistic-FrFT scheme on the Cameraman image. It is noticed that the correlation, histogram deviation, and irregular deviation results are appreciated at different FrFT angles. So, the parameters of the FrFT can be used as additional keys for encryption and achieving reliable cybersecurity for robust image communication. Table 15 presents the subjective encryption and decryption results of the test images at different FrFT angles. It is

| TABLE 13. FSIM results of the deciphered images in the existence of |  |
|---|--|
| channel noise for the different chaotic maps in the FrFT domain.    |  |
|   |  |
|   |  |

| Image     | Scheme        | FSIM    |        |        |        |        |  |
|-----------|---------------|---------|--------|--------|--------|--------|--|
|           |               | 0.01    | 0.05   | 0.1    | 0.15   | 0.20   |  |
| Cameraman | Cat-FrFT      | 0.5123  | 0.4689 | 0.4475 | 0.4347 | 0.4304 |  |
|           | Baker-FrFT    | 0.8355  | 0.6730 | 0.5996 | 0.5601 | 0.5322 |  |
|           | Logistic-FrFT | 0.83596 | 0.6726 | 0.6031 | 0.5596 | 0.5325 |  |
| Peppers   | Cat-FrFT      | 0.5778  | 0.5073 | 0.4714 | 0.4518 | 0.4398 |  |
|           | Baker-FrFT    | 0.8333  | 0.6651 | 0.5914 | 0.5455 | 0.5177 |  |
|           | Logistic-FrFT | 0.8331  | 0.6654 | 0.5881 | 0.5444 | 0.5177 |  |
| Boat      | Cat-FrFT      | 0.5152  | 0.4918 | 0.4802 | 0.4697 | 0.4664 |  |
|           | Baker-FrFT    | 0.8510  | 0.7062 | 0.6350 | 0.5962 | 0.5691 |  |
|           | Logistic-FrFT | 0.8533  | 0.7063 | 0.6374 | 0.5959 | 0.5667 |  |

also shown that the encryption and decryption results of the Logistic-FrFT scheme for the test images are appreciated and recommended. It is also noticed that the FrFT-based encryption process has good key sensitivity results, where the decryption process is not valid when introducing a little difference in the FrFT angle.

## VII. COMPARATIVE ANALYSIS AND DISCUSSIONS

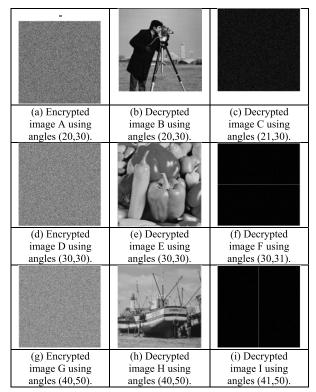
To verify and ensure the proposed encryption schemes effectiveness for reliable image transmission over insecure channels, various experiments have been carried out to compare the statistical security based on NPCR, correlation coefficient, PSNR, UACI, and entropy [4, 6-8, 11-18, 21-23].

The comparative study between the proposed encryption schemes and the traditional schemes is performed on the color

| Angles of<br>FrFT | $r_{xy}$                   | $H_D$                     | $D_I$                     |
|-------------------|----------------------------|---------------------------|---------------------------|
| M1(30,20)         | -897.5581×10 <sup>-6</sup> | 68.0771×10 <sup>-3</sup>  | 715.3391×10 <sup>-3</sup> |
| M2(30,30)         | -854.6761×10-6             | 68.0770×10-3              | 713.2111×10 <sup>-3</sup> |
| M3(40,50)         | -392.0038×10 <sup>-3</sup> | 68.0771×10 <sup>-3</sup>  | 715.2905×10 <sup>-3</sup> |
| M4(40,40)         | -152.9726×10 <sup>-6</sup> | 68.0771×10 <sup>-3</sup>  | 714.5004×10 <sup>-3</sup> |
| M5(43,64)         | 6.9893×10 <sup>-3</sup>    | 1.3381                    | 870.7886×10 <sup>-3</sup> |
| M6(20,31)         | -1.3768×10 <sup>-3</sup>   | 1.3384                    | 861.3739×10 <sup>-3</sup> |
| M7(22,37)         | -8.2376×10 <sup>-3</sup>   | 1.3347                    | 874.5637×10 <sup>-3</sup> |
| M8(78,83)         | -1.9829×10 <sup>-3</sup>   | 1.3348                    | 872.3221×10 <sup>-3</sup> |
| M9(45,45)         | -2.5965×10 <sup>-3</sup>   | 1.6738                    | 978.1494×10 <sup>-3</sup> |
| M10(0,10)         | -4.1398×10 <sup>-3</sup>   | 68.0771×10 <sup>-3</sup>  | 717.1124×10 <sup>-3</sup> |
| M11(0,22)         | -1.2992×10 <sup>-3</sup>   | 68.0771×10 <sup>-3</sup>  | 716.8655×10 <sup>-3</sup> |
| M12(0,35)         | -5.3082×10 <sup>-3</sup>   | 1.3343                    | 871.2768×10 <sup>-3</sup> |
| M13(0,40)         | 2.9440×10-3                | 68.07708×10 <sup>-3</sup> | 716.1636×10 <sup>-3</sup> |
| M14(0,73)         | -619.4967×10 <sup>-6</sup> | 1.3359                    | 866.1727×10 <sup>-3</sup> |
| M15(0,95)         | -8.5473×10 <sup>-3</sup>   | 1.3337                    | 871.0174×10 <sup>-3</sup> |
| M16(20,0)         | 1.3339×10 <sup>-3</sup>    | 68.0771×10 <sup>-3</sup>  | 717.4581×10 <sup>-3</sup> |
| M17(34,0)         | 1.4024×10 <sup>-3</sup>    | 68.0770×10 <sup>-3</sup>  | 716.6617×10 <sup>-3</sup> |
| M18(46,0)         | -1.1239×10 <sup>-3</sup>   | 68.0770×10 <sup>-3</sup>  | 716.2322×10 <sup>-3</sup> |
| M19(60,0)         | -3.1264×10 <sup>-3</sup>   | 68.0771×10 <sup>-3</sup>  | 714.8971×10 <sup>-3</sup> |
| M20(82,0)         | -1.7061×10 <sup>-3</sup>   | 68.0771×10 <sup>-3</sup>  | 716.7511×10 <sup>-3</sup> |

 TABLE 14. Encryption quality results for the Logistic-FrFT scheme on the Cameraman image.

| TABLE 15. | Encryption and | decryption with | different FrFT angles. |
|-----------|----------------|-----------------|------------------------|
|-----------|----------------|-----------------|------------------------|



Lena image. The values of entropy, correlation coefficient, NPCR, UACI, and the PSNR results are listed in Table 16

**TABLE 16.** The estimated entropy, correlation coefficient, NPCR and UACI results of the eciphered Lena image and the PSNR (dB) results of the deciphered Lena image for the proposed schemes and the literature-related schemes in [4], [6]–[8], [11]–[18], [20]–[22].

| Scheme            | Entropy | $r_{xy}$ | NPCR  | UACI  | PSNR  |
|-------------------|---------|----------|-------|-------|-------|
| Cat-<br>FrFT      | 7.5937  | -0.0002  | 99.82 | 29.73 | 42.79 |
| Baker-<br>FrFT    | 7.7190  | 0.0017   | 99.76 | 26.48 | 43.28 |
| Logistic-<br>FrFT | 7.7771  | -0.0219  | 99.74 | 27.52 | 43.17 |
| Ref. [4]          | 7.5890  |          |       |       |       |
| Ref. [6]          |         | 0.0013   | 99.58 | 31.02 |       |
| Ref. [7]          |         |          |       |       |       |
| Ref. [8]          |         | 0.1955   |       |       |       |
| Ref. [11]         | 7.6251  | 0.0435   | 99.71 | 33.45 |       |
| Ref. [12]         |         | 0.0985   |       |       |       |
| Ref. [13]         |         | 0.0056   |       |       |       |
| Ref. [14]         |         | 0.0021   | 99.60 | 28.13 |       |
| Ref. [15]         |         | 0.0024   | 99.57 | 27.53 |       |
| Ref. [16]         | 7.7594  | 0.0046   |       |       |       |
| Ref. [17]         |         | 0.0219   |       |       |       |
| Ref. [18]         |         | -0.0064  |       |       |       |
| Ref. [21]         |         | 0.0001   | 99.56 | 31.17 | 41.51 |
| Ref. [22]         |         | 0.0020   | 99.65 | 33.48 |       |
| Ref. [23]         |         | -0.0006  |       |       | 42.88 |

for the proposed and traditional schemes in [4], [6]–[8], [11]–[18], [20]–[22].

We notice that the entropies of the cipherimages for the proposed schemes are closer to 8 compared to those of the other schemes. So, the information leakage during the encryption process can be neglected, ensuring the robustness of the proposed schemes to the entropy attack compared to the other-related schemes. Also, it is obvious that the proposed schemes correlation coefficient values are closer to zero than the other related schemes. In other words, the cipherimage and the plainimage are not correlated. Moreover, the numerical values of NPCR and UACI demonstrate that the proposed ciphering schemes are better in the presence of differential attacks. Furthermore, based on the PSNR values (dB) of the decrypted Lena image using the proposed ciphering schemes, it is noticed that the proposed ciphering schemes are more efficient than the traditional schemes.

#### **VIII. CONCLUSION**

This paper provided an investigation of image encryption using different chaotic maps in spatial and FrFT domains. The parameters of the FrFT are considered as additional keys for encryption. Experimental results and theoretical security analysis proved that the suggested encryption schemes are more secure and effective. Based on the numerical results presented, the proposed encryption schemes demonstrate three advantages. They have a high level of efficiency represented in the confusion property. The enciphered images have good statistical properties. The proposed encryption schemes are immune to noise. Furthermore, it is noticed that the Cat-FrFT scheme is more susceptible to channel noise than the Baker-FrFT and the Logistic-FrFT schemes. Therefore, the Cat-FrFT scheme may be suitable for the channel-noise-free case. However, the Baker-FrFT and the Logistic-FrFT schemes can work efficiently in the cases of channel noise due to their high

robustness to the channel noise. For robust and reliable transmission and storage of digital multimedia data, we intend, as a future work, to develop and implement algorithms that include deep-learning-based cybersecurity mechanisms.

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